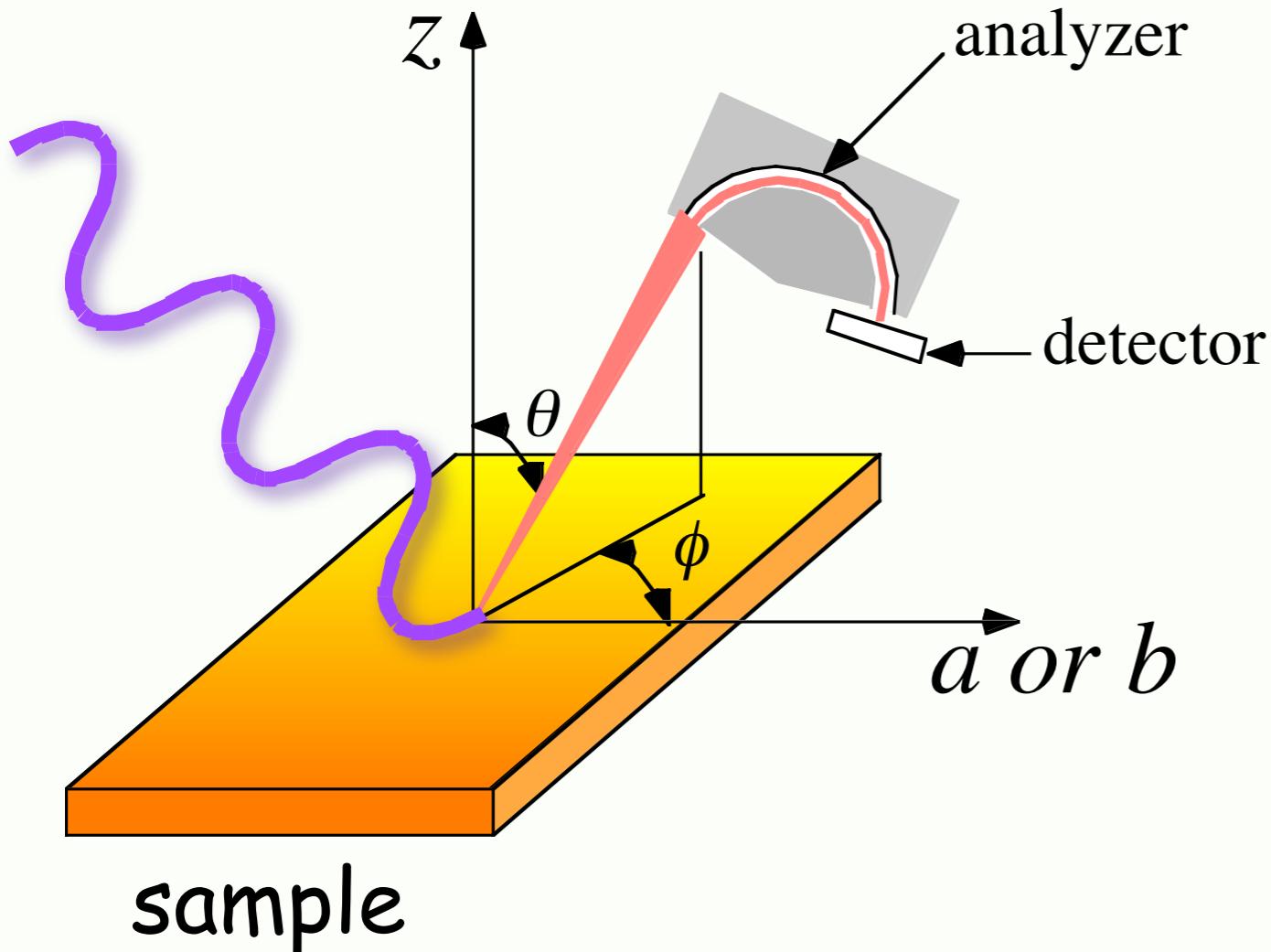


# ARPES part II

Adam Kamiński

Ames Laboratory and Iowa State University

# ARPES experiment



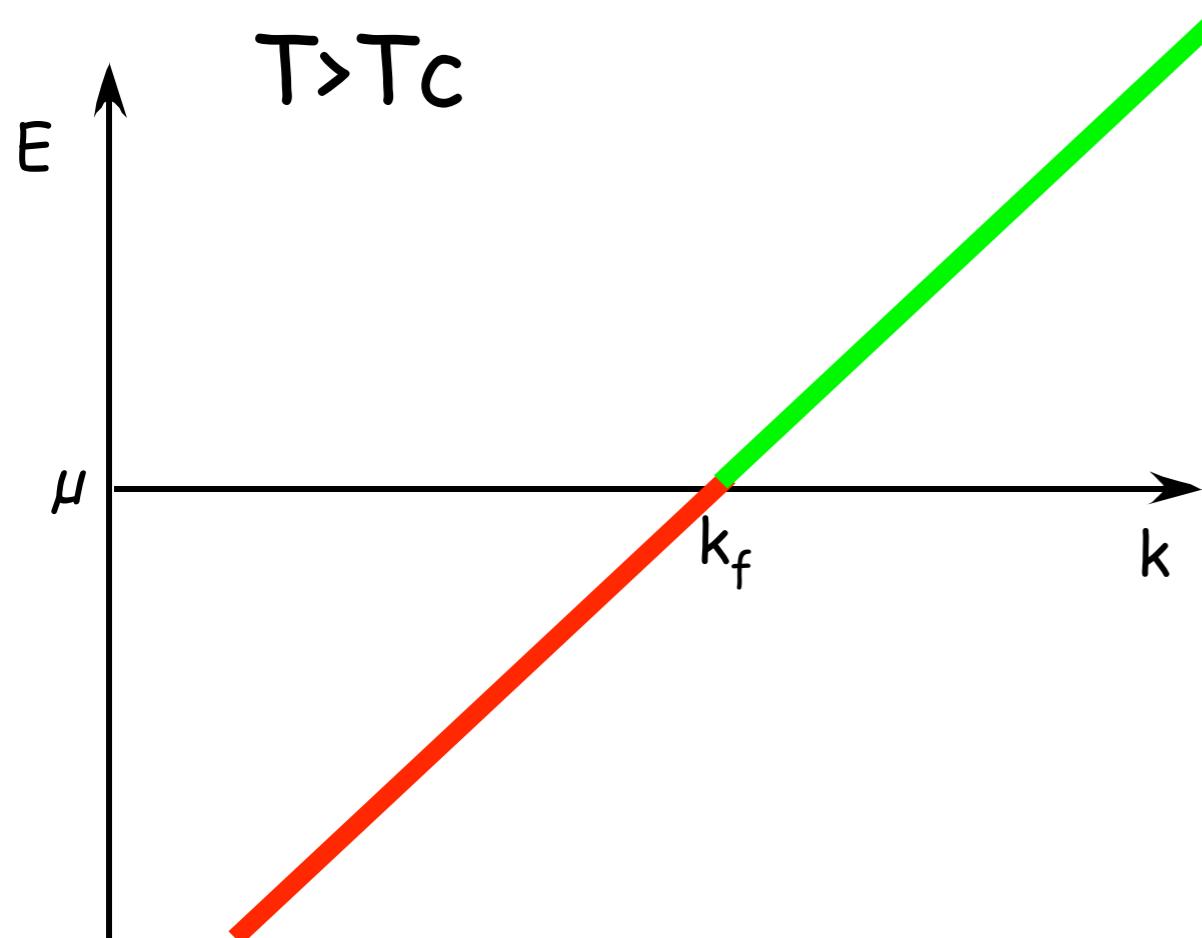
We need:  
binding energy -  $E_b$   
initial momentum -  $k^i$

$$E_b = E - h\nu + W$$

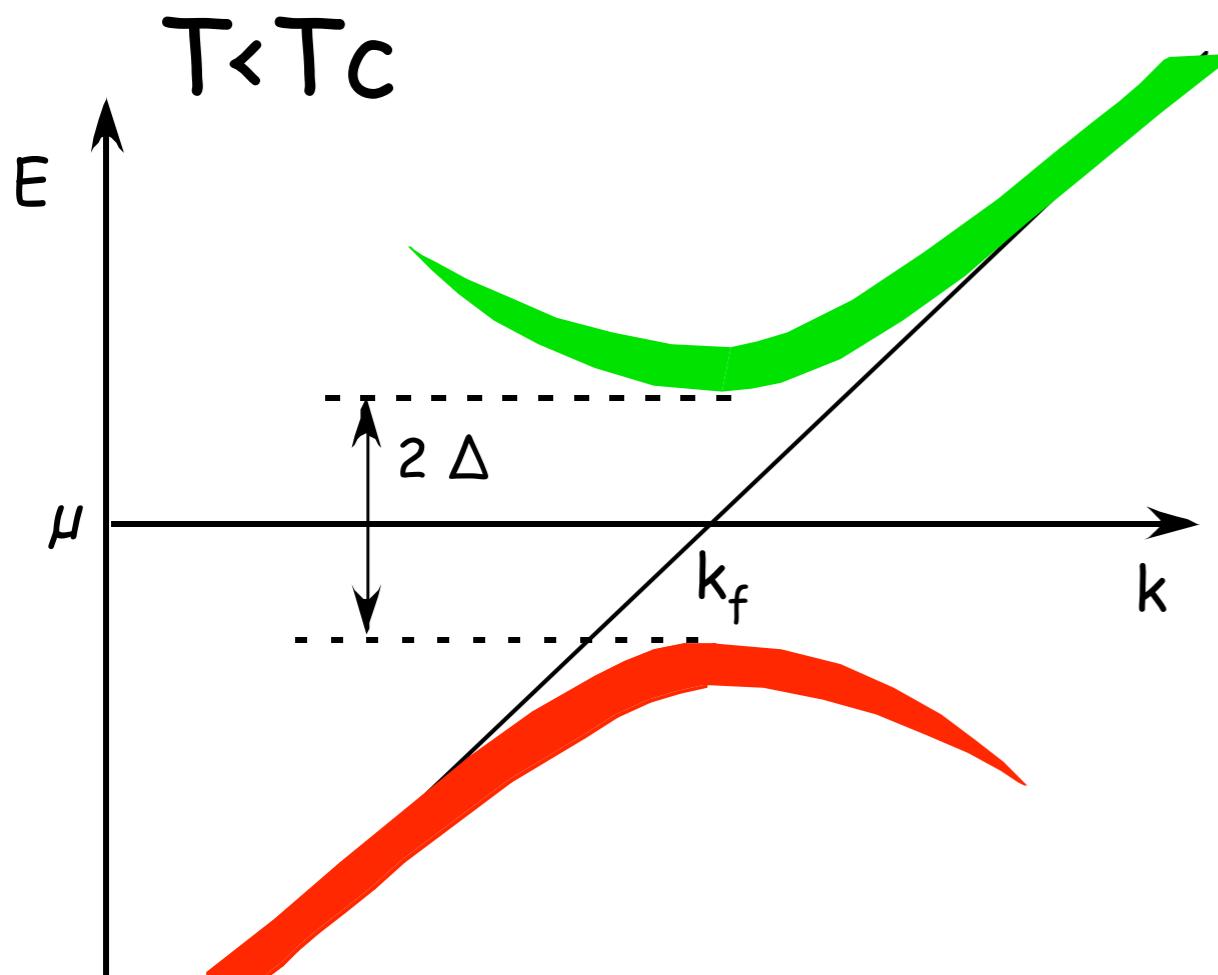
$$k_{||}^i = k_{||}^f = \sqrt{2mE/h^2} \sin\theta$$

$$k_{\perp}^i = k_{\perp}^f - G = \sqrt{2mE/h^2} \cos\theta - G$$

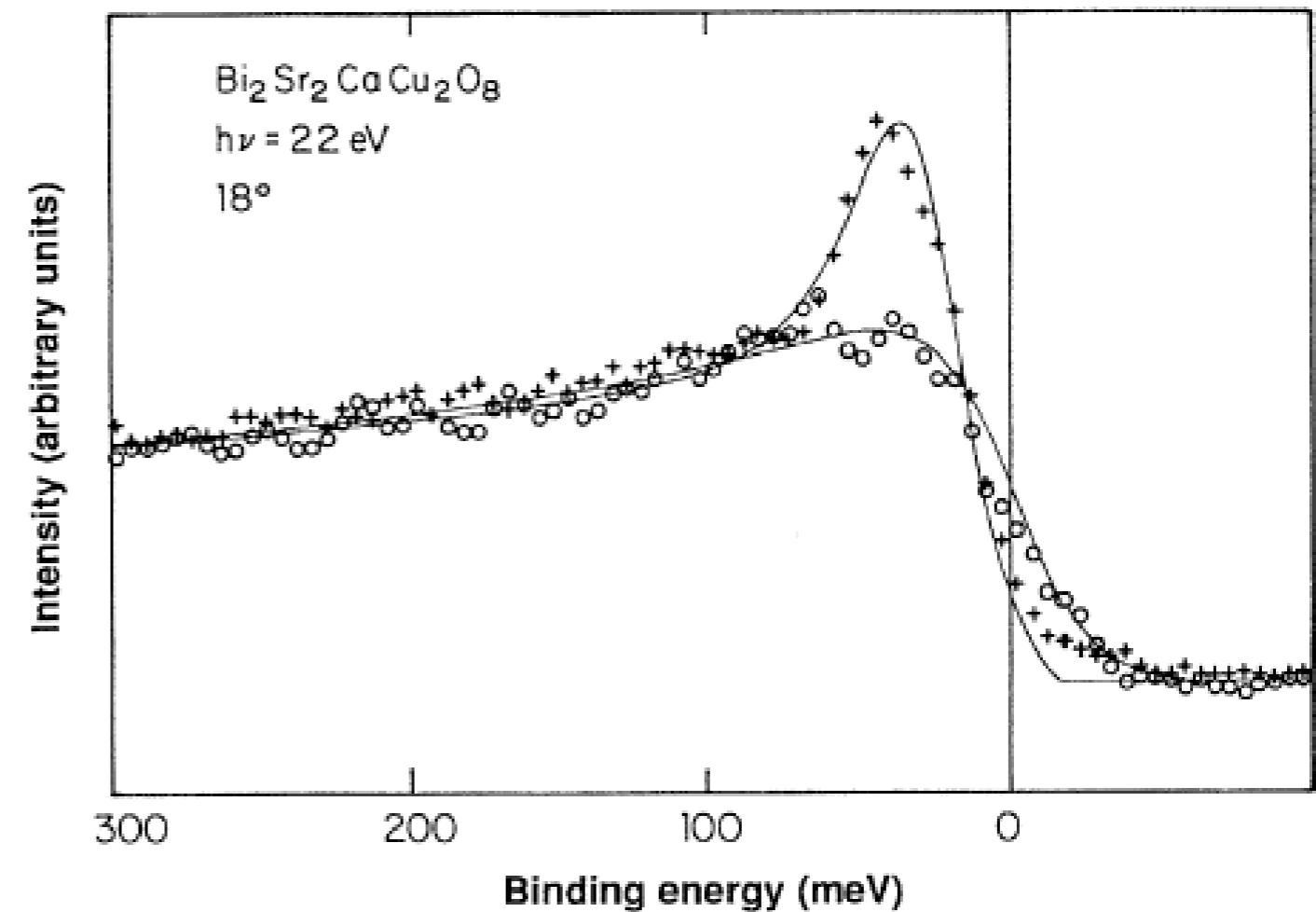
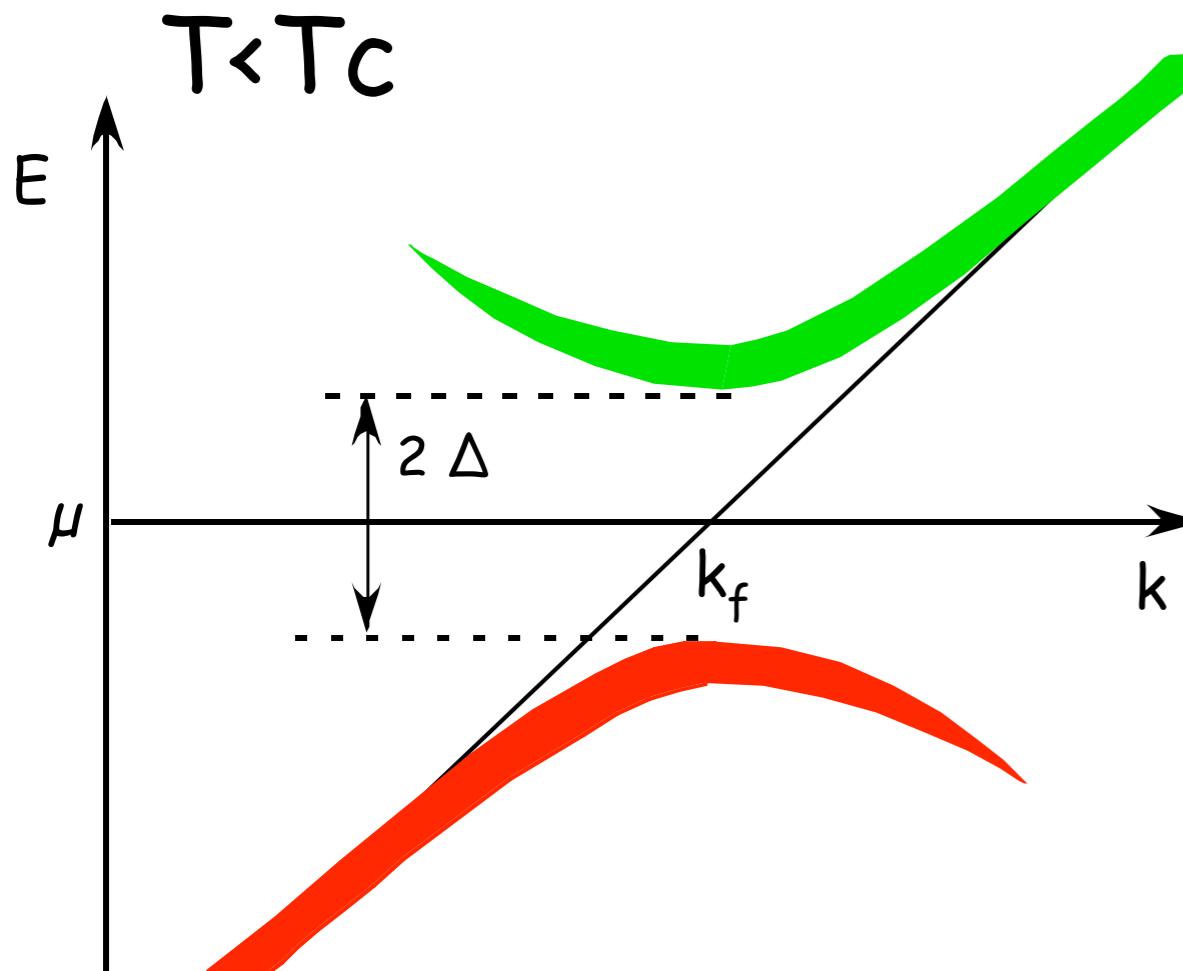
# Energy gaps (superconducting etc...)



# Energy gaps (superconducting etc...)

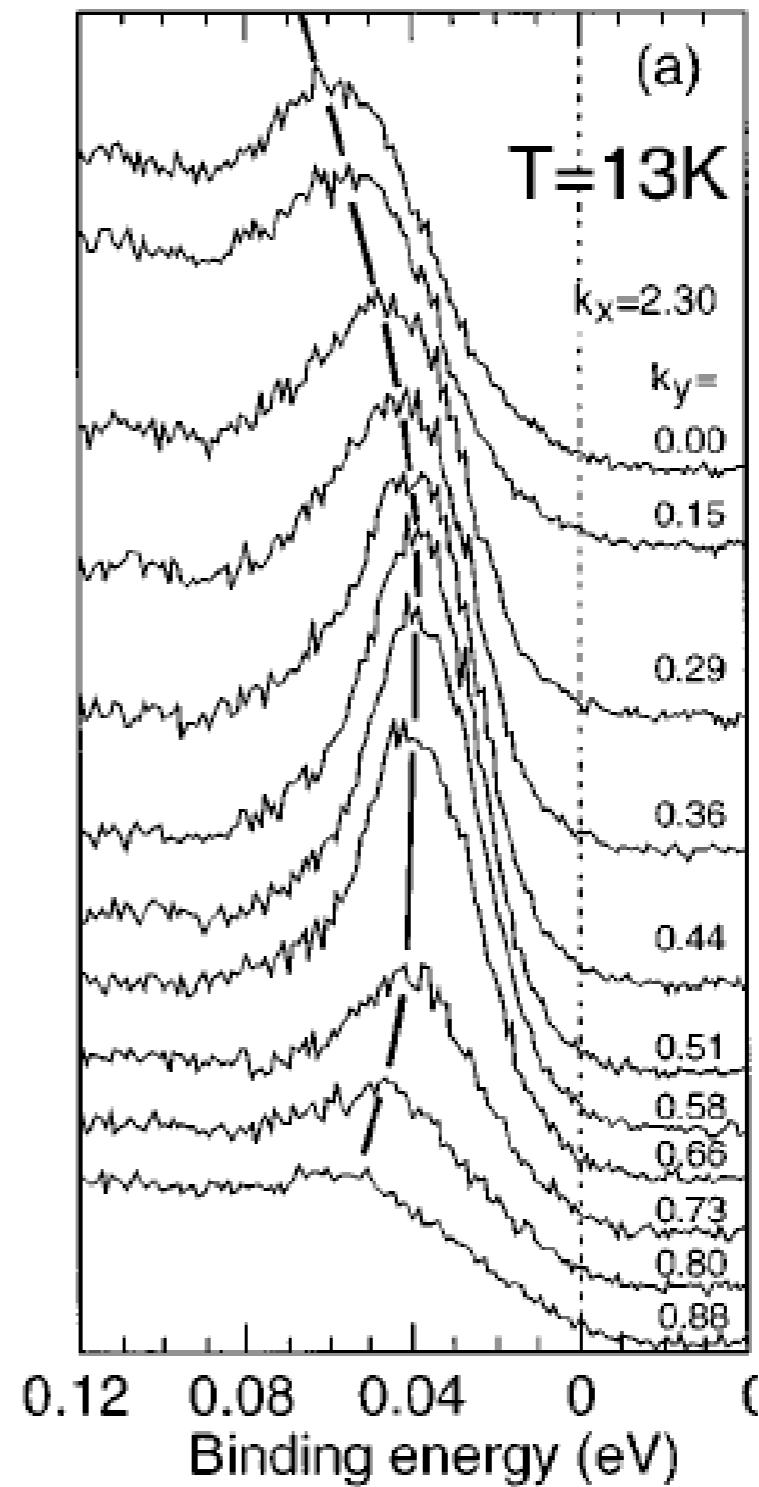
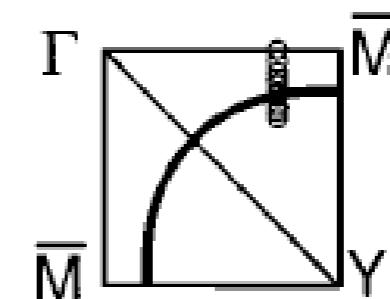
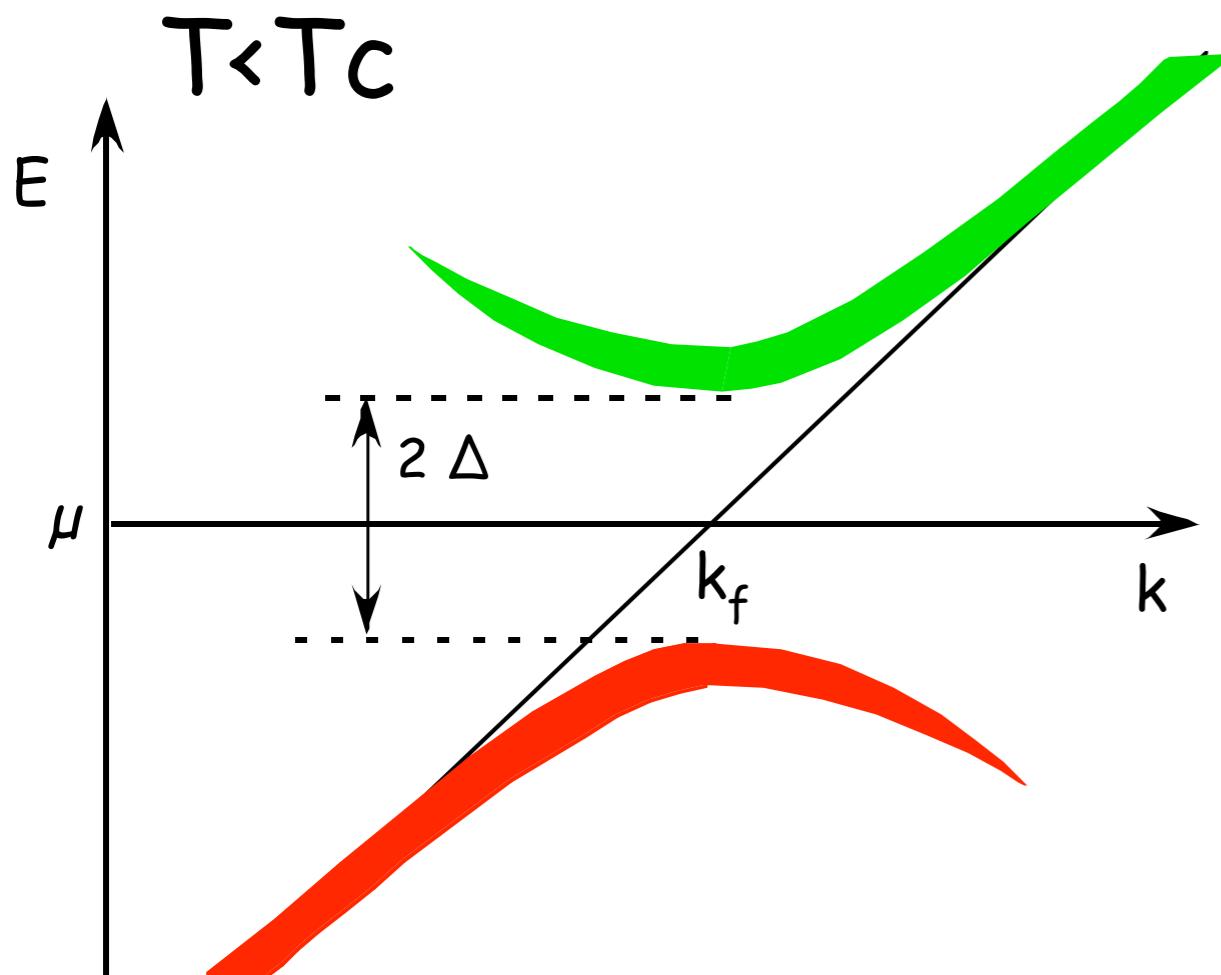


# Energy gaps (superconducting etc...)

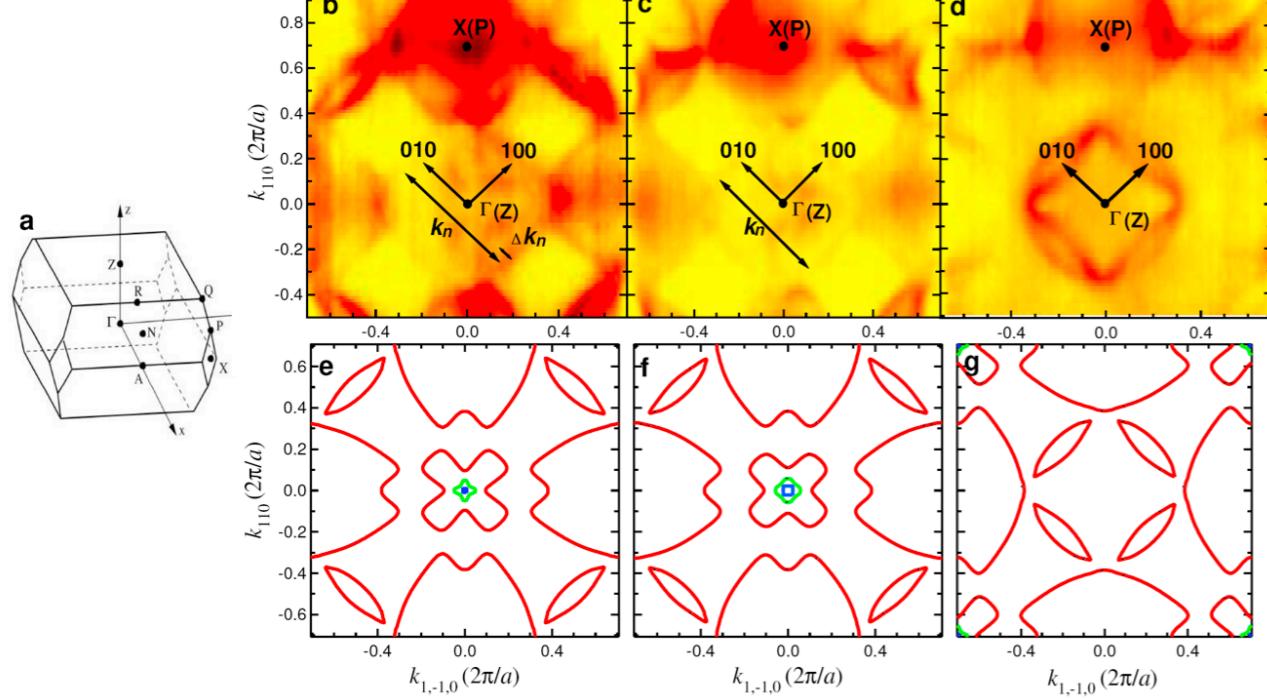


C. G. Olson *et al.*, Science **245**, 731-733 (1989)

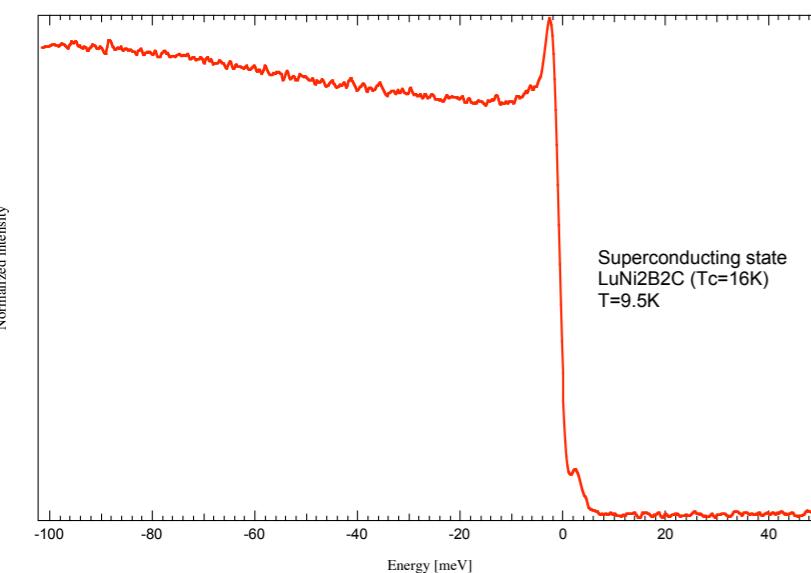
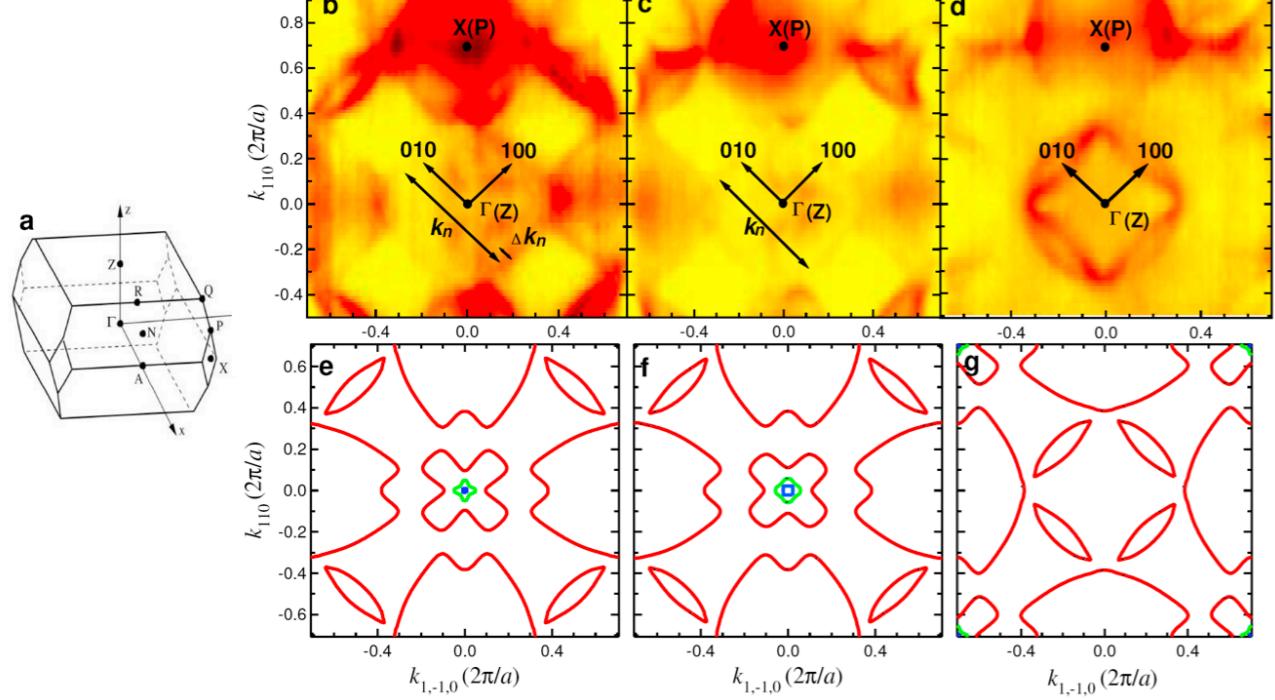
# Energy gaps (superconducting etc...)



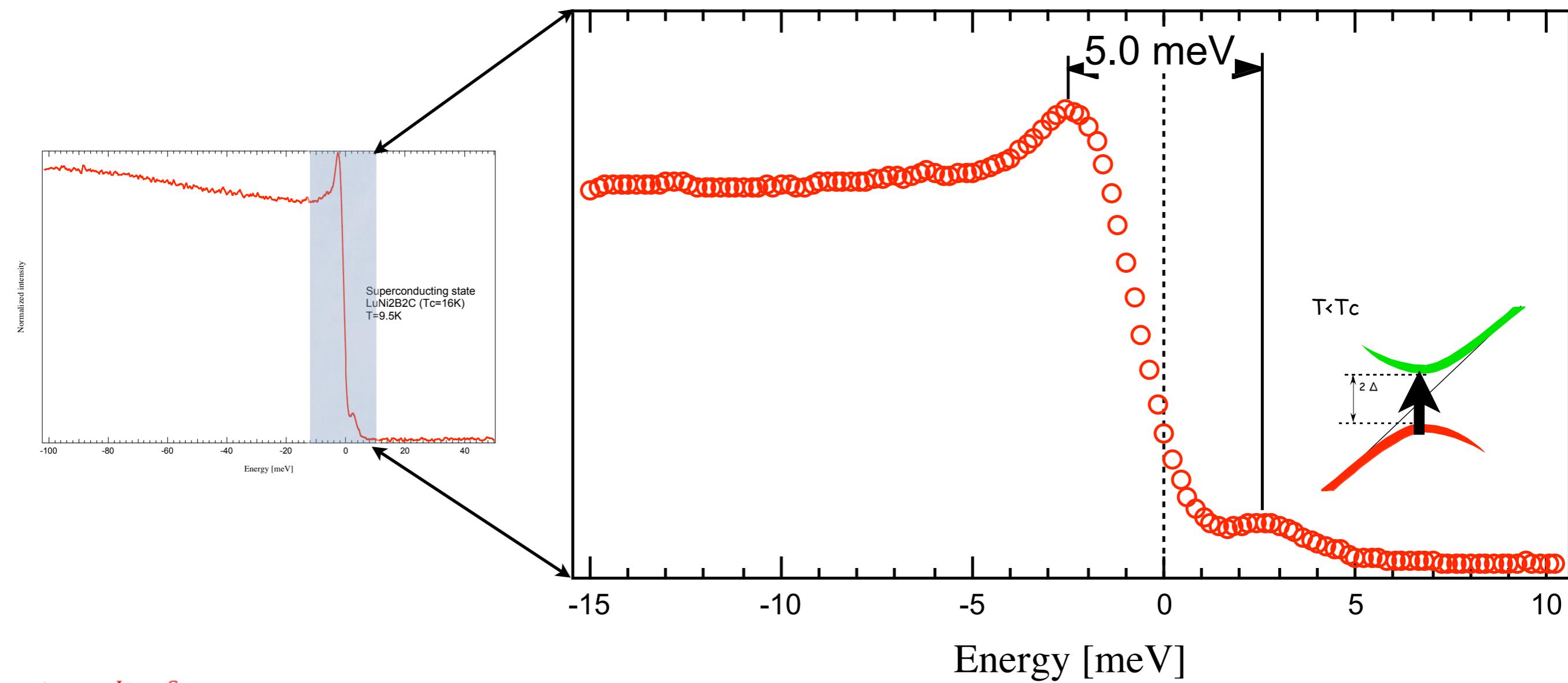
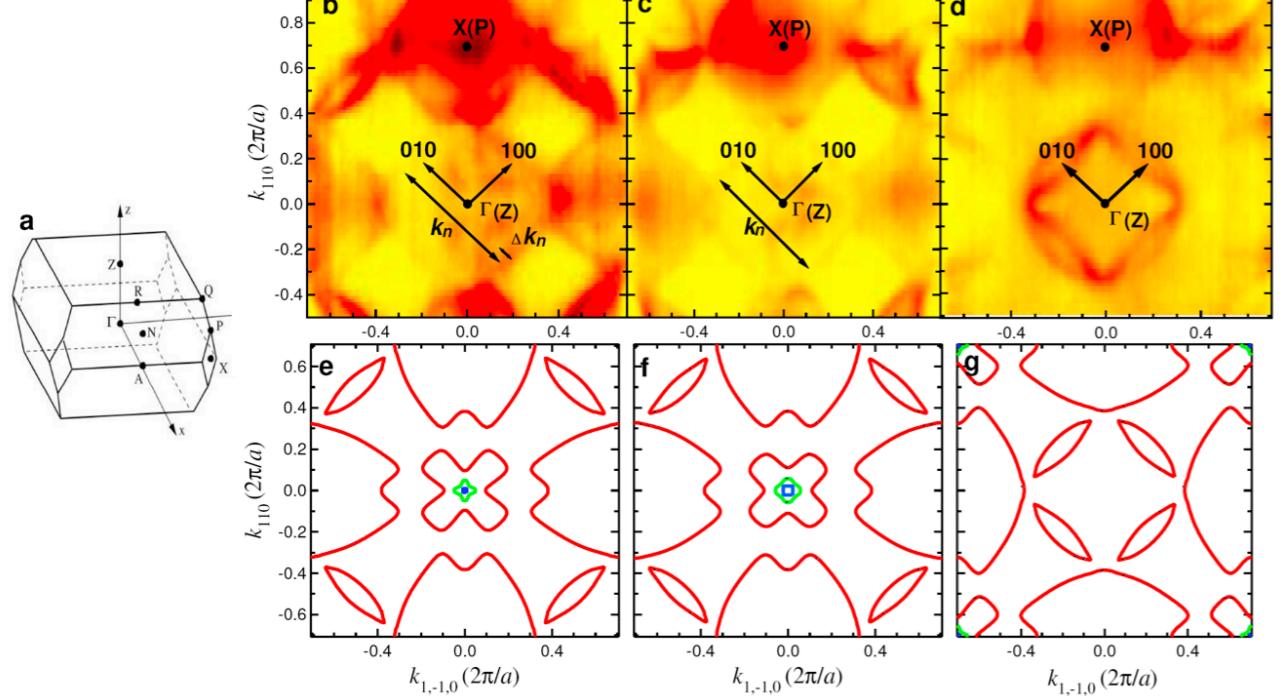
# RNi<sub>2</sub>B<sub>2</sub>C



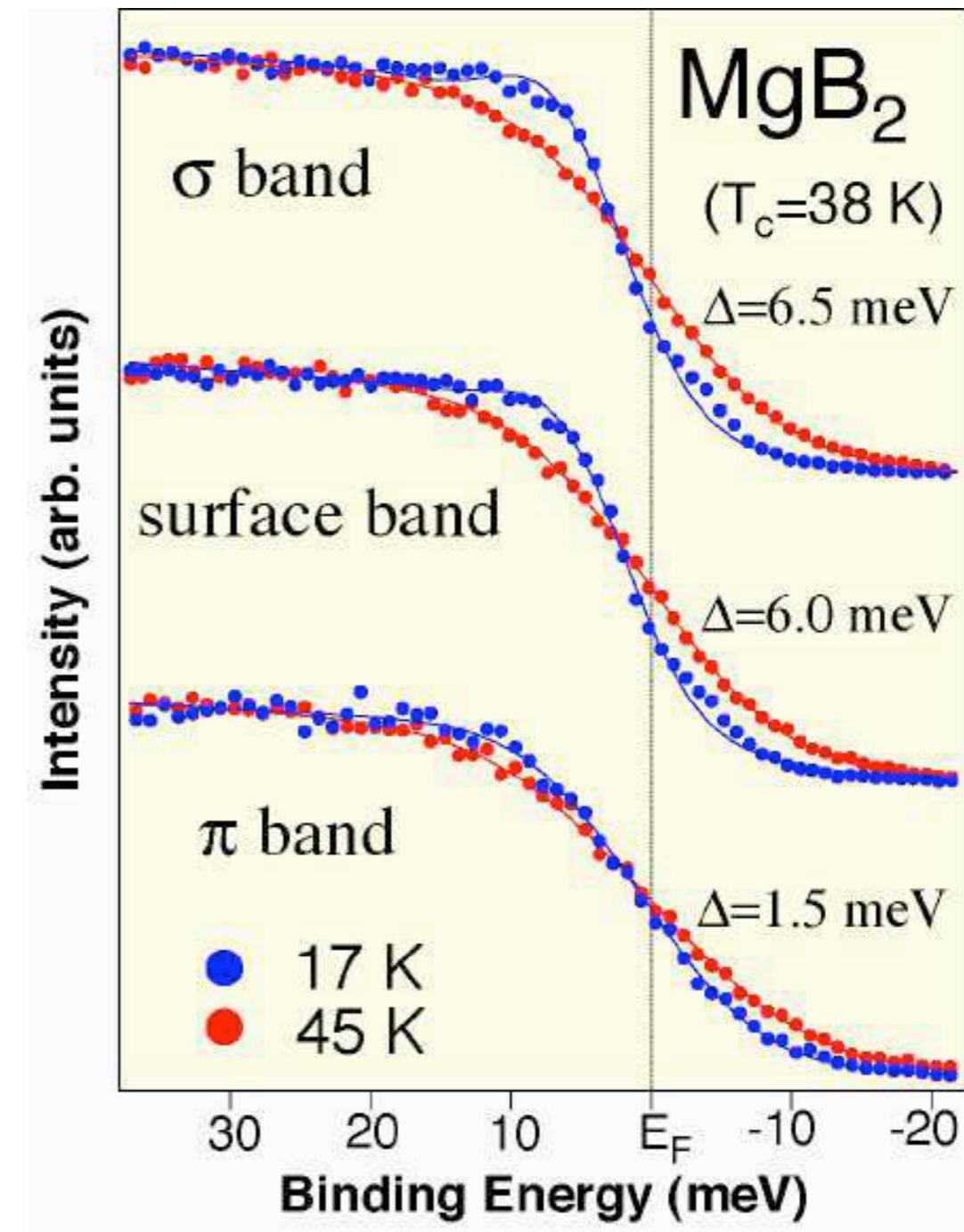
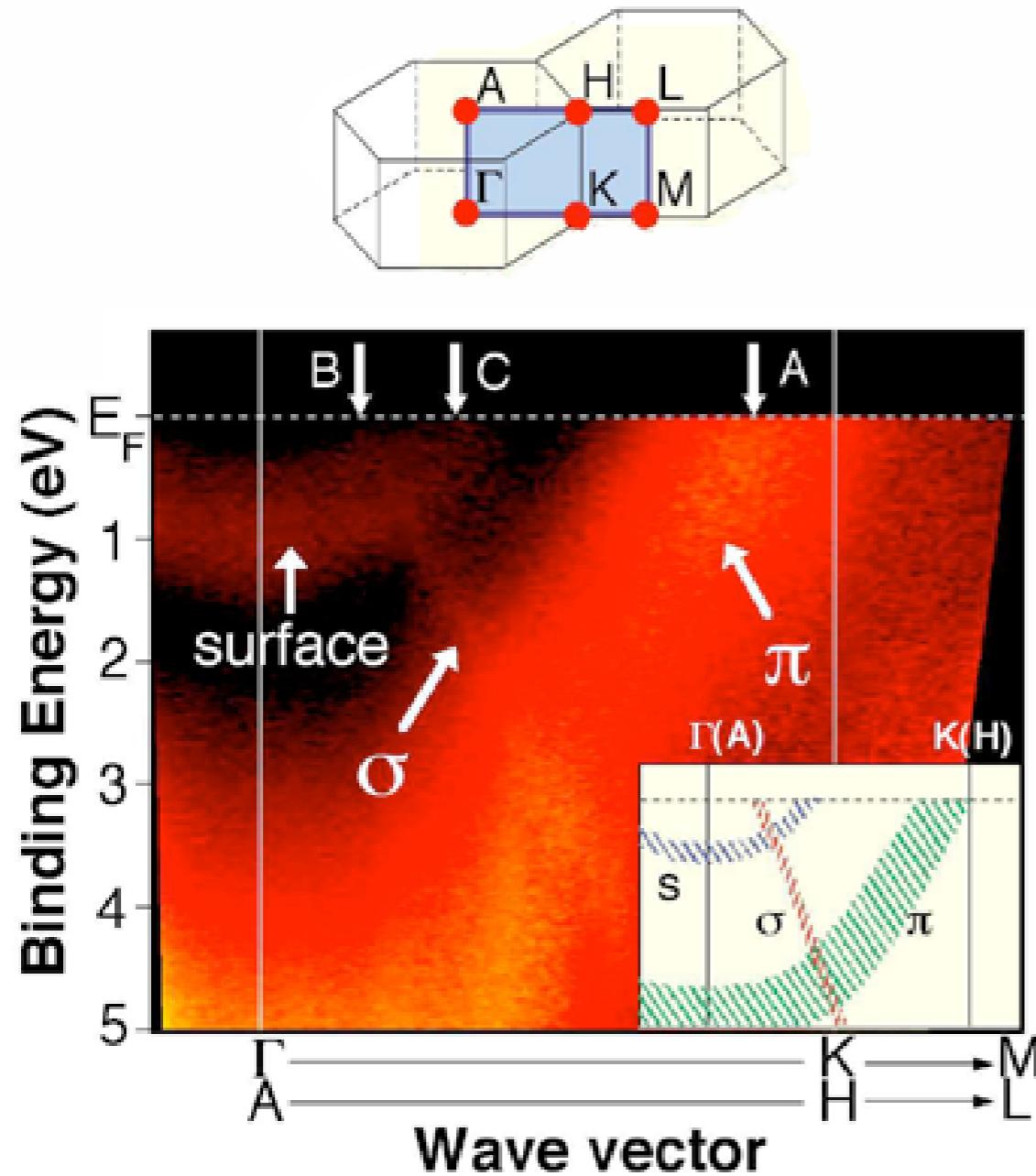
# RNi<sub>2</sub>B<sub>2</sub>C



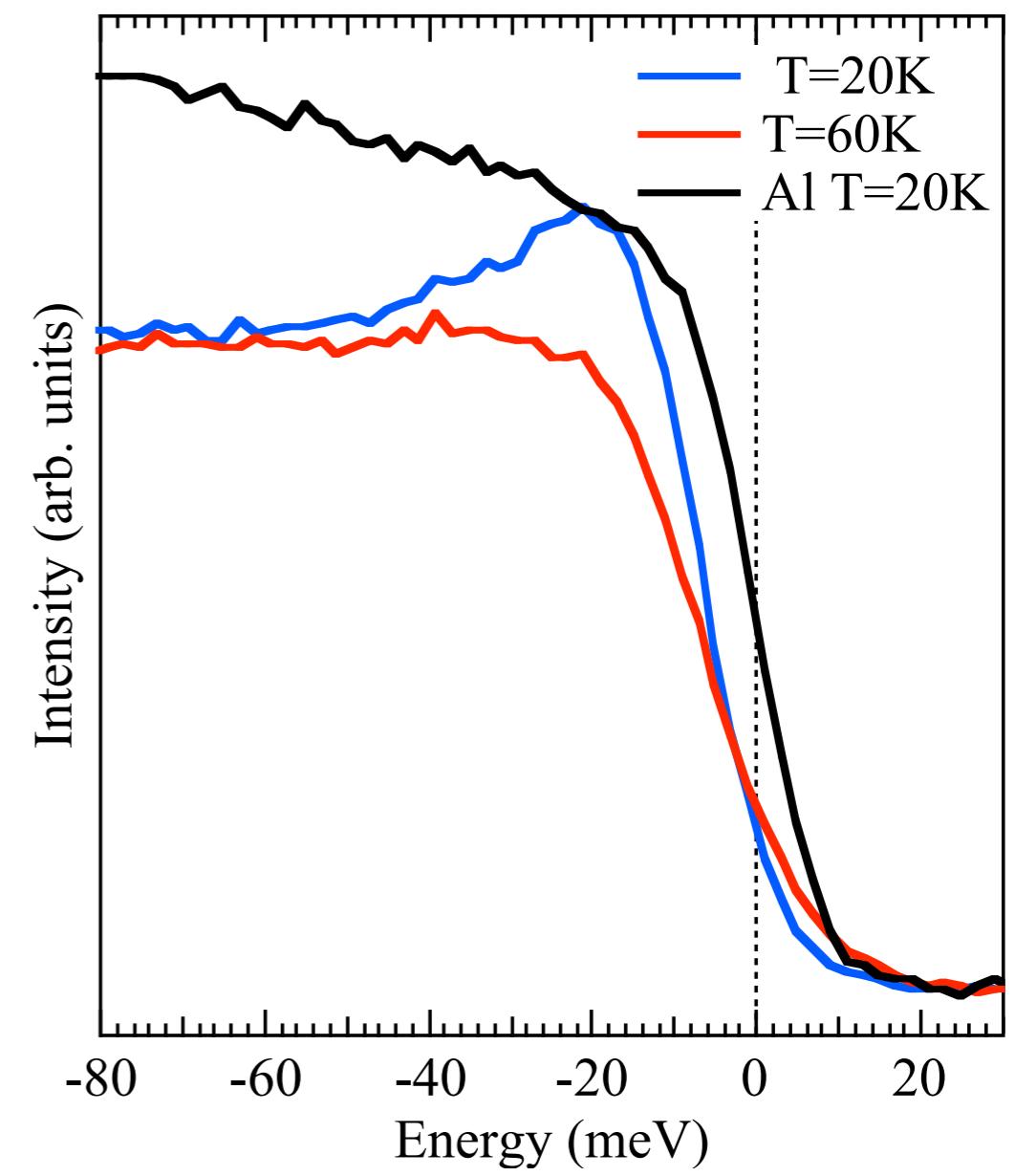
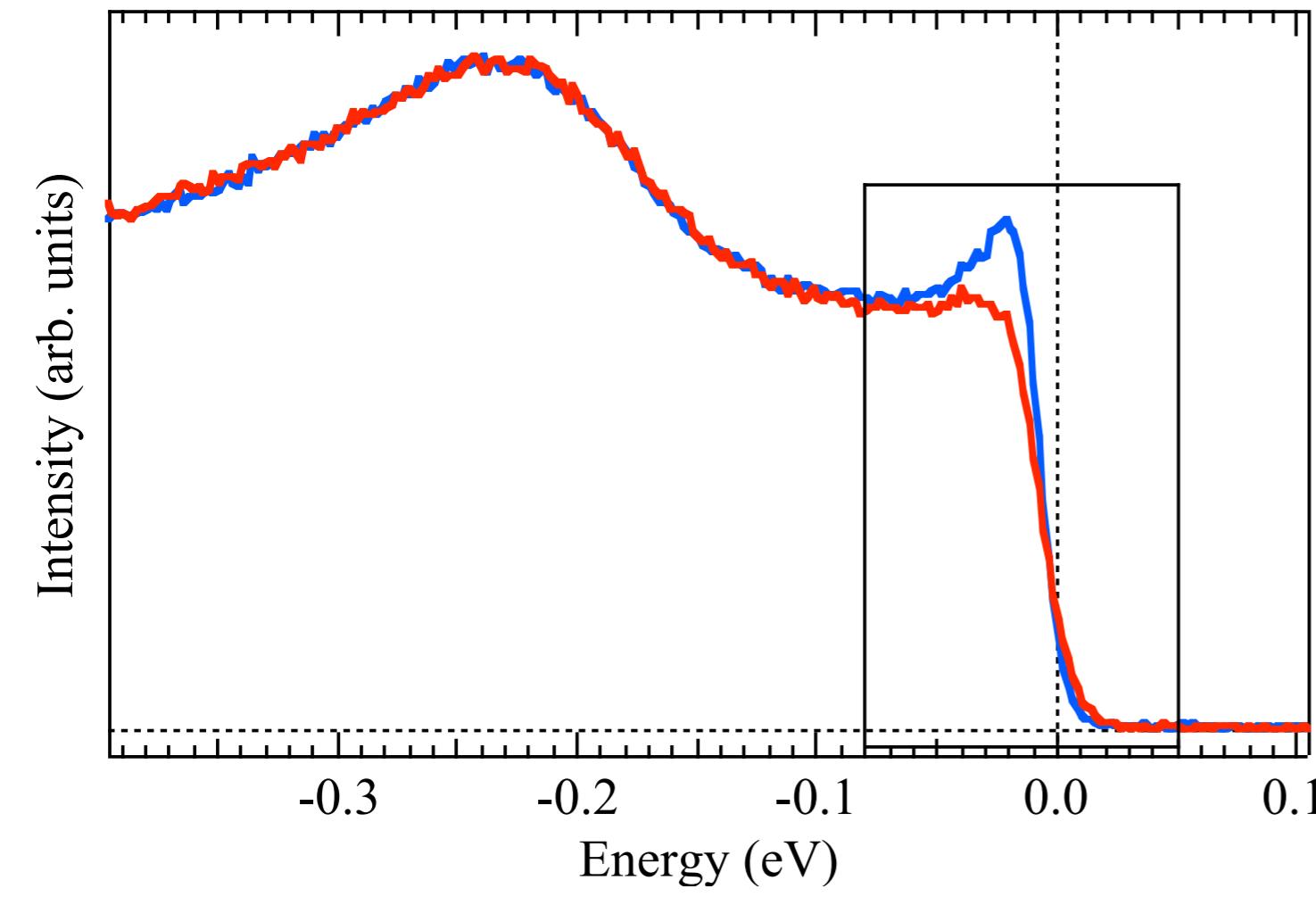
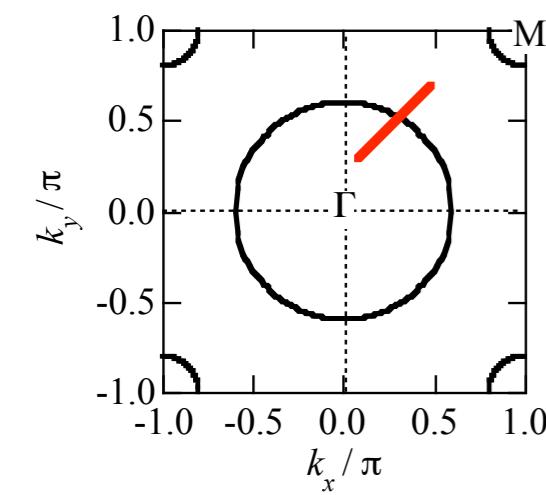
# RNi<sub>2</sub>B<sub>2</sub>C



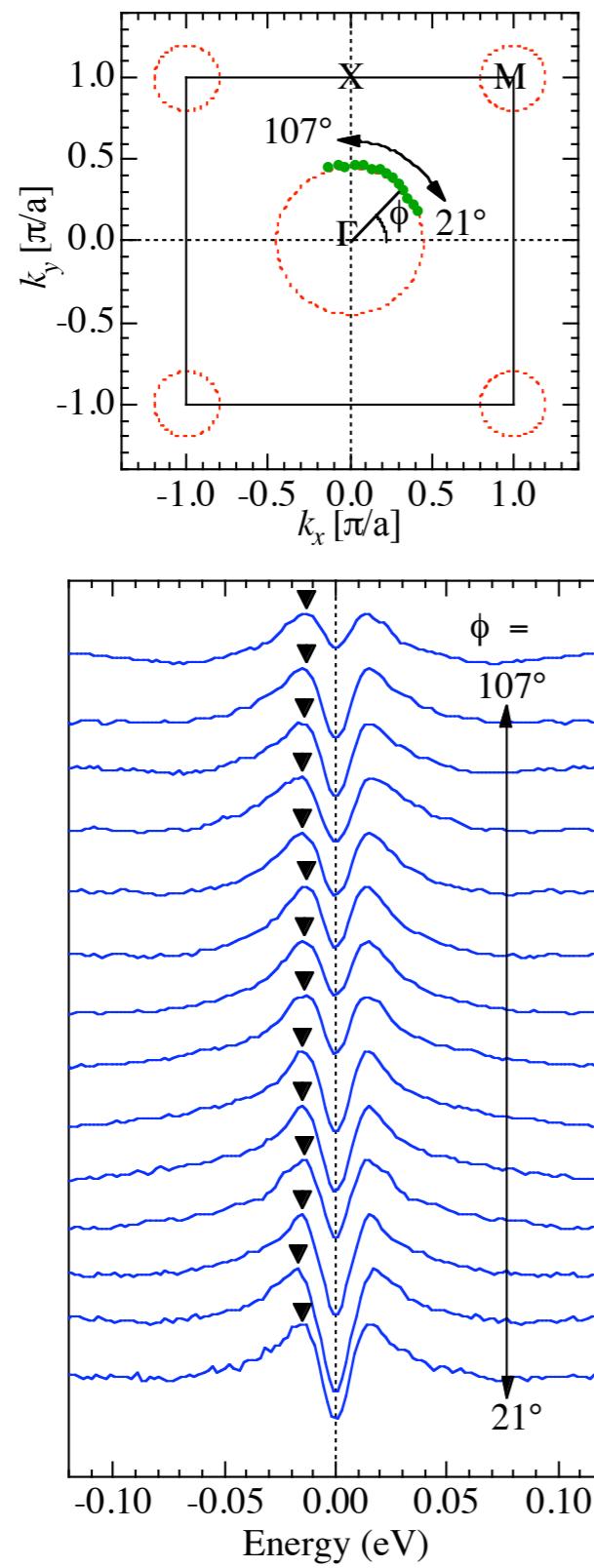
# Two band superconductivity in $\text{MgB}_2$



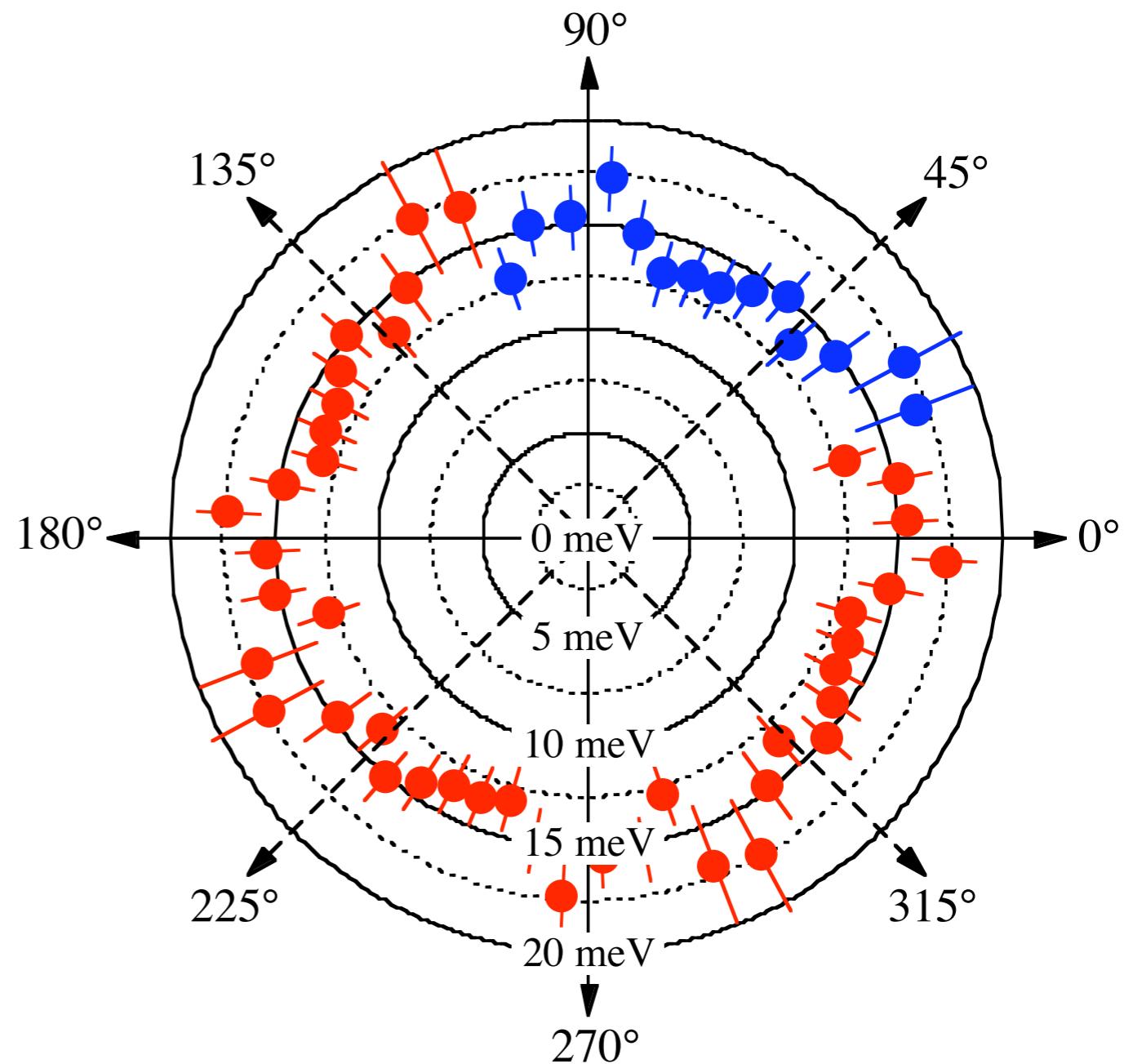
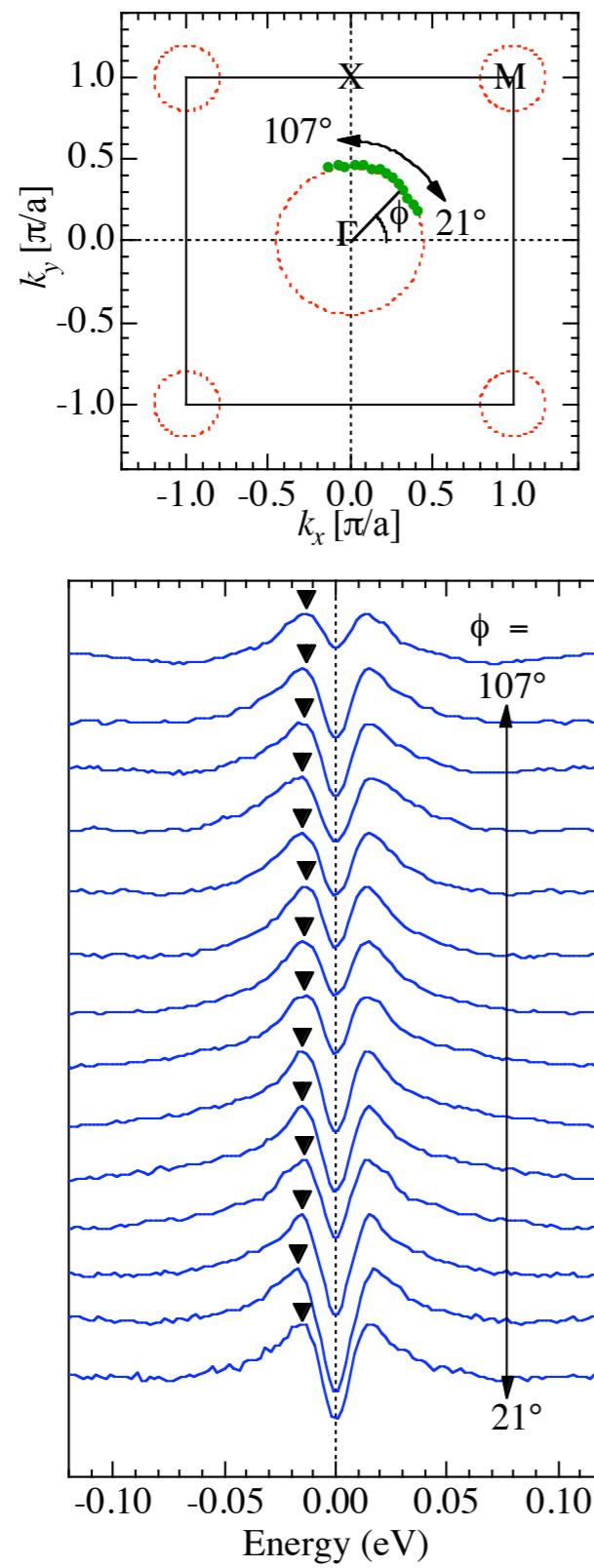
# Superconducting gap



# Momentum dependence of the superconducting gap

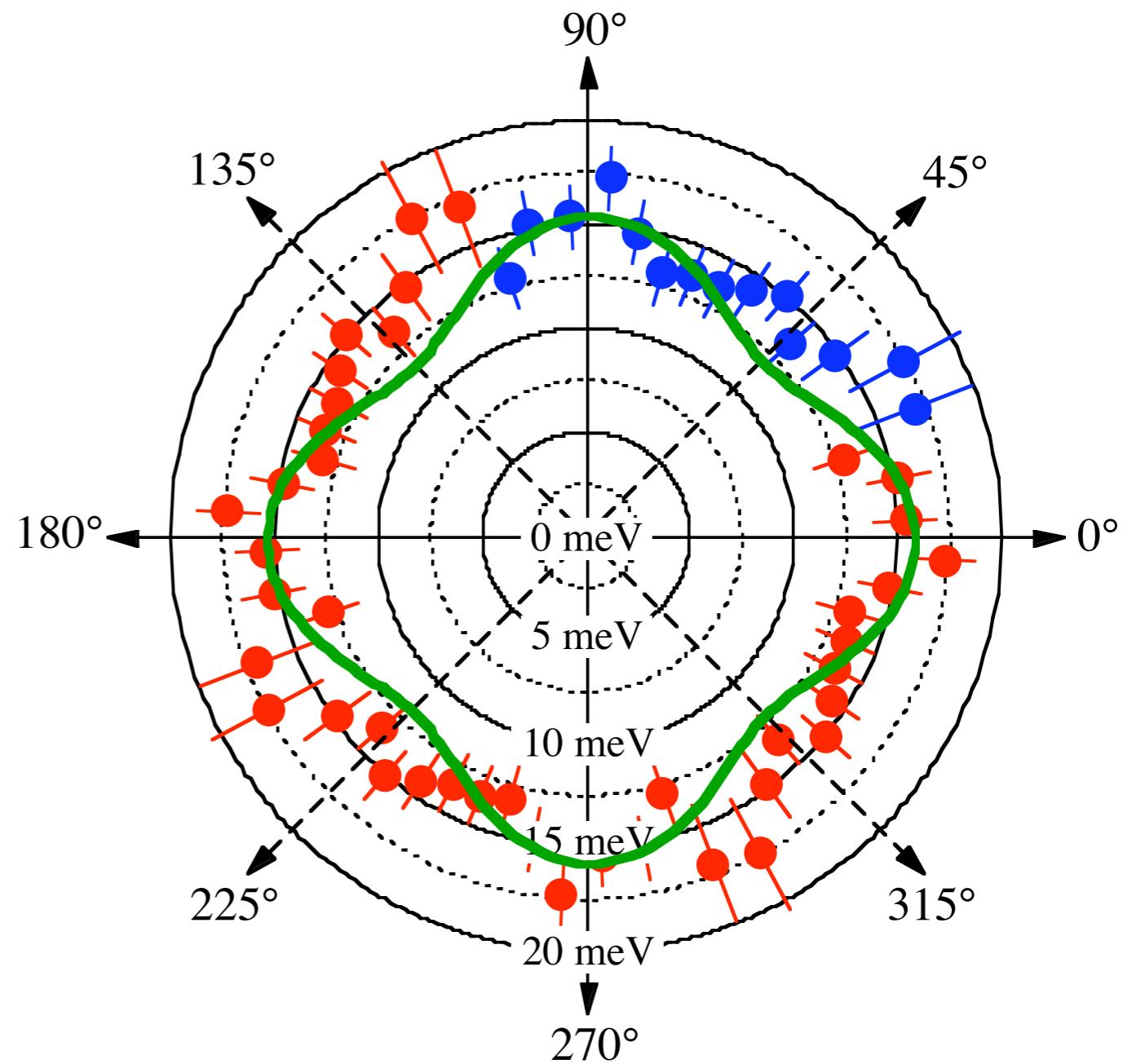
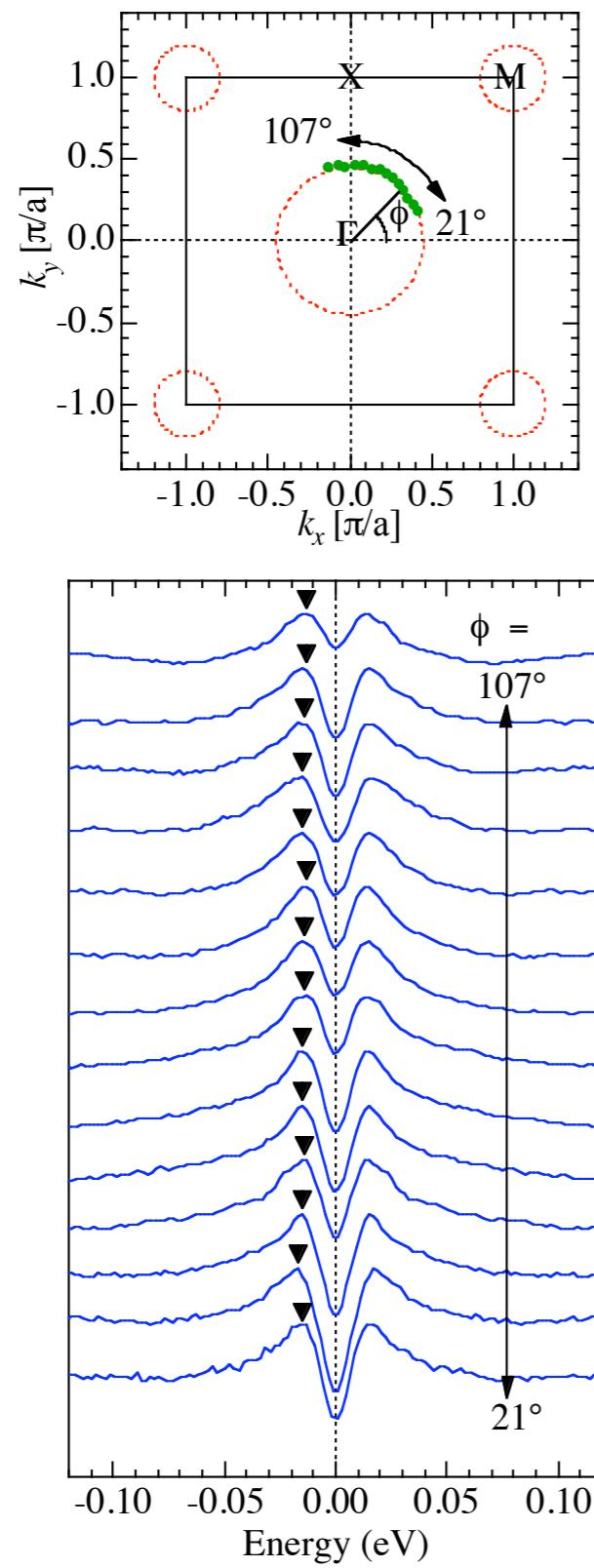


# Momentum dependence of the superconducting gap



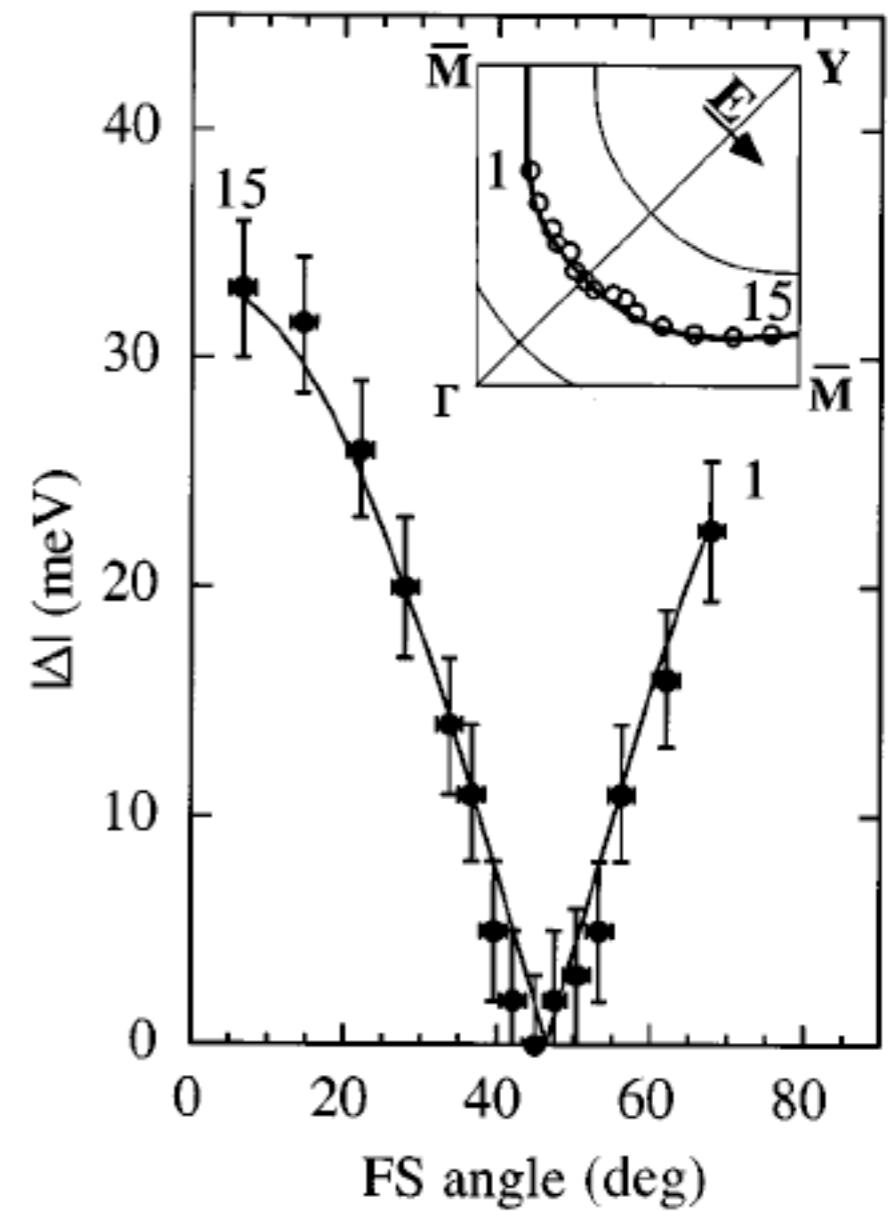
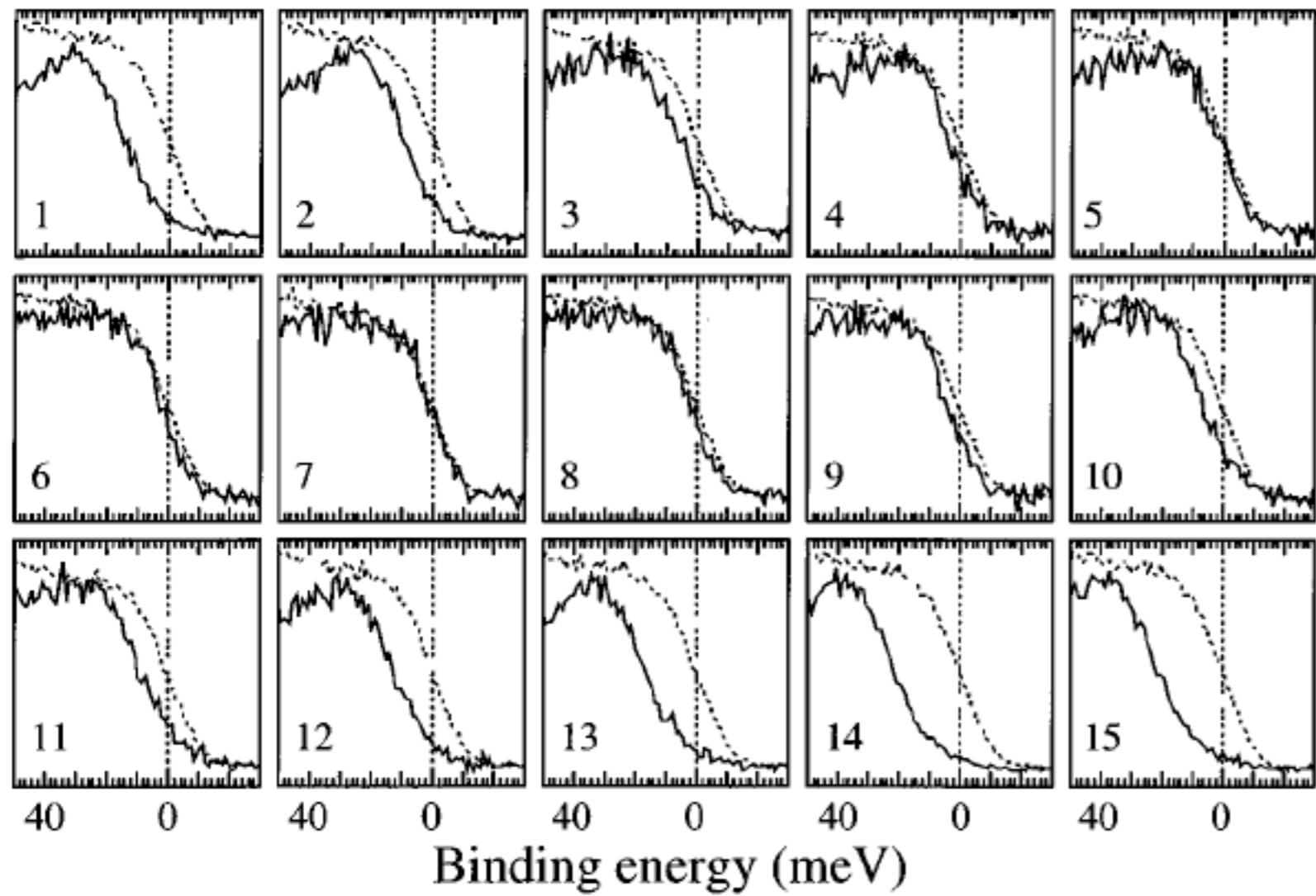
We can exclude d-wave symmetry  
of the order parameter

# Momentum dependence of the superconducting gap

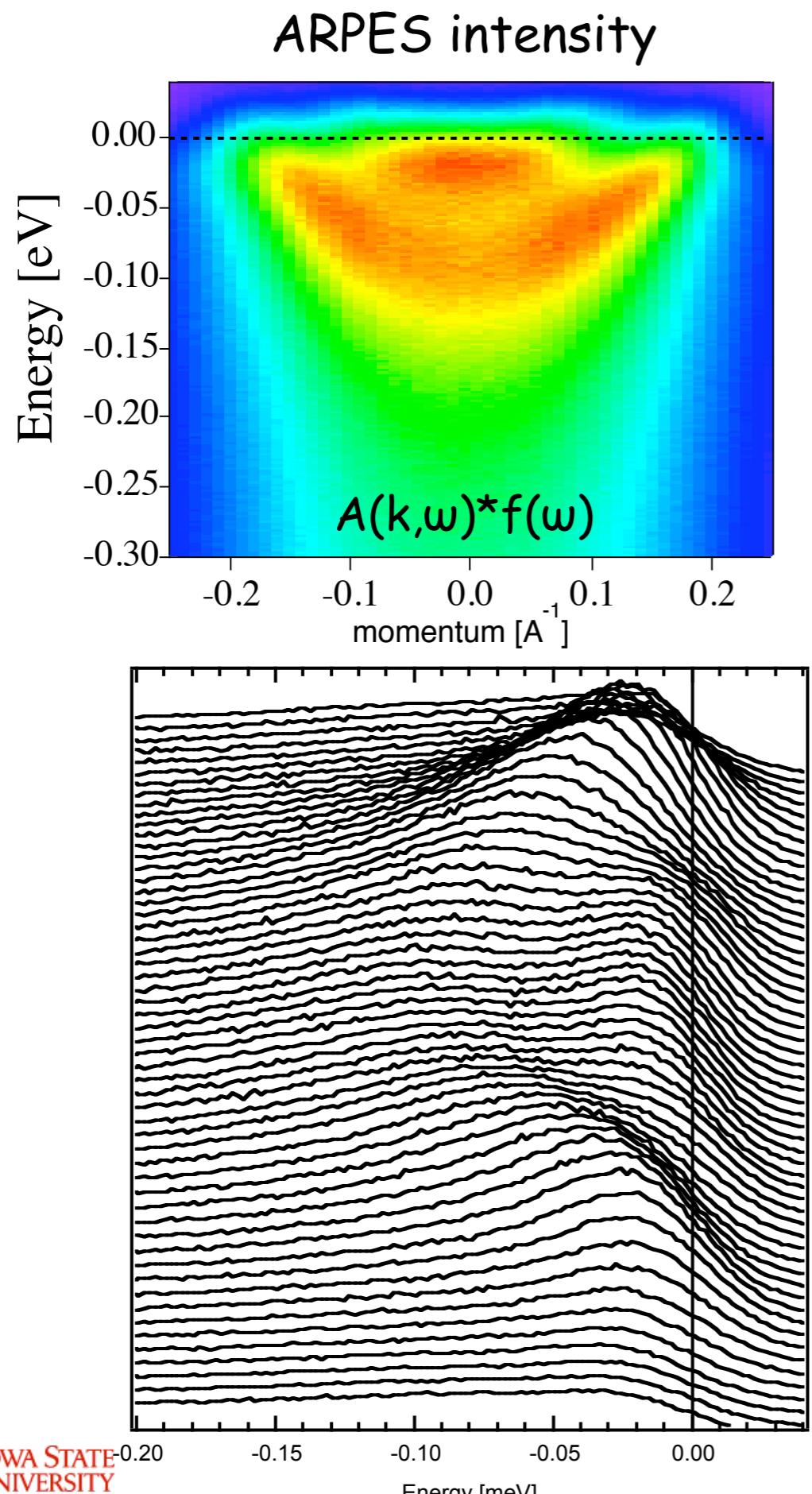


We can exclude d-wave symmetry  
of the order parameter

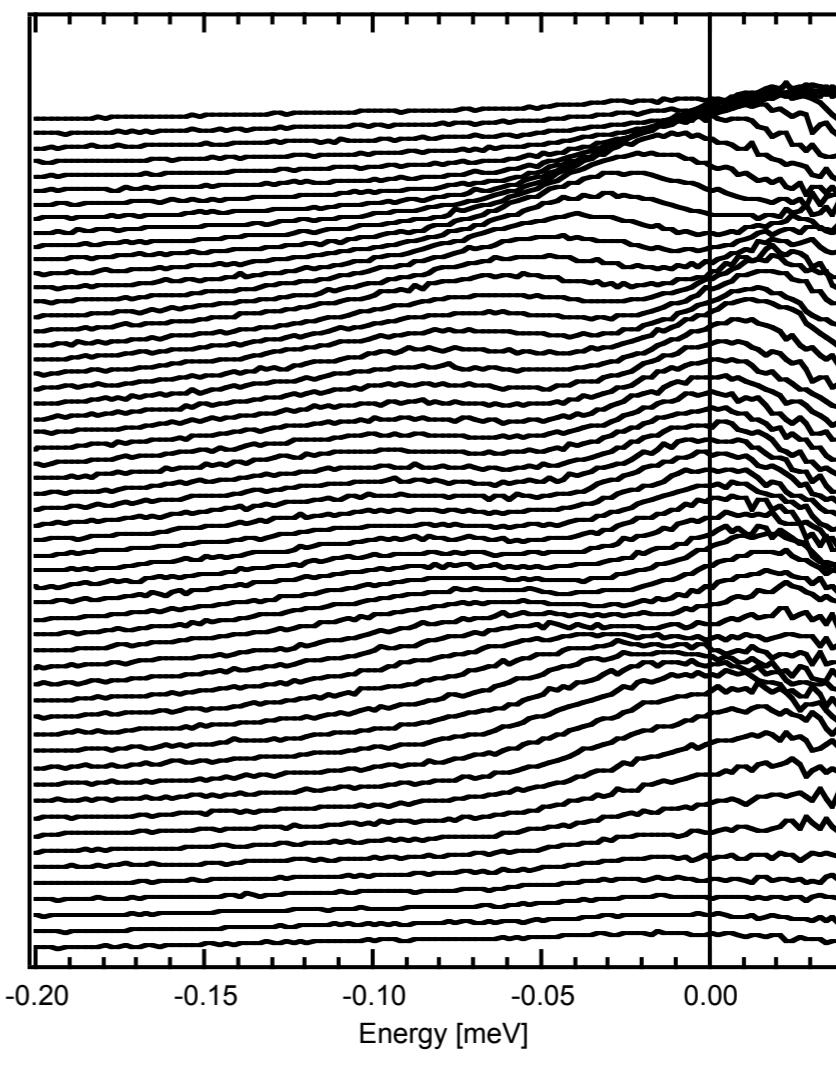
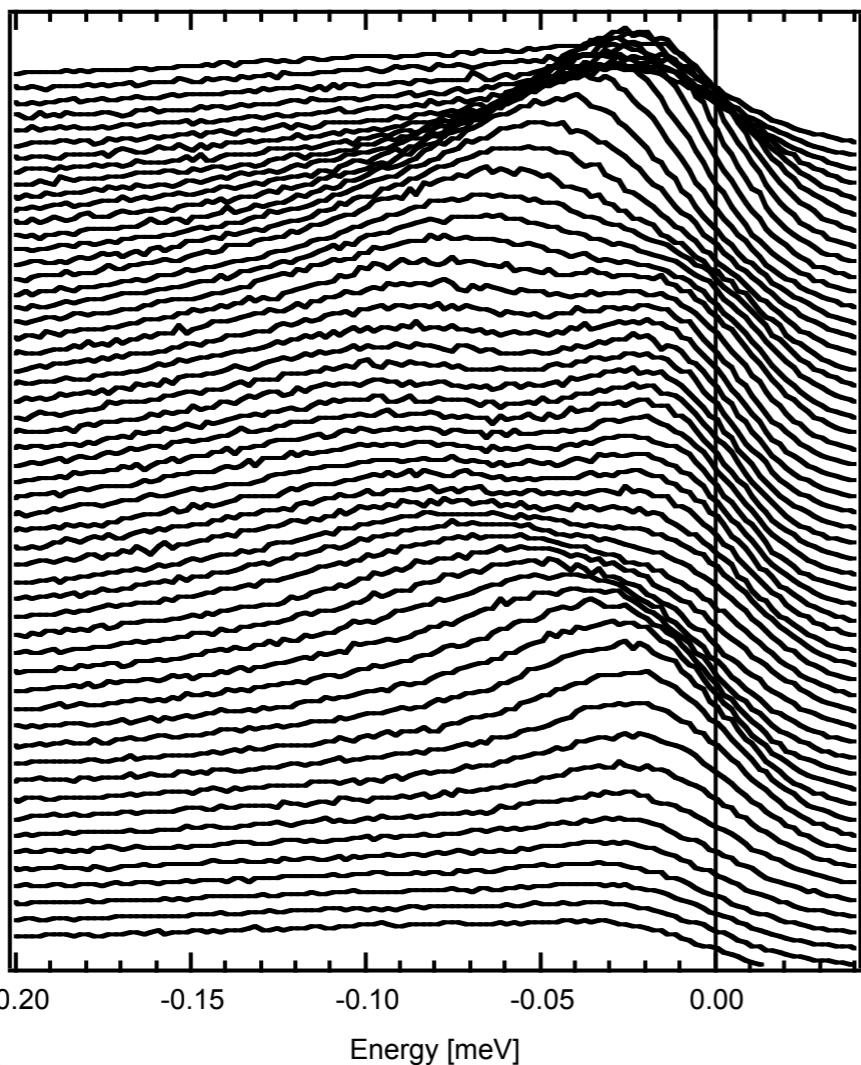
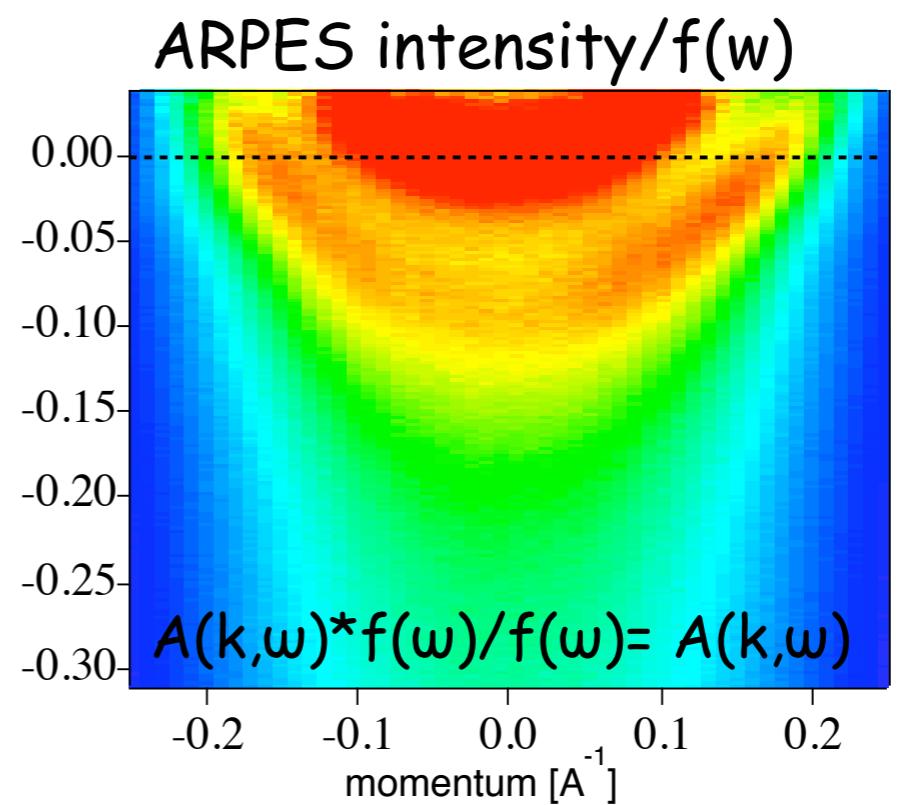
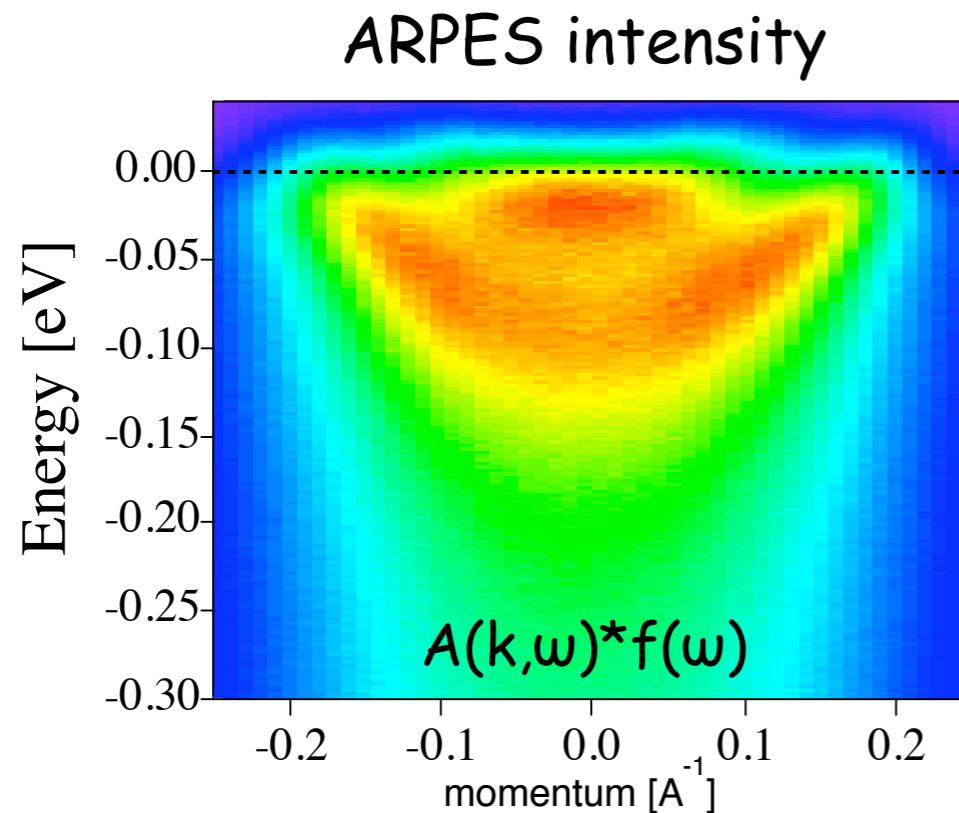
# superconducting gap => order parameter



$$I = \langle \Psi_i | \mathbf{A} \cdot \mathbf{p} | \Psi_f \rangle^2 A(\mathbf{k}, \omega) f(\omega)$$



T=100K



T=100K



IOWA STATE  
UNIVERSITY  
AMES LABORATORY

# Useful tool for analyzing gaps in ARPES spectra: symmetrization method.

M. R. Norman et al., *Nature* **392**, 157 (1998)

# Useful tool for analyzing gaps in ARPES spectra: symmetrization method.

M. R. Norman et al., *Nature* **392**, 157 (1998)

$$I \sim A(k, \omega) f(\omega)$$

# Useful tool for analyzing gaps in ARPES spectra: symmetrization method.

M. R. Norman et al., *Nature* **392**, 157 (1998)

$$I \sim A(k, \omega) f(\omega) \quad f(-\omega) = 1 - f(\omega)$$

# Useful tool for analyzing gaps in ARPES spectra: symmetrization method.

M. R. Norman et al., *Nature* **392**, 157 (1998)

$$I \sim A(k, \omega) f(\omega) \quad f(-\omega) = 1 - f(\omega)$$

$$S \sim A(k_f, \omega) f(\omega) + A(k_f, -\omega) f(-\omega) = A(k_f, \omega)$$

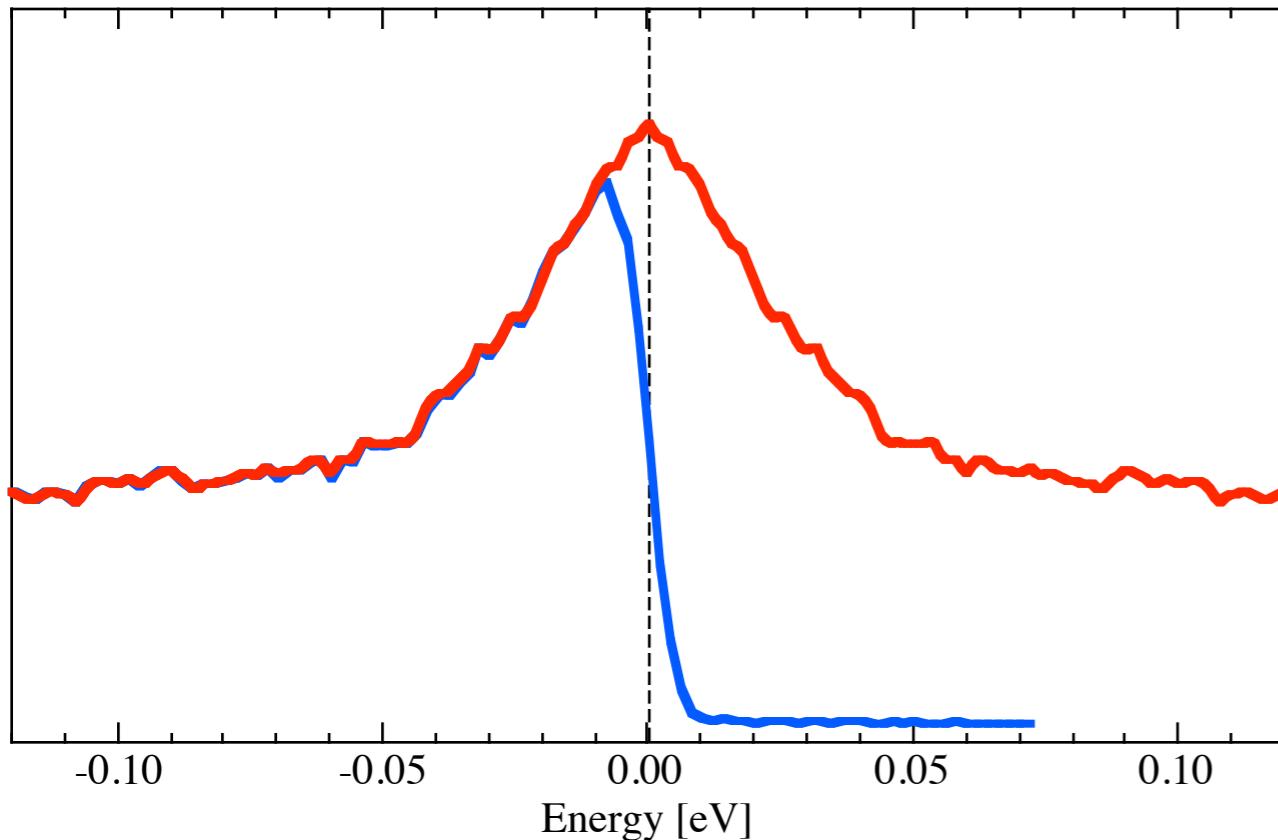
# Useful tool for analyzing gaps in ARPES spectra: symmetrization method.

M. R. Norman et al., *Nature* **392**, 157 (1998)

$$I \sim A(k, \omega) f(\omega)$$

$$f(-\omega) = 1 - f(\omega)$$

$$S \sim A(k_f, \omega) f(\omega) + A(k_f, -\omega) f(-\omega) = A(k_f, \omega)$$



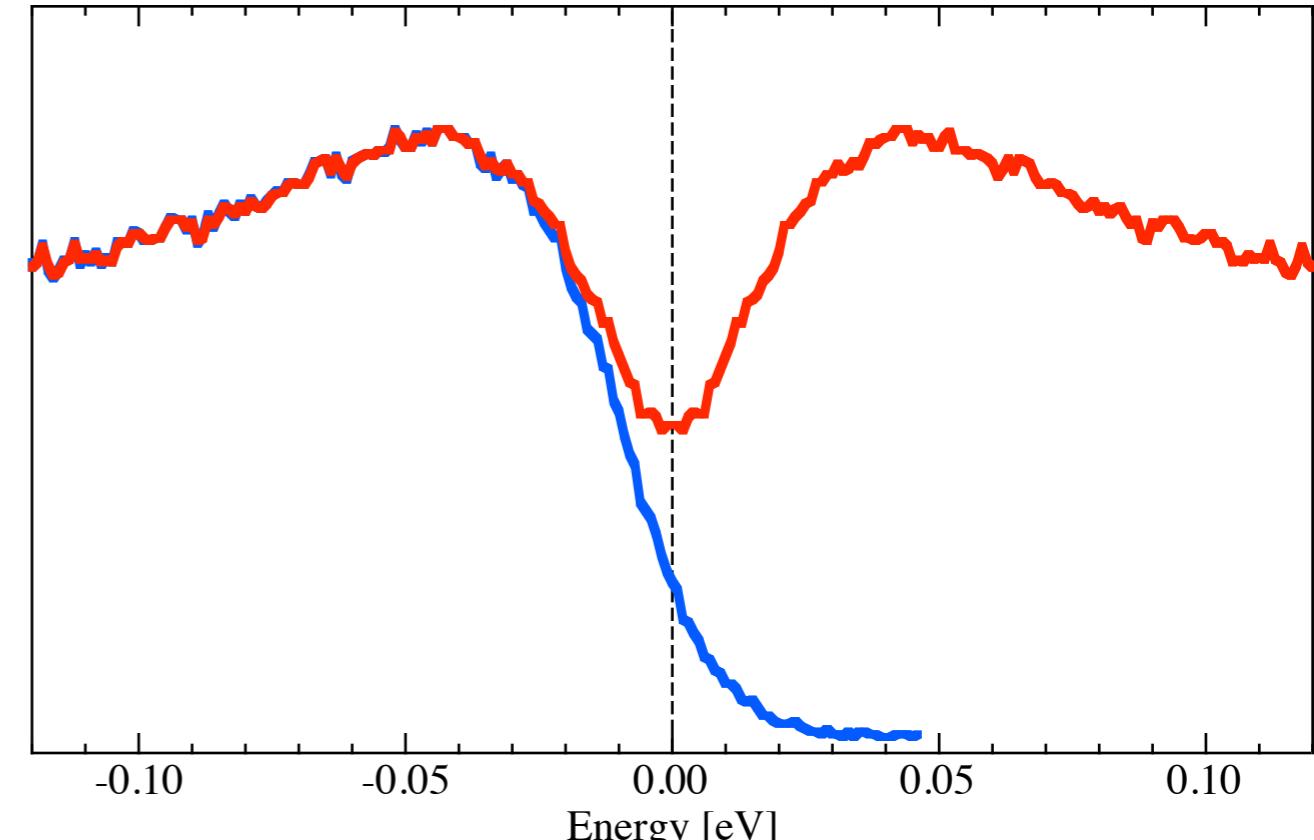
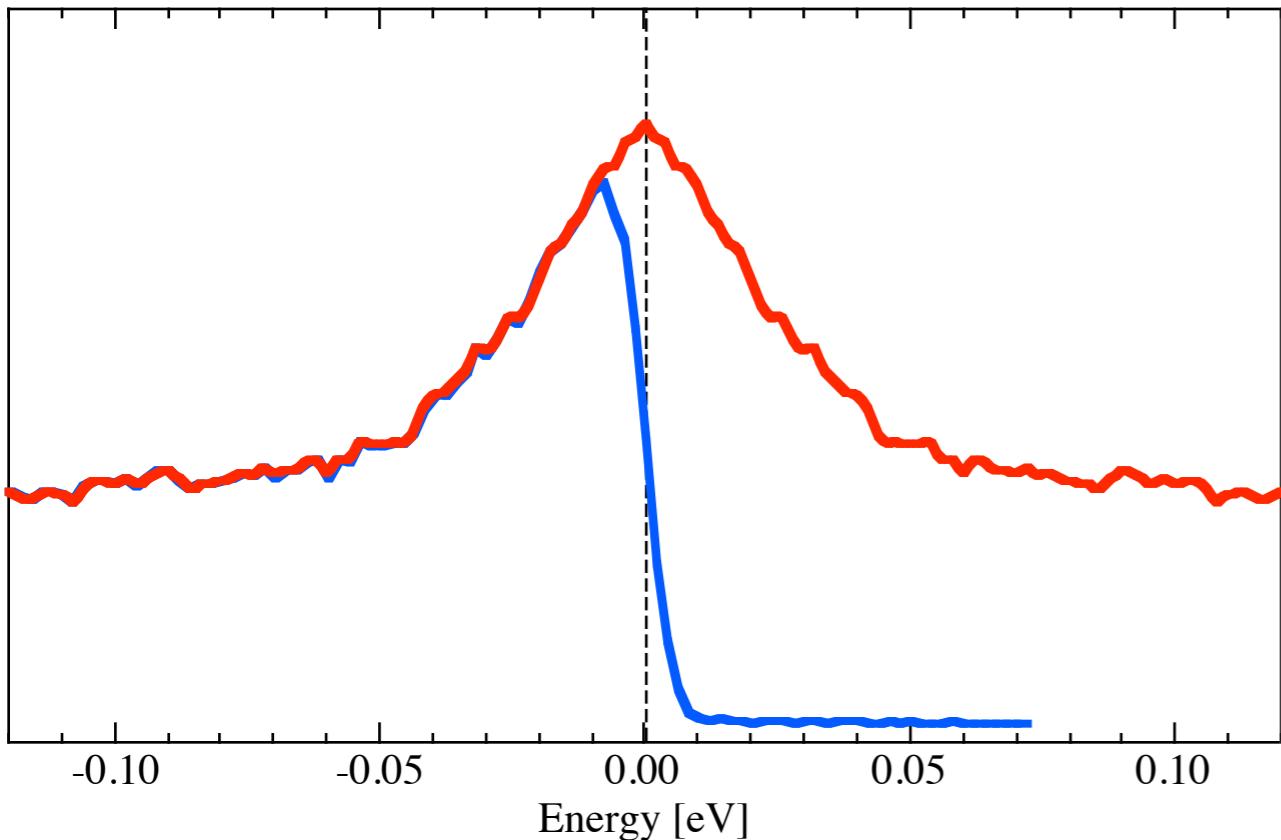
# Useful tool for analyzing gaps in ARPES spectra: symmetrization method.

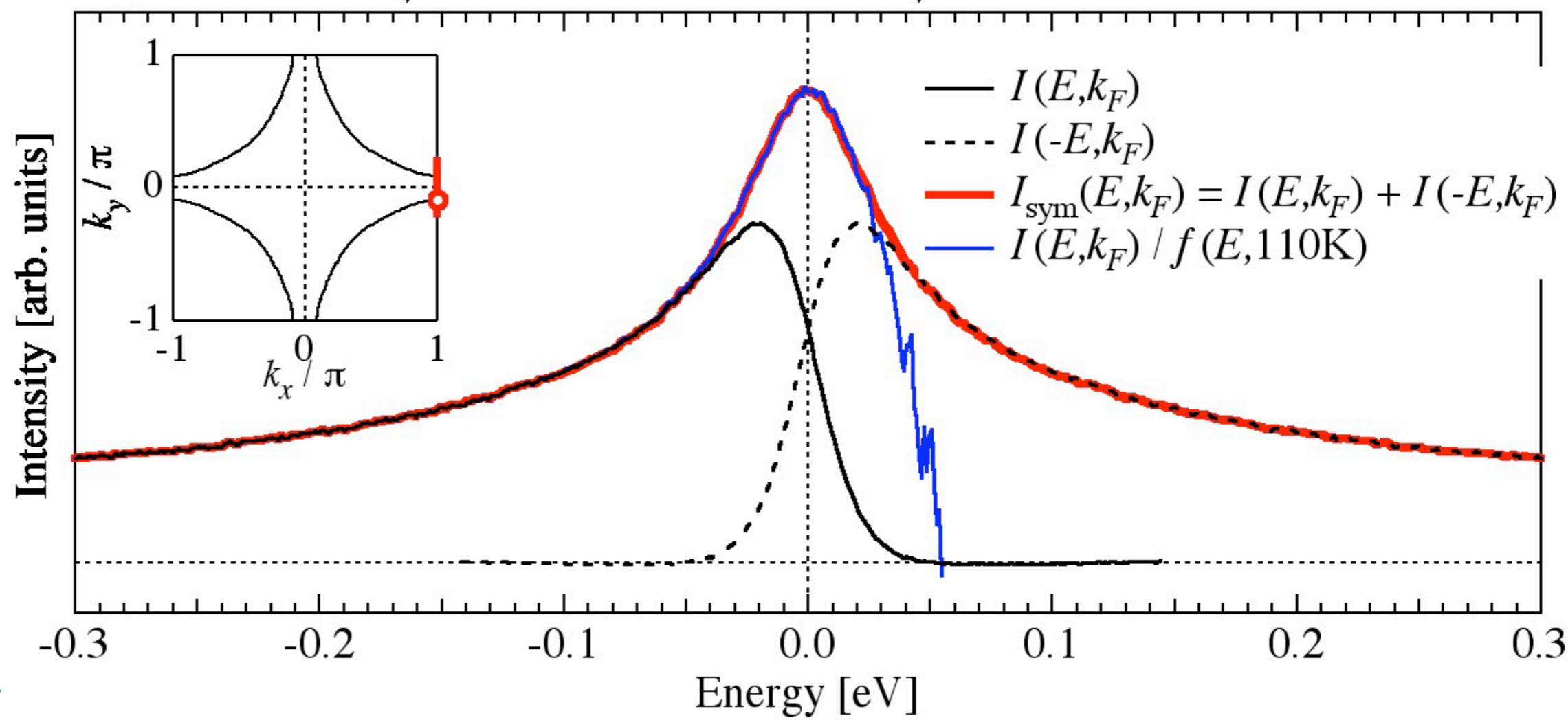
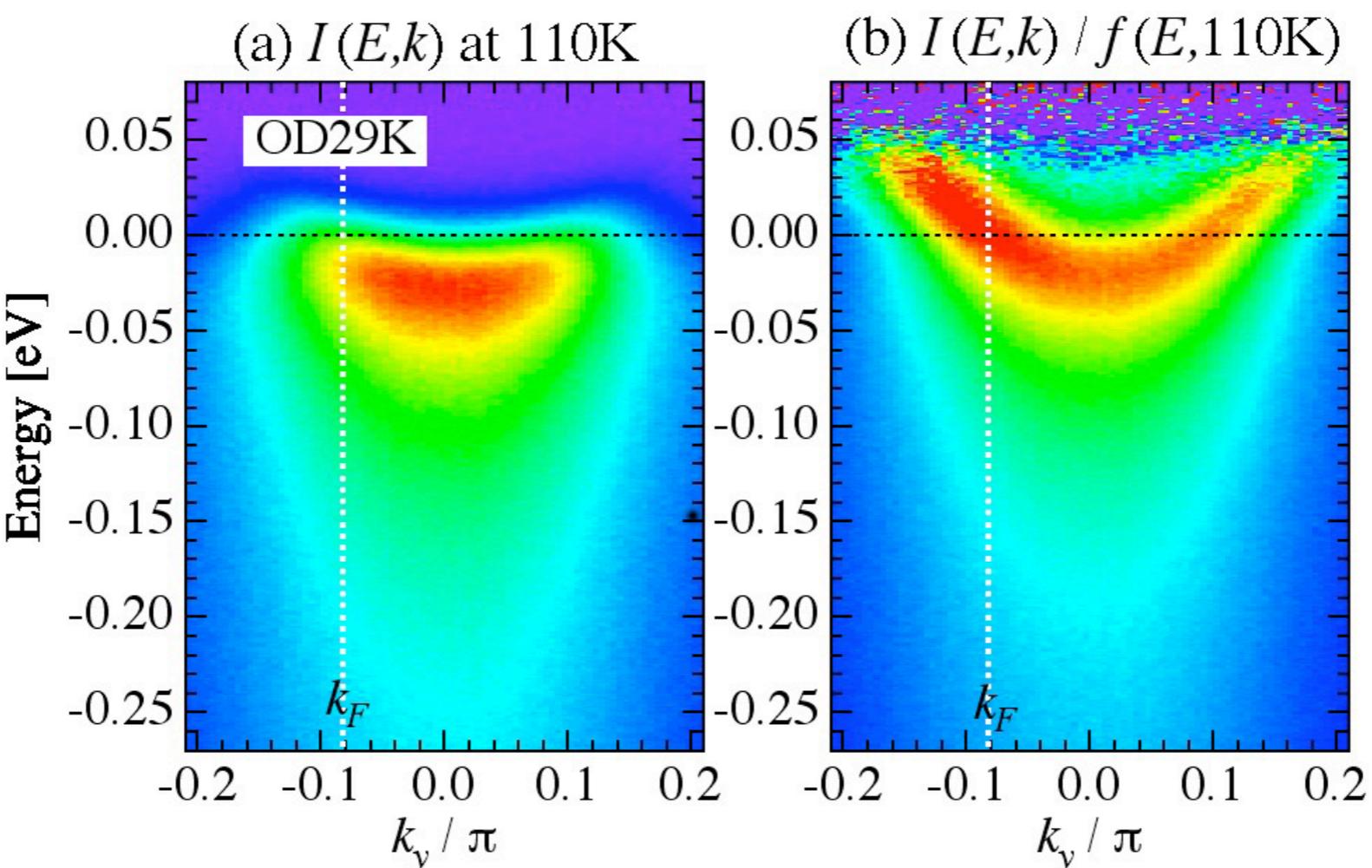
M. R. Norman et al., *Nature* **392**, 157 (1998)

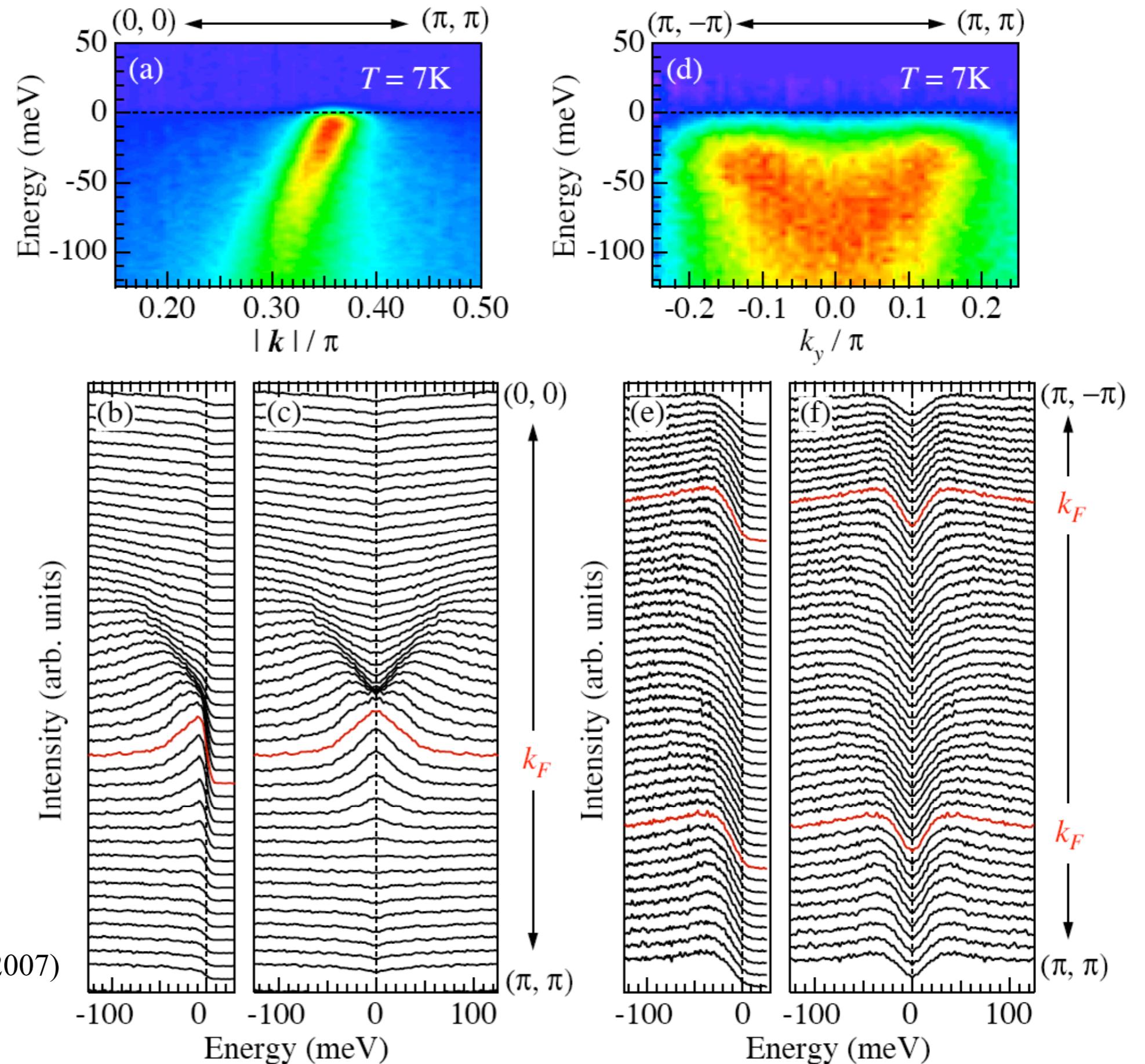
$$I \sim A(k, \omega) f(\omega)$$

$$f(-\omega) = 1 - f(\omega)$$

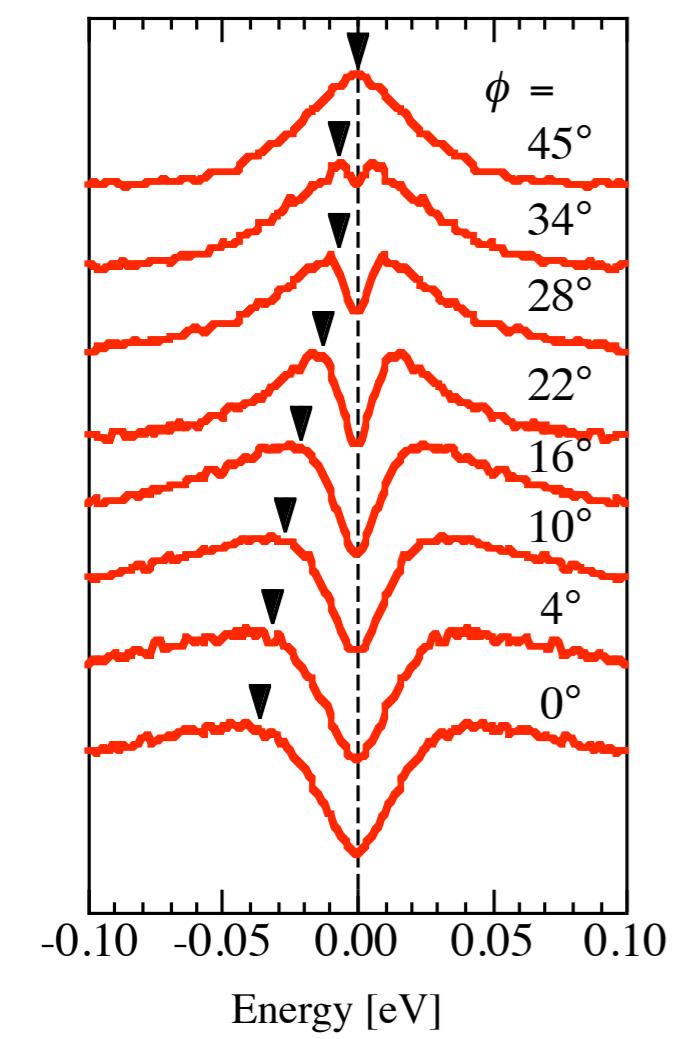
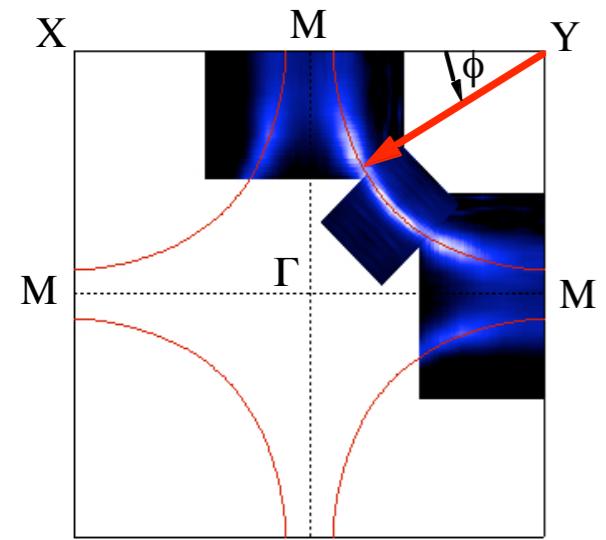
$$S \sim A(k_f, \omega) f(\omega) + A(k_f, -\omega) f(-\omega) = A(k_f, \omega)$$

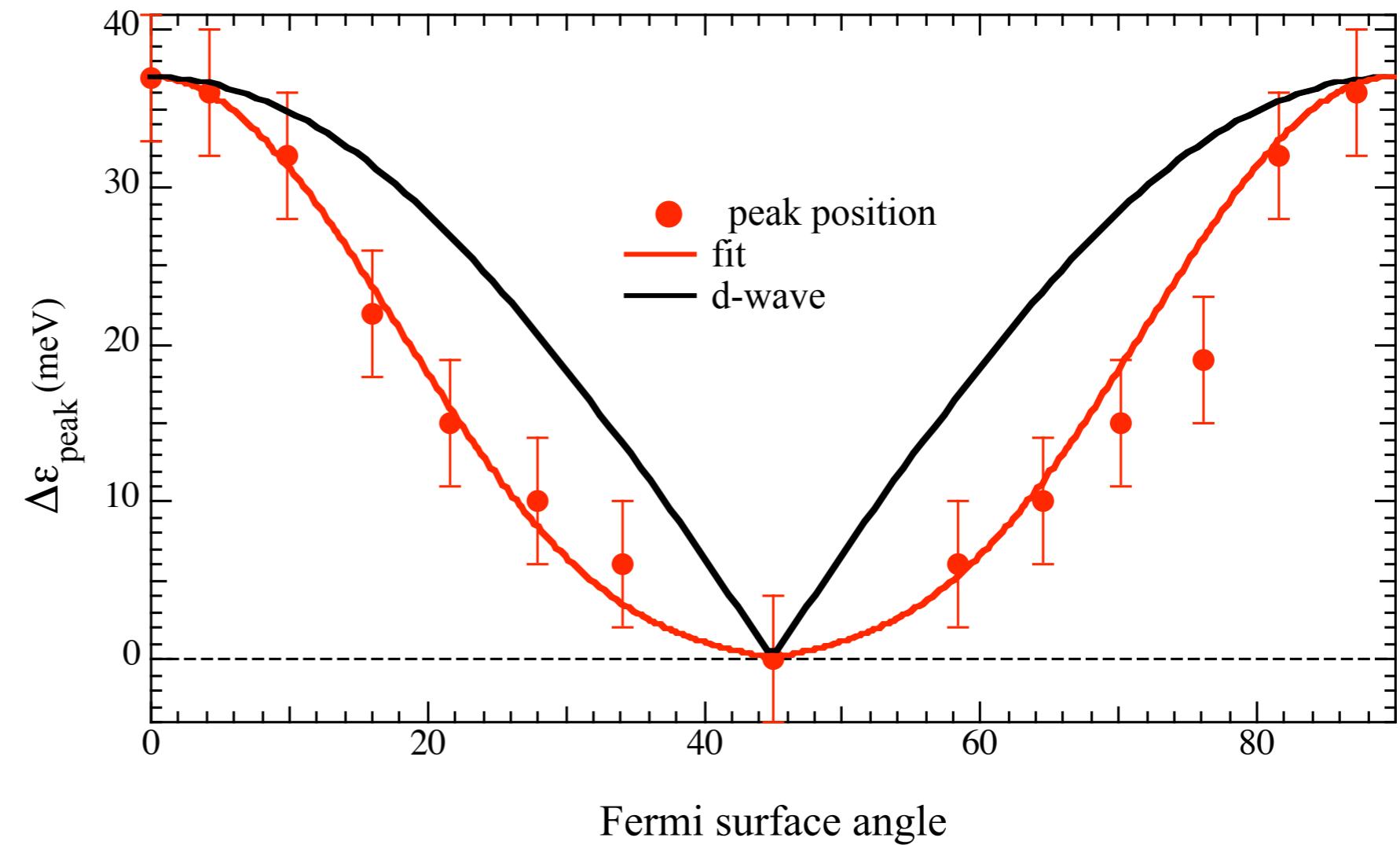
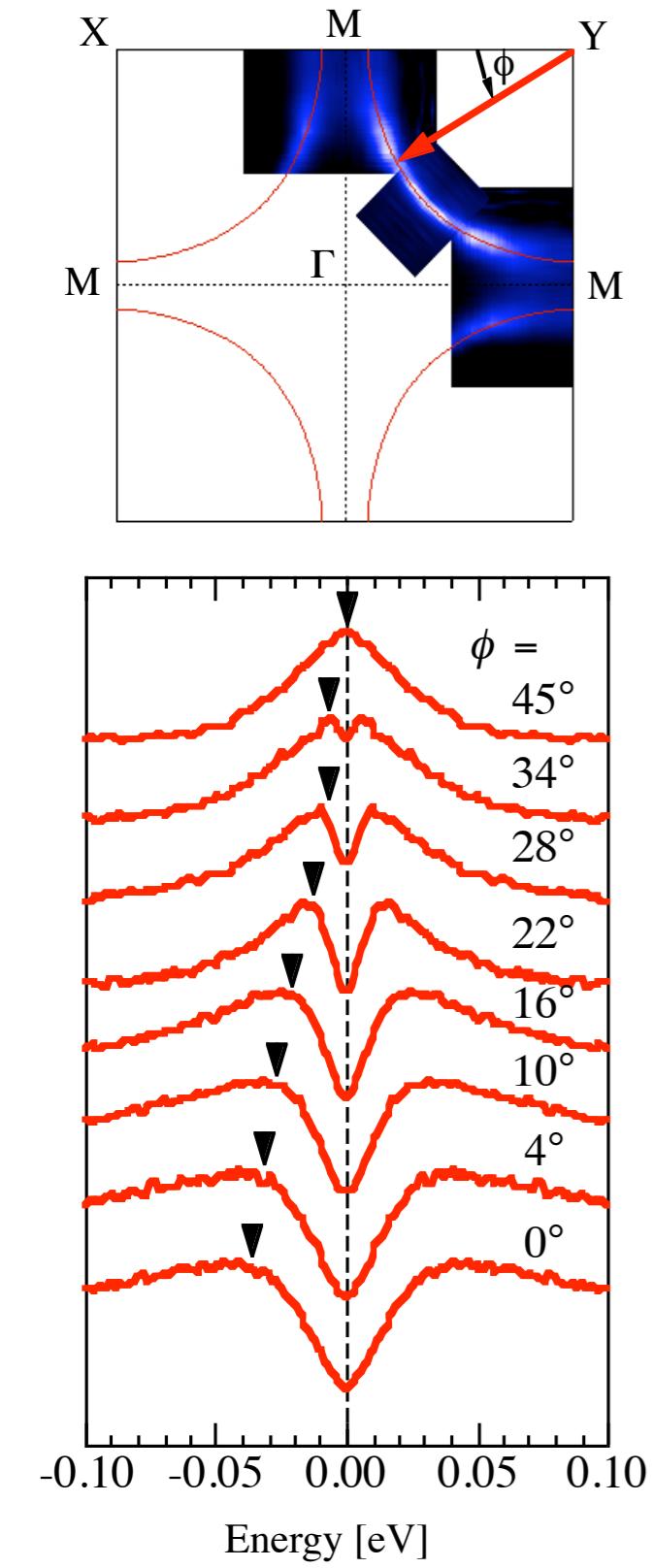




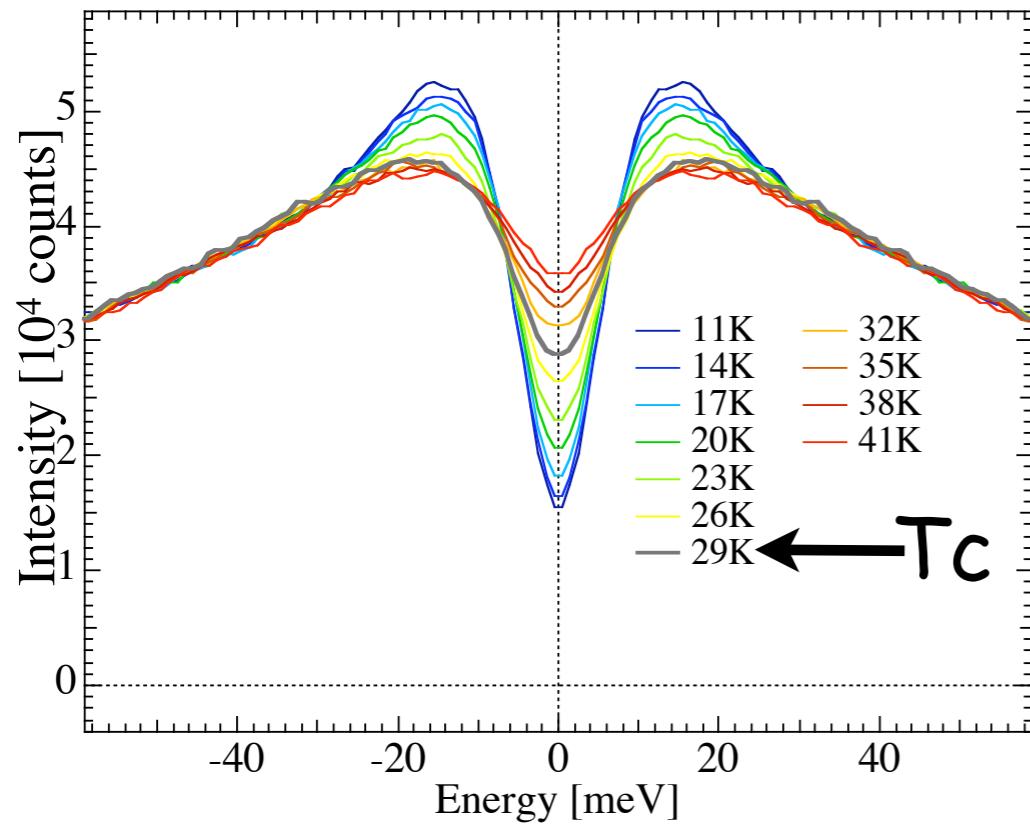


T. Kondo et al.,  
Phys. Rev. Lett. **98**, 267004 (2007)

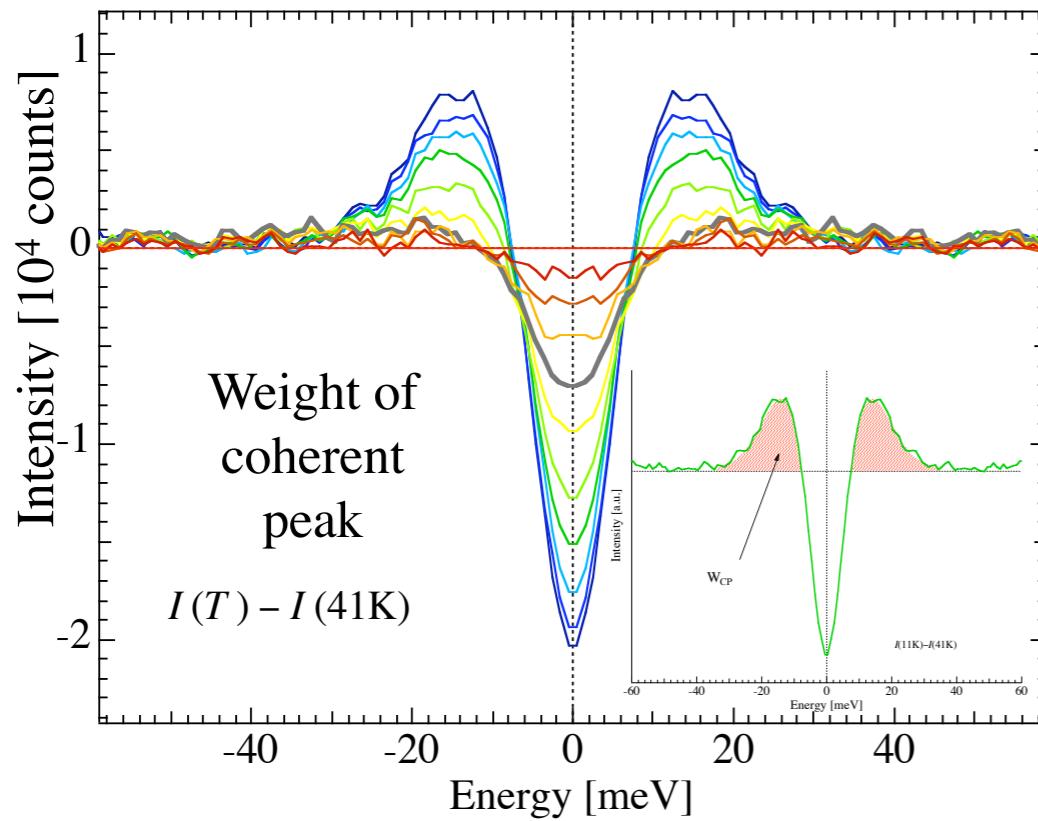
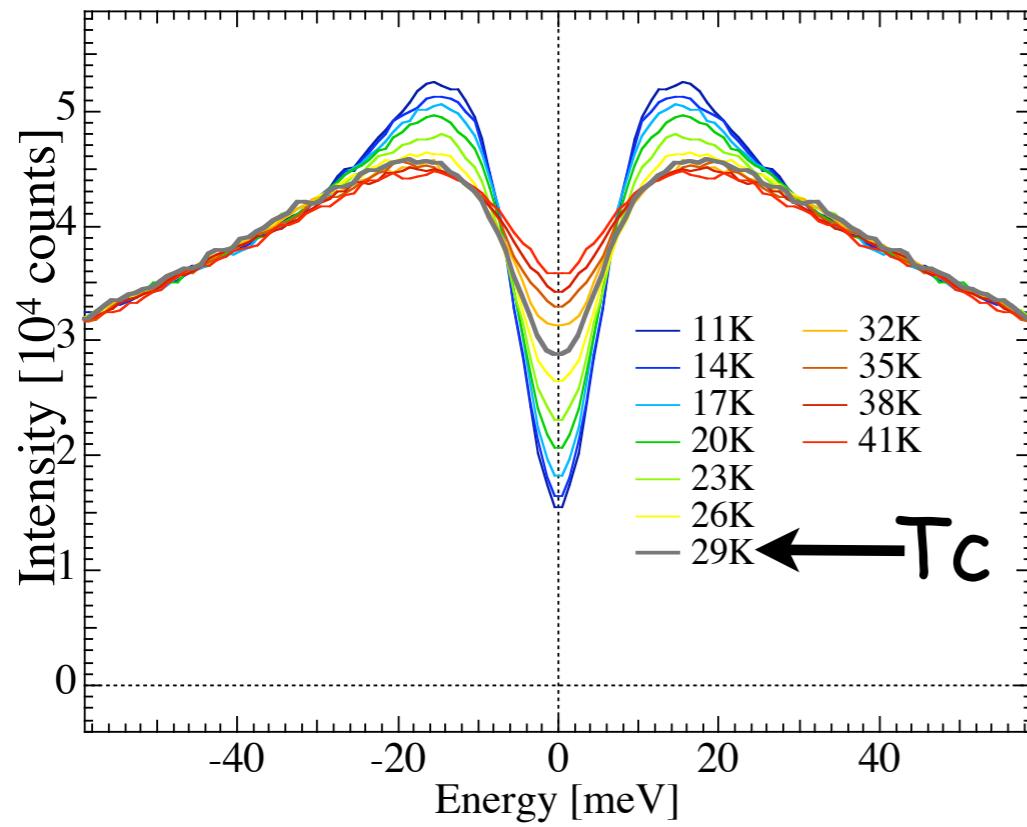




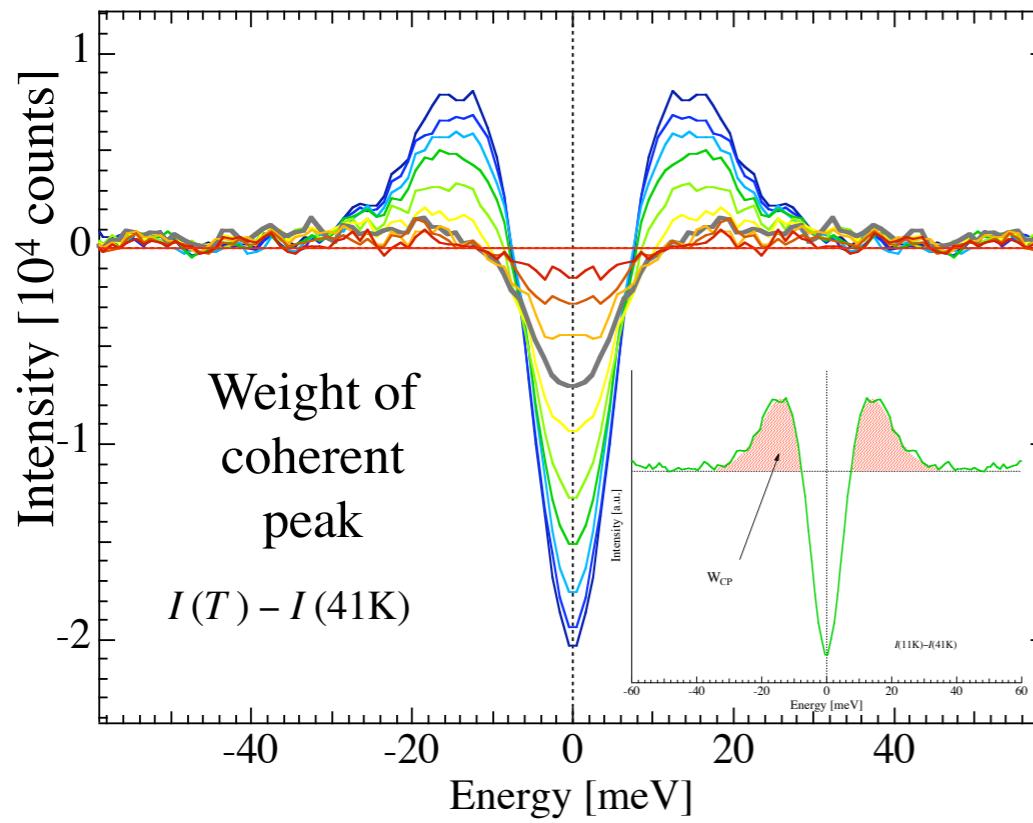
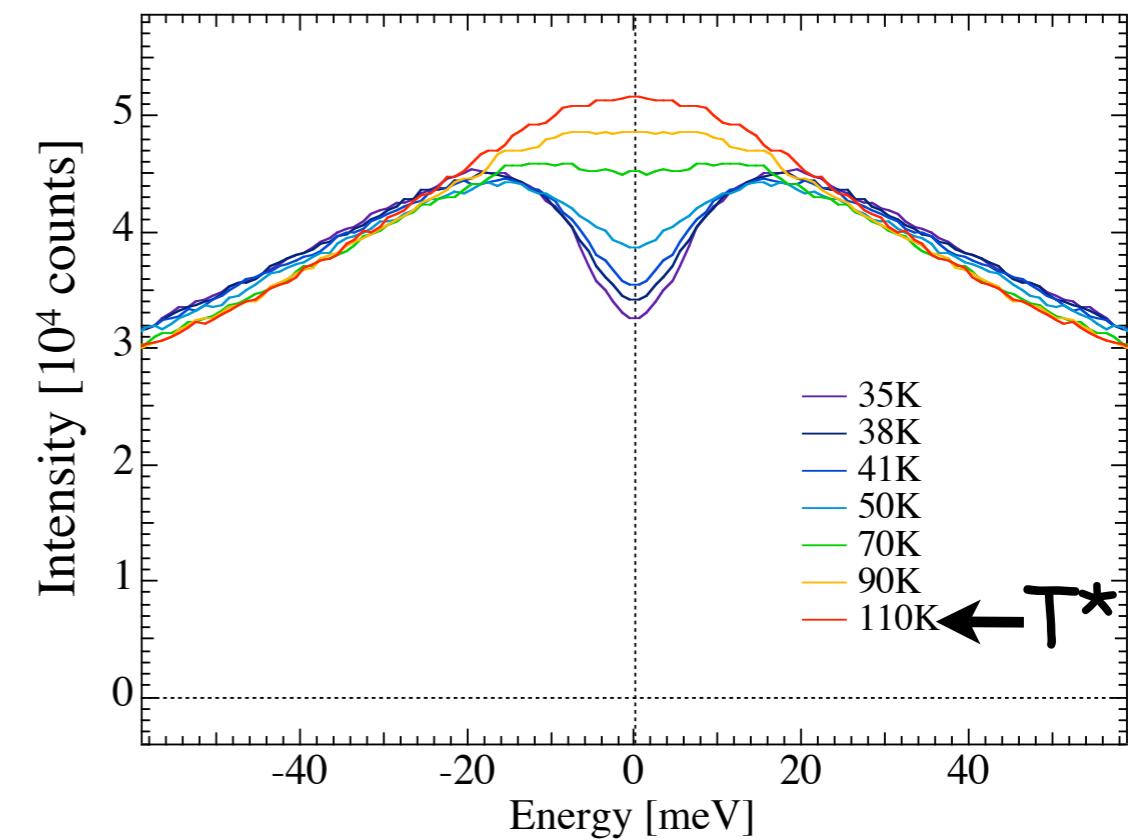
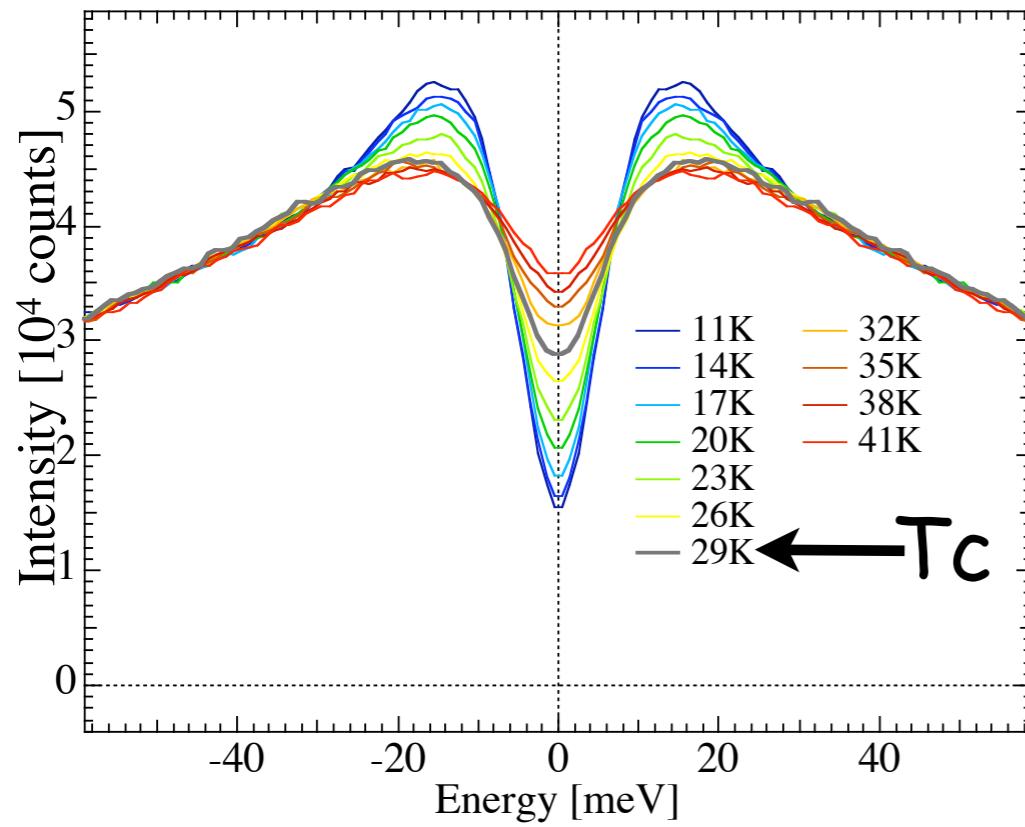
# Spectral changes across $T_c$ and $T^*$ at antinode



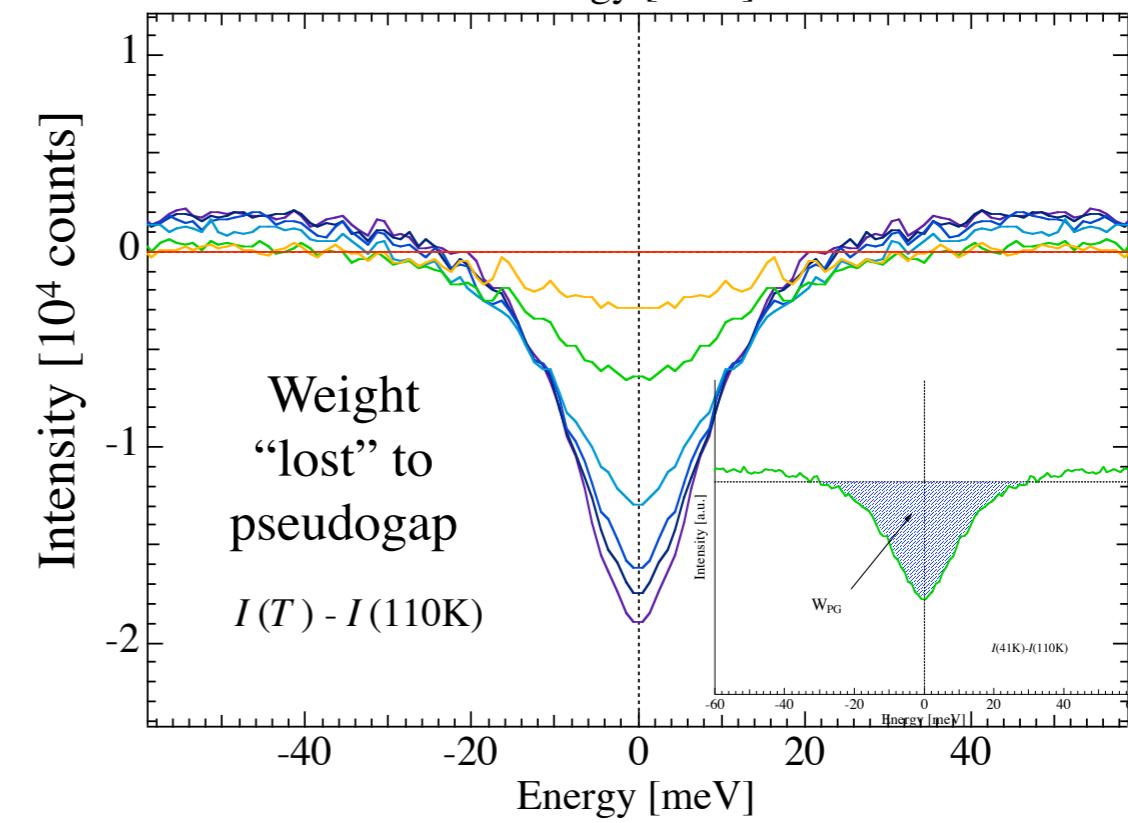
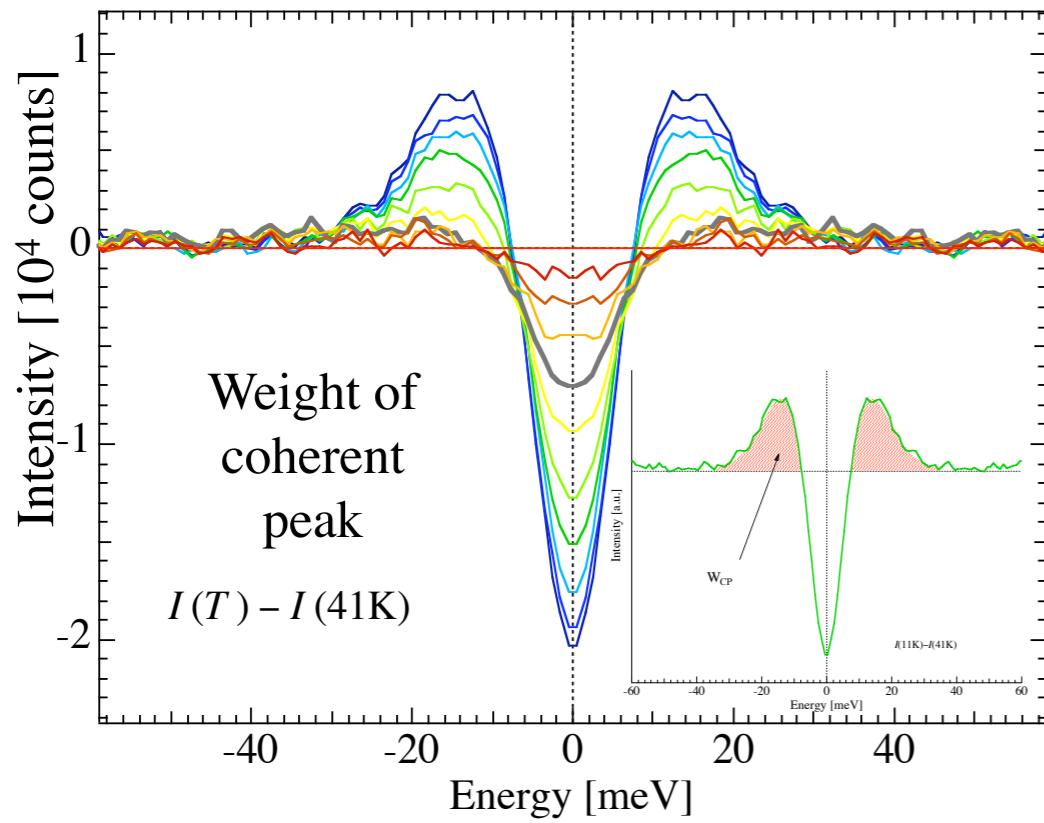
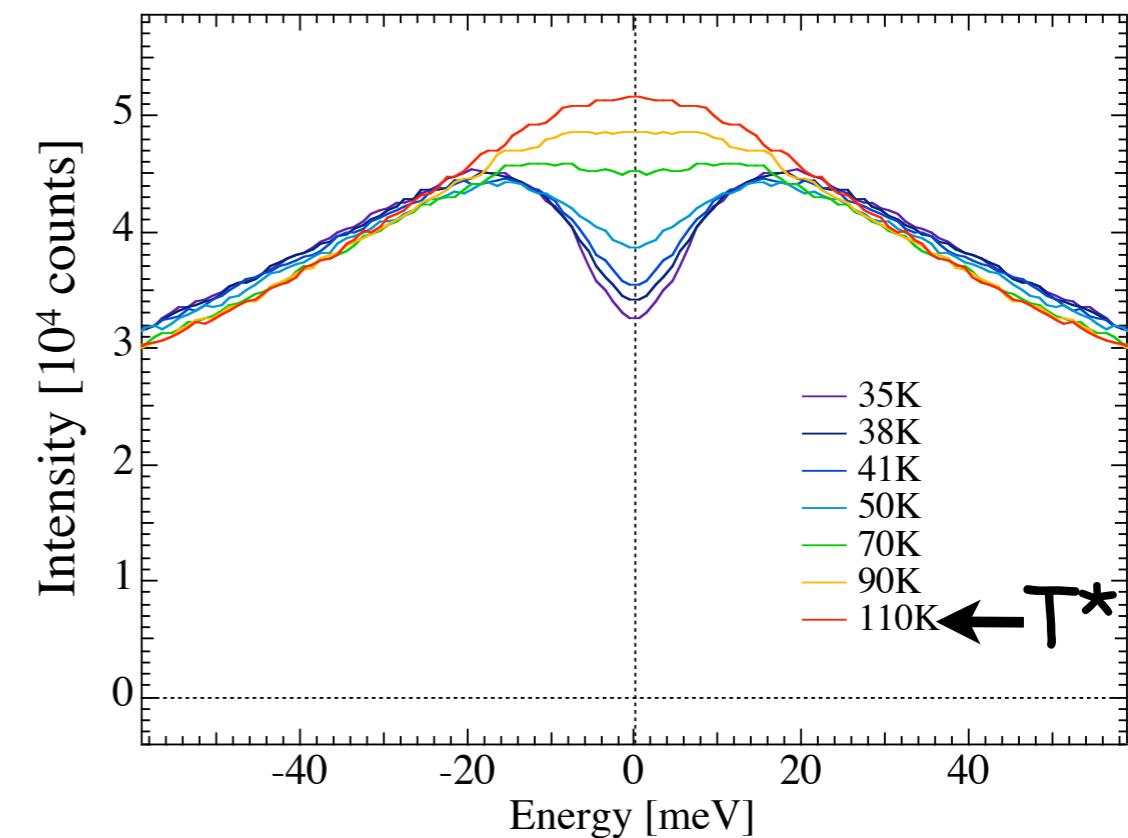
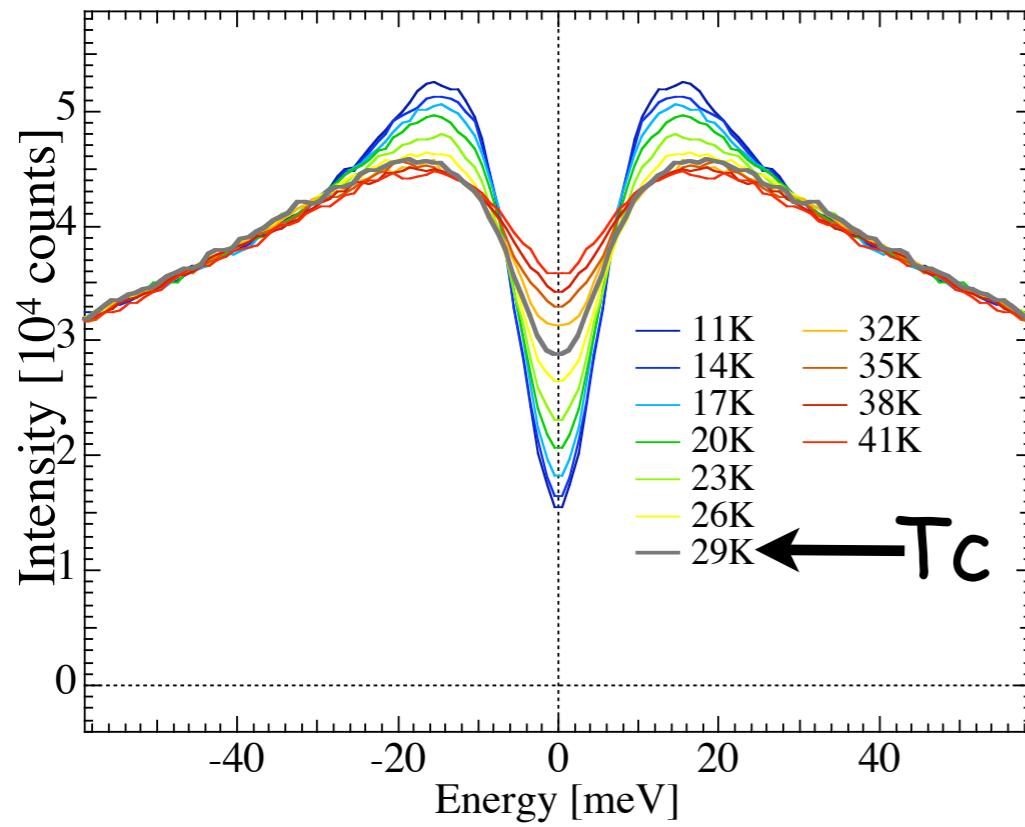
# Spectral changes across $T_c$ and $T^*$ at antinode

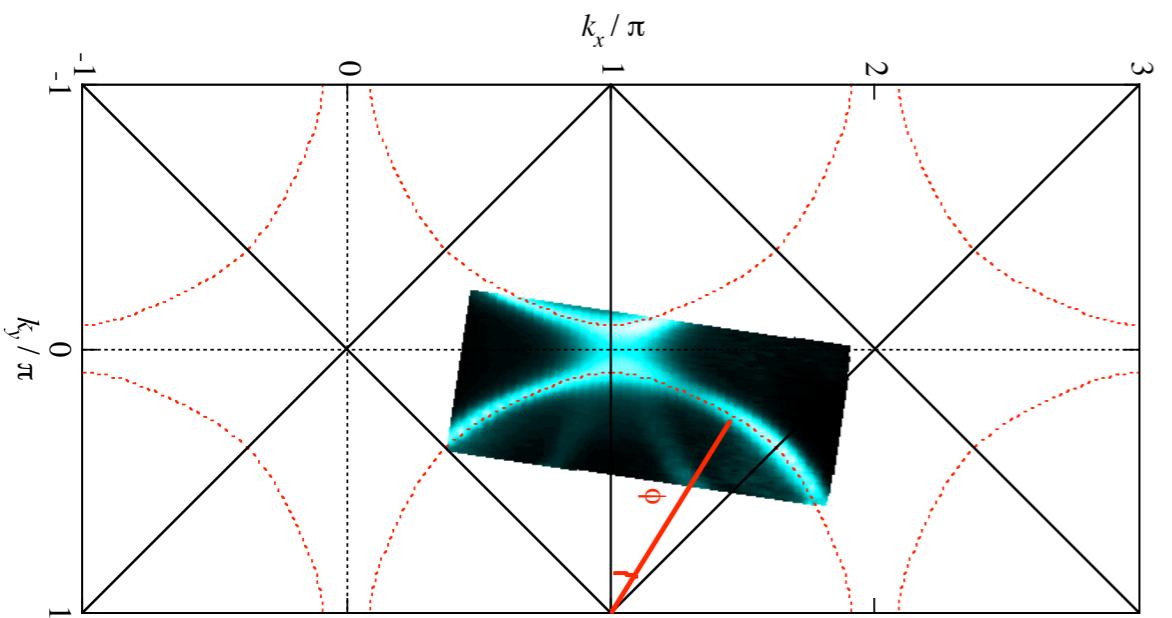


# Spectral changes across $T_c$ and $T^*$ at antinode

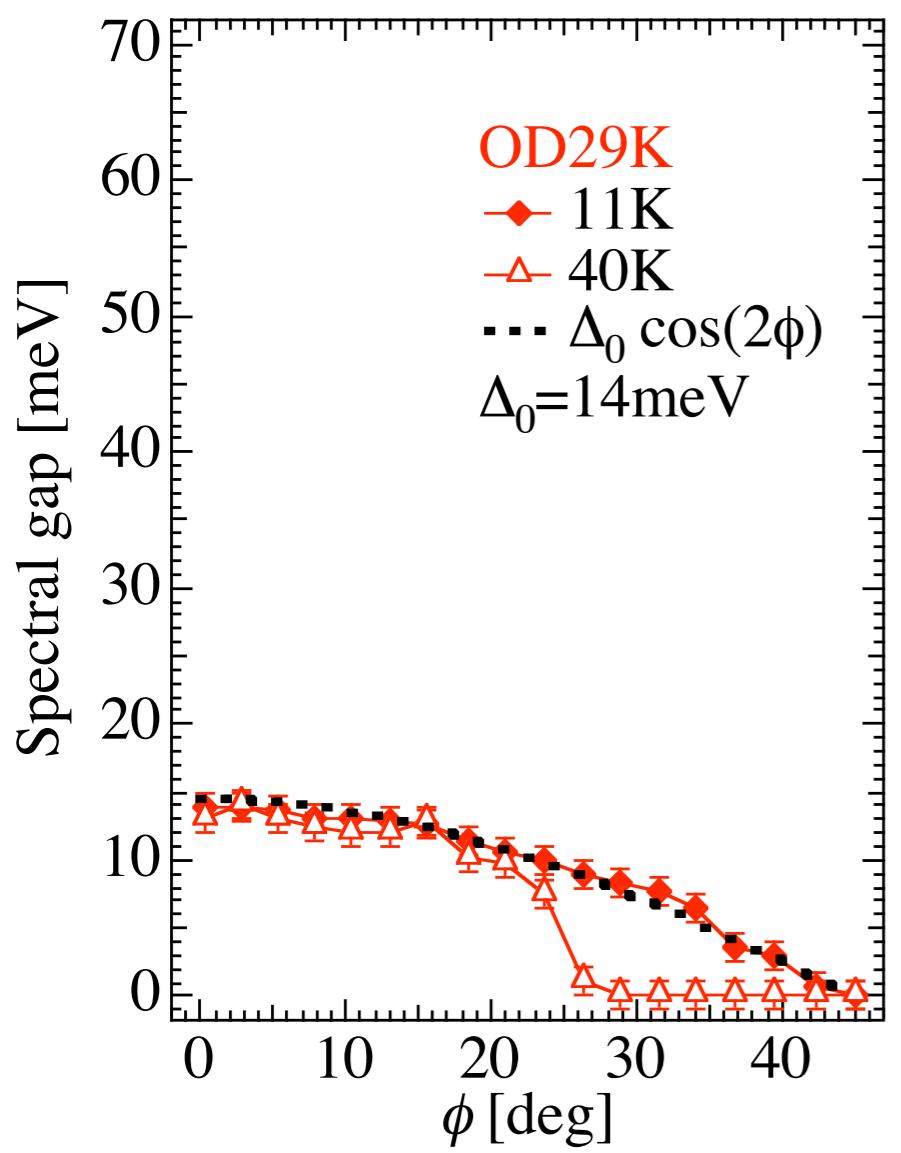


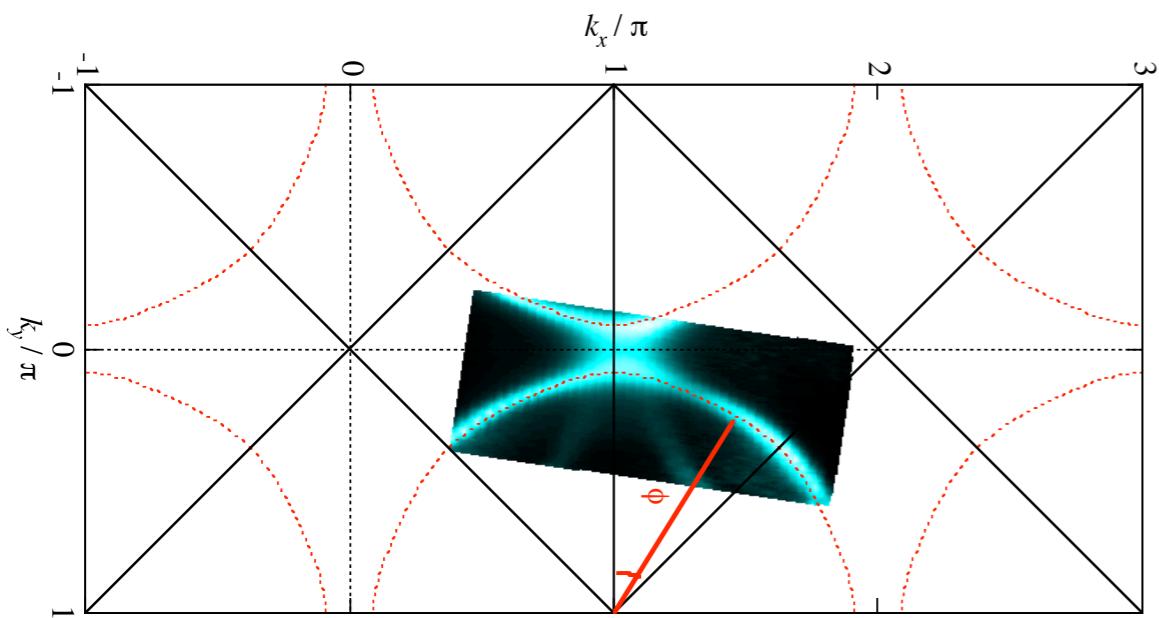
# Spectral changes across $T_c$ and $T^*$ at antinode



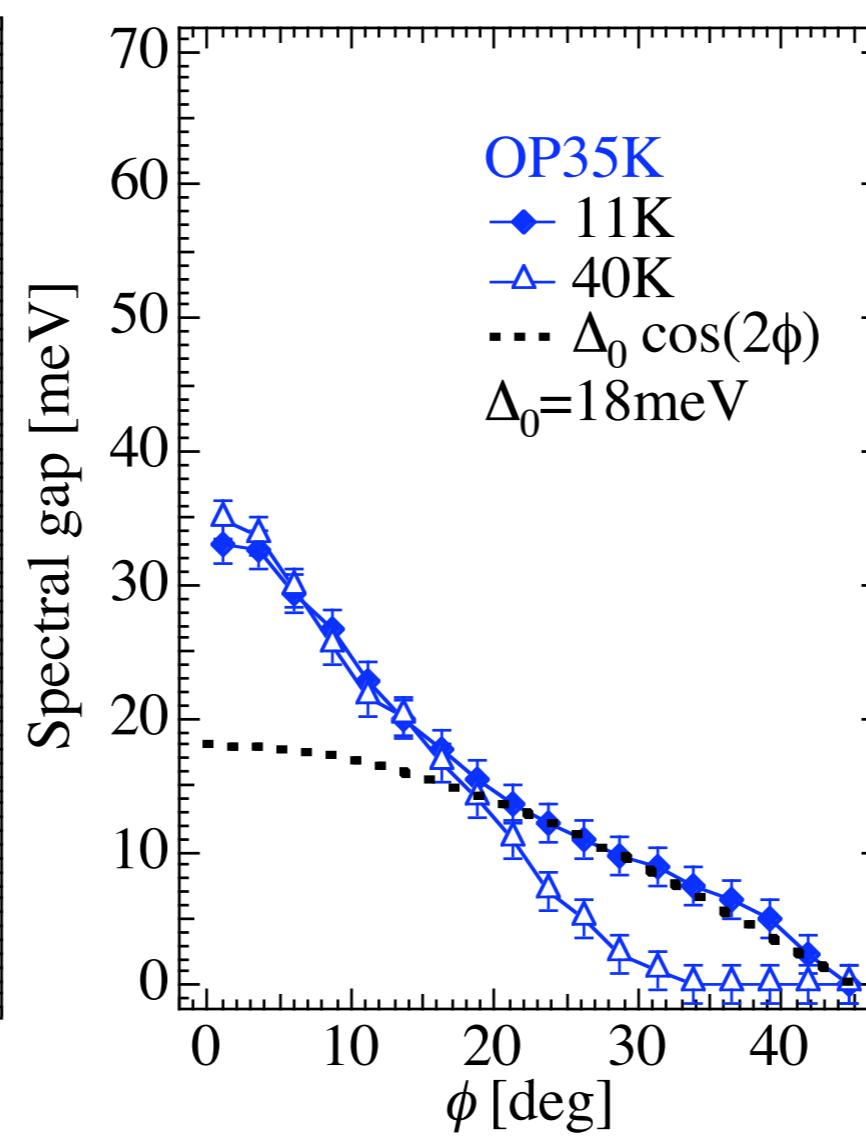
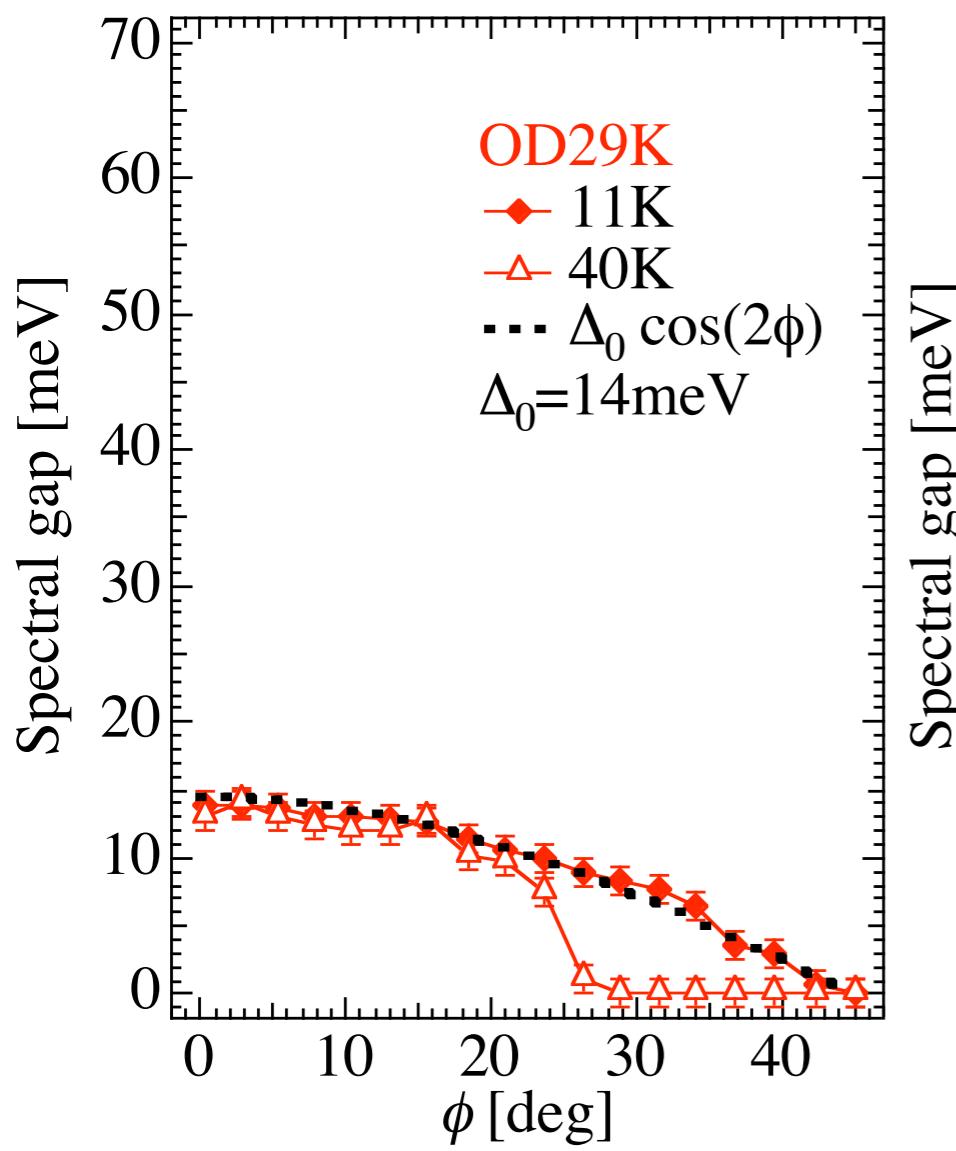


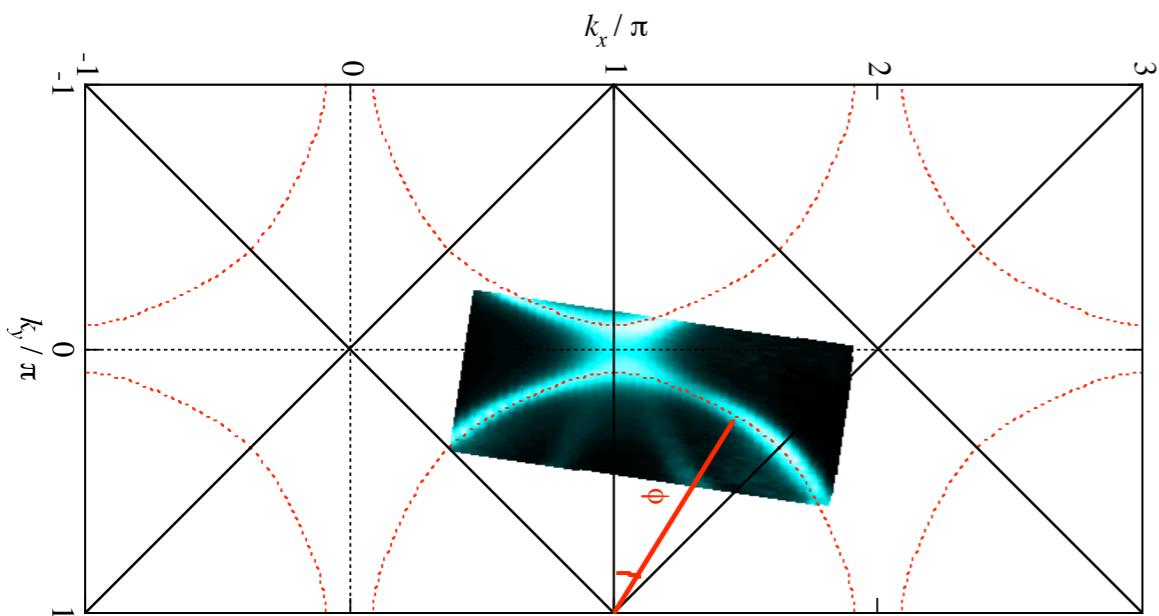
# Spectral gap



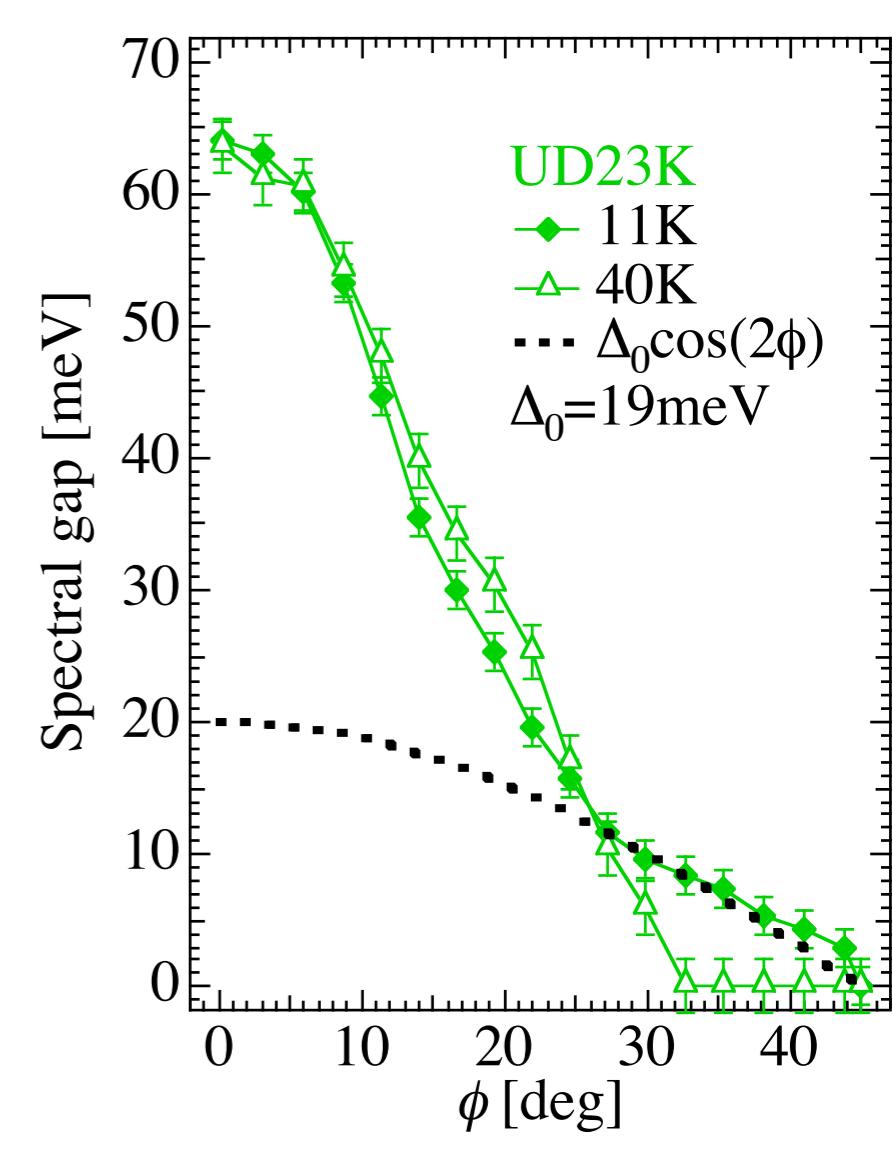
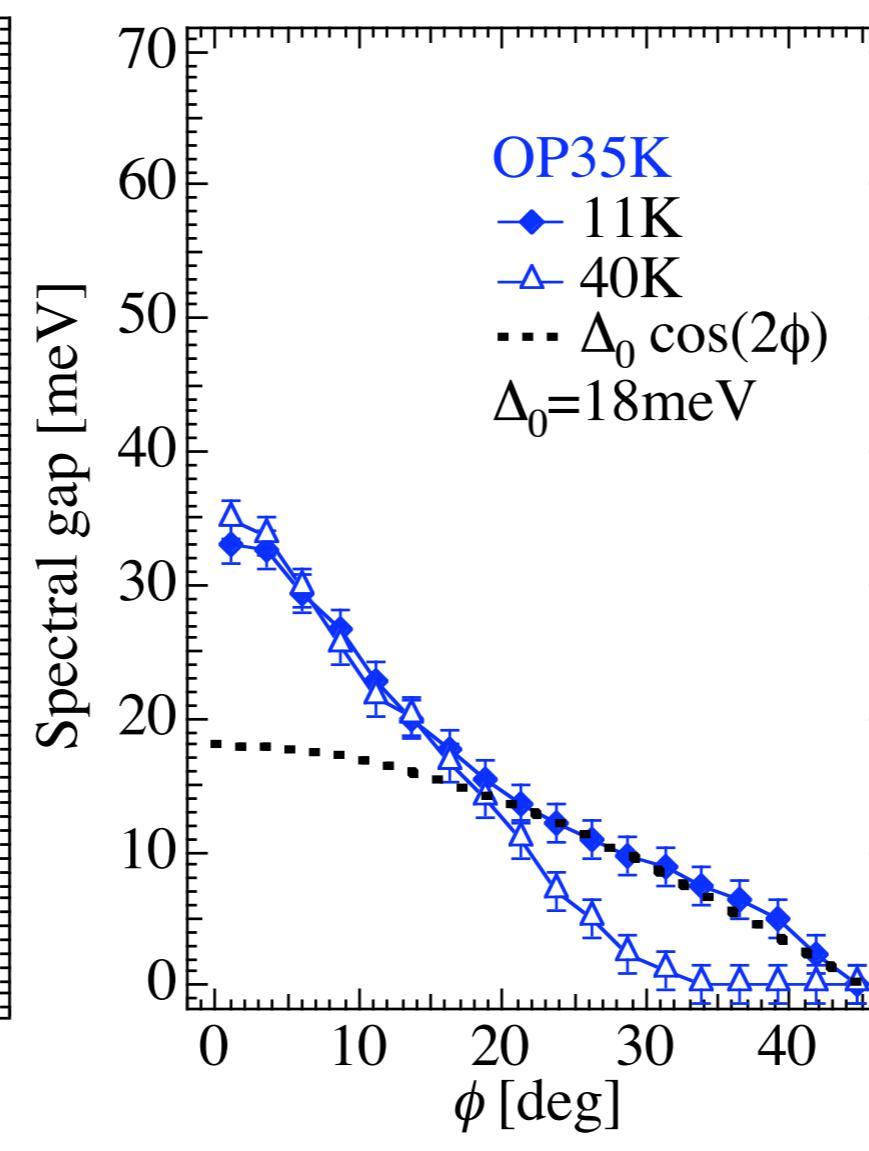
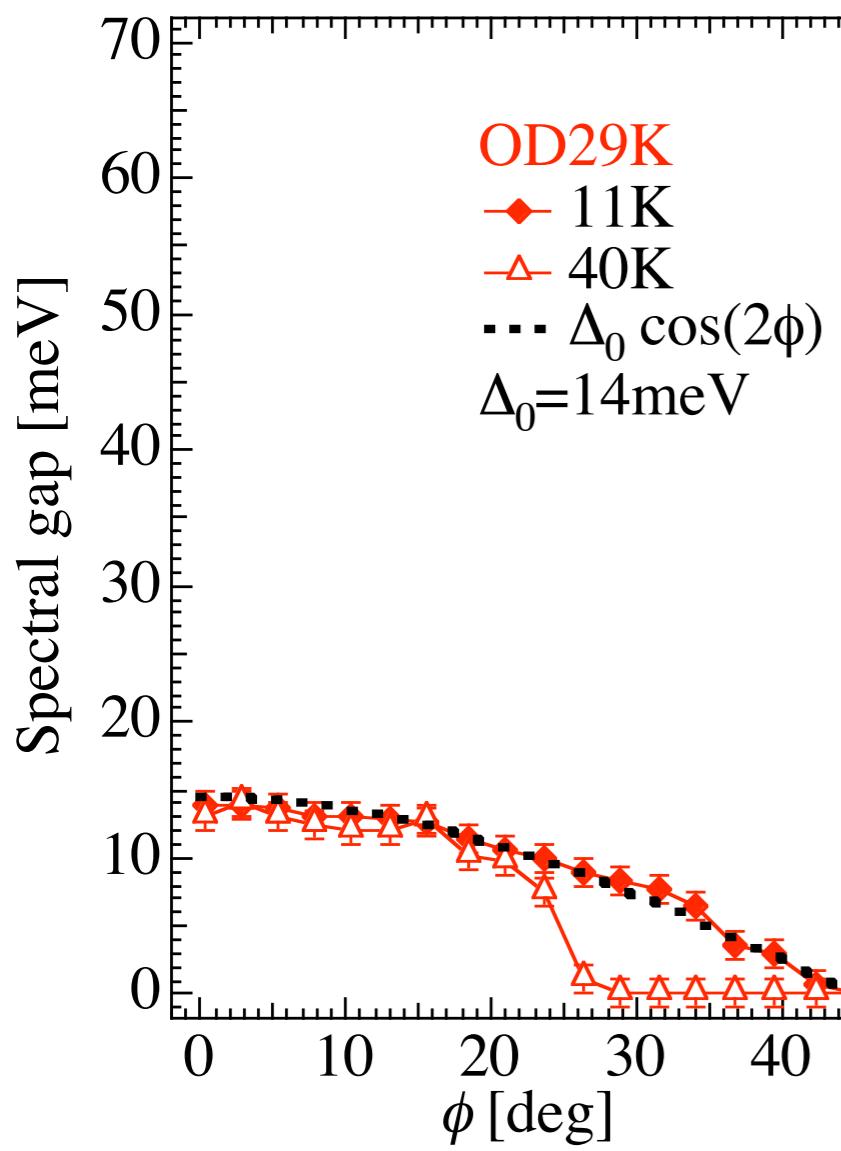


# Spectral gap

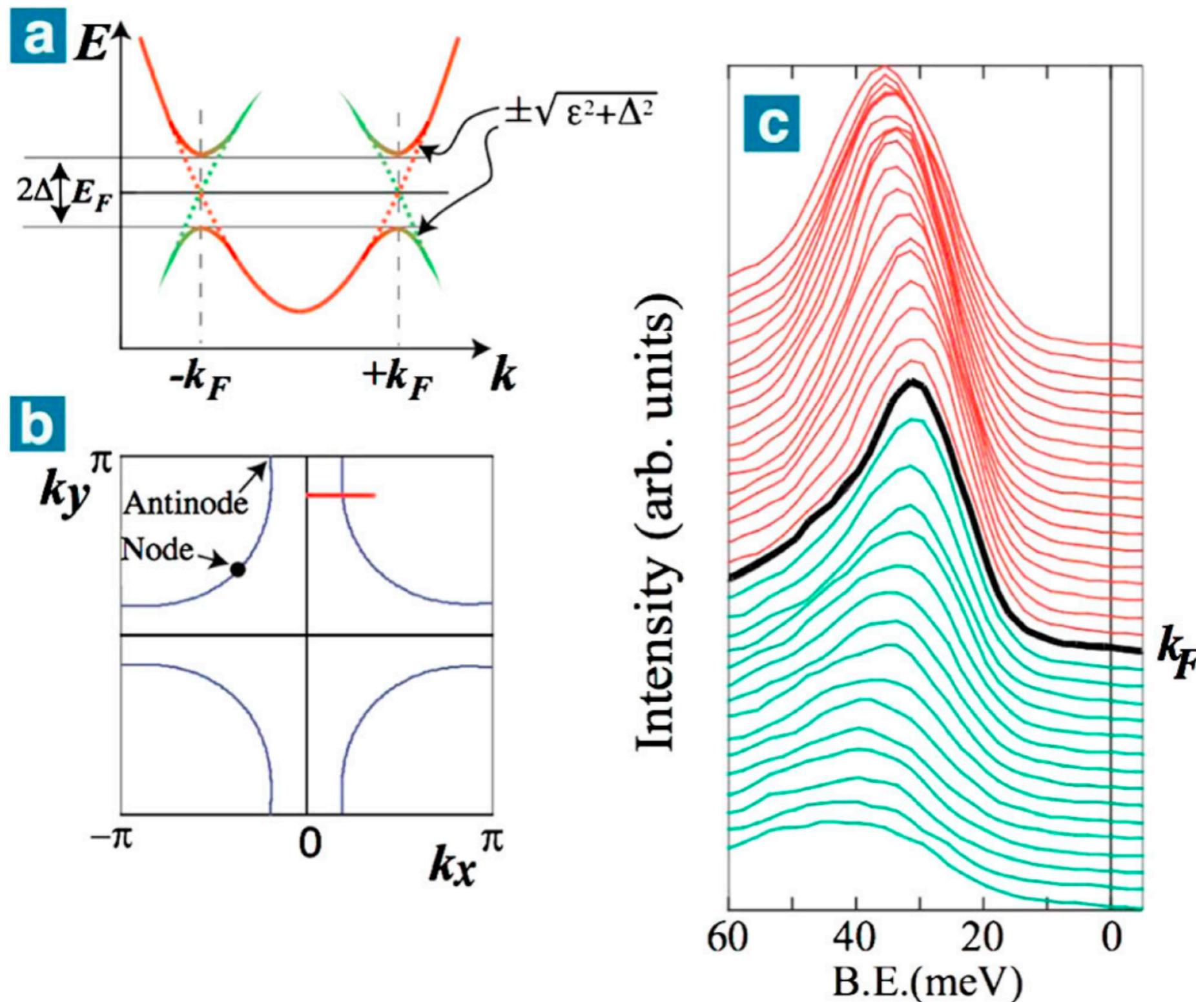




# Spectral gap

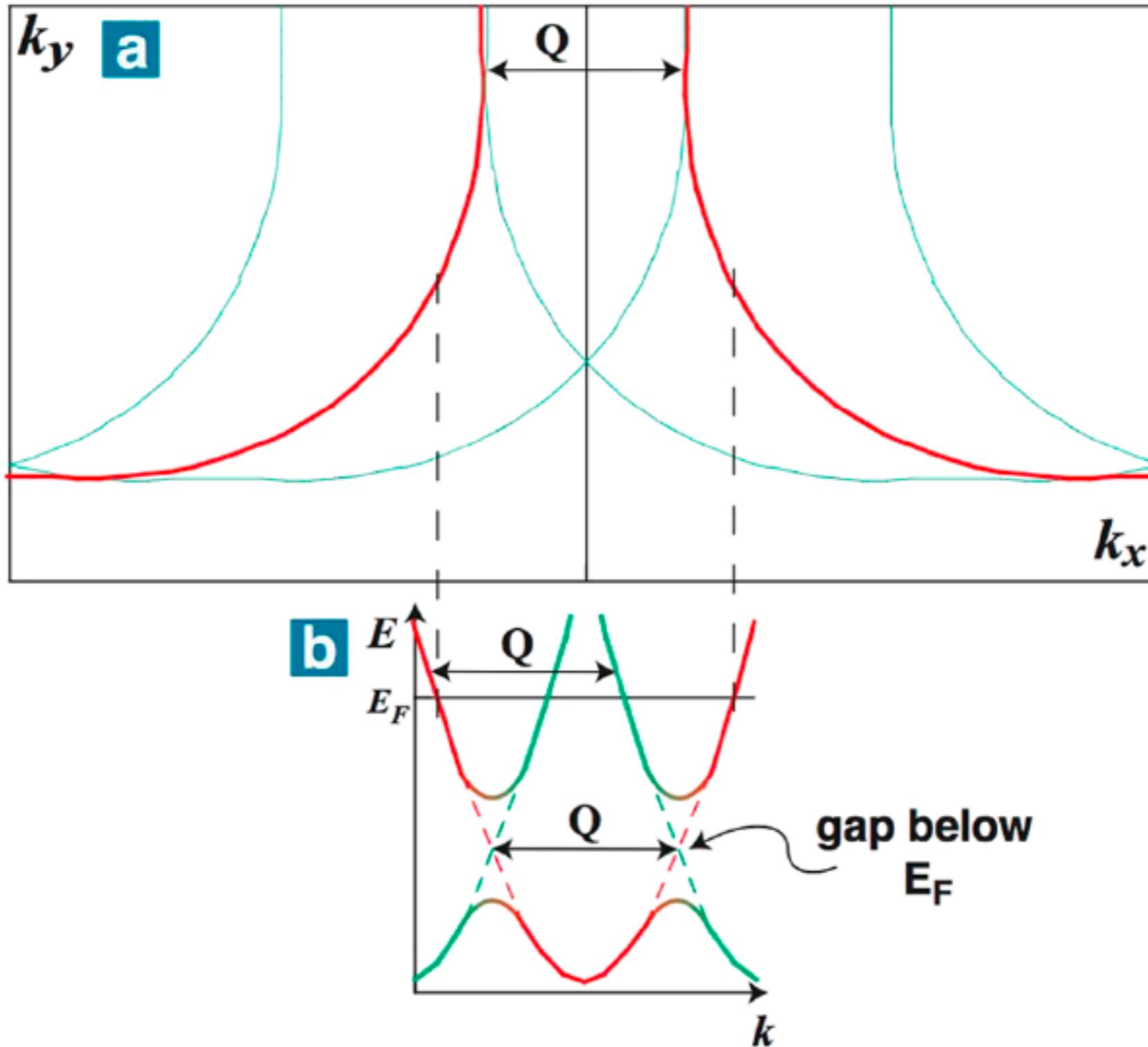


# Superconducting (pairing) gap



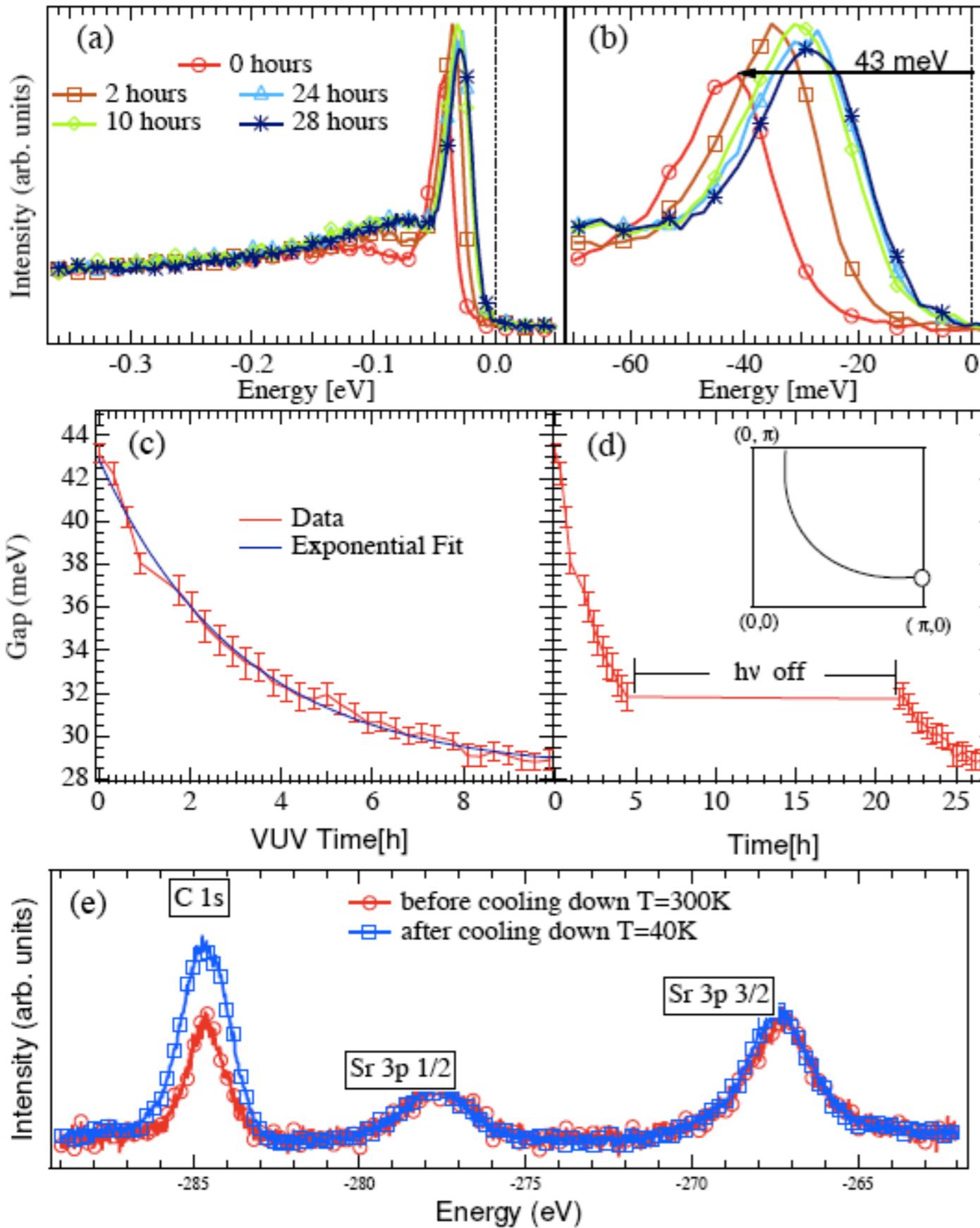
A. Kanigel et al., Phys. Rev. Lett 101, 137002 (2008)

# Charge Density Wave (CDW) gap

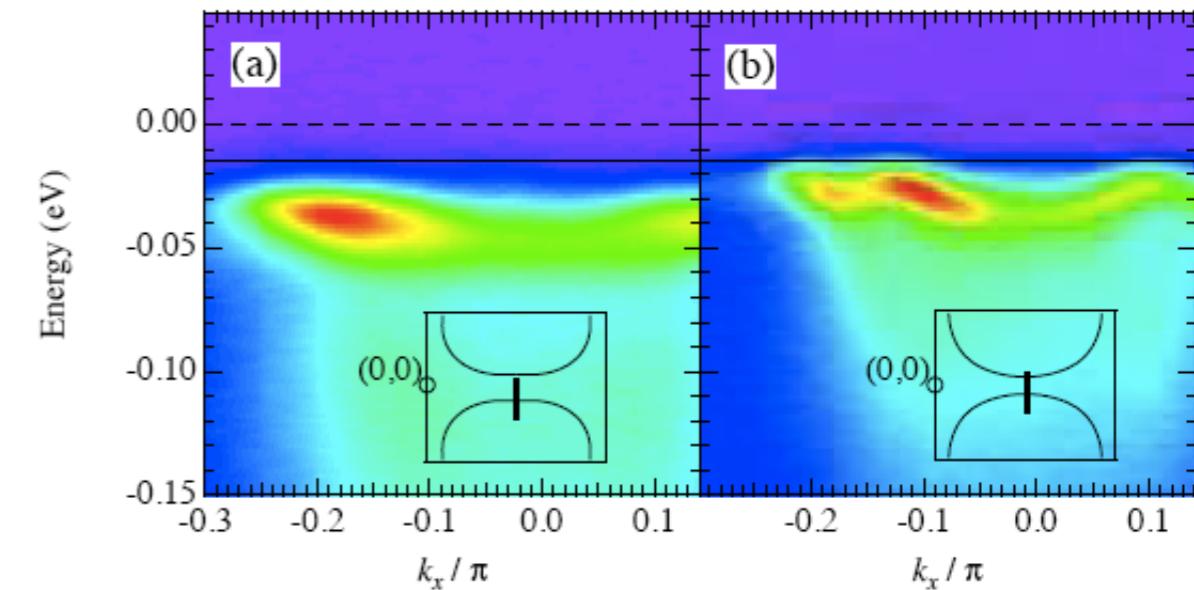


A. Kanigel et al., Phys. Rev. Lett 101, 137002 (2008)

# side note - less than perfect vacuum conditions

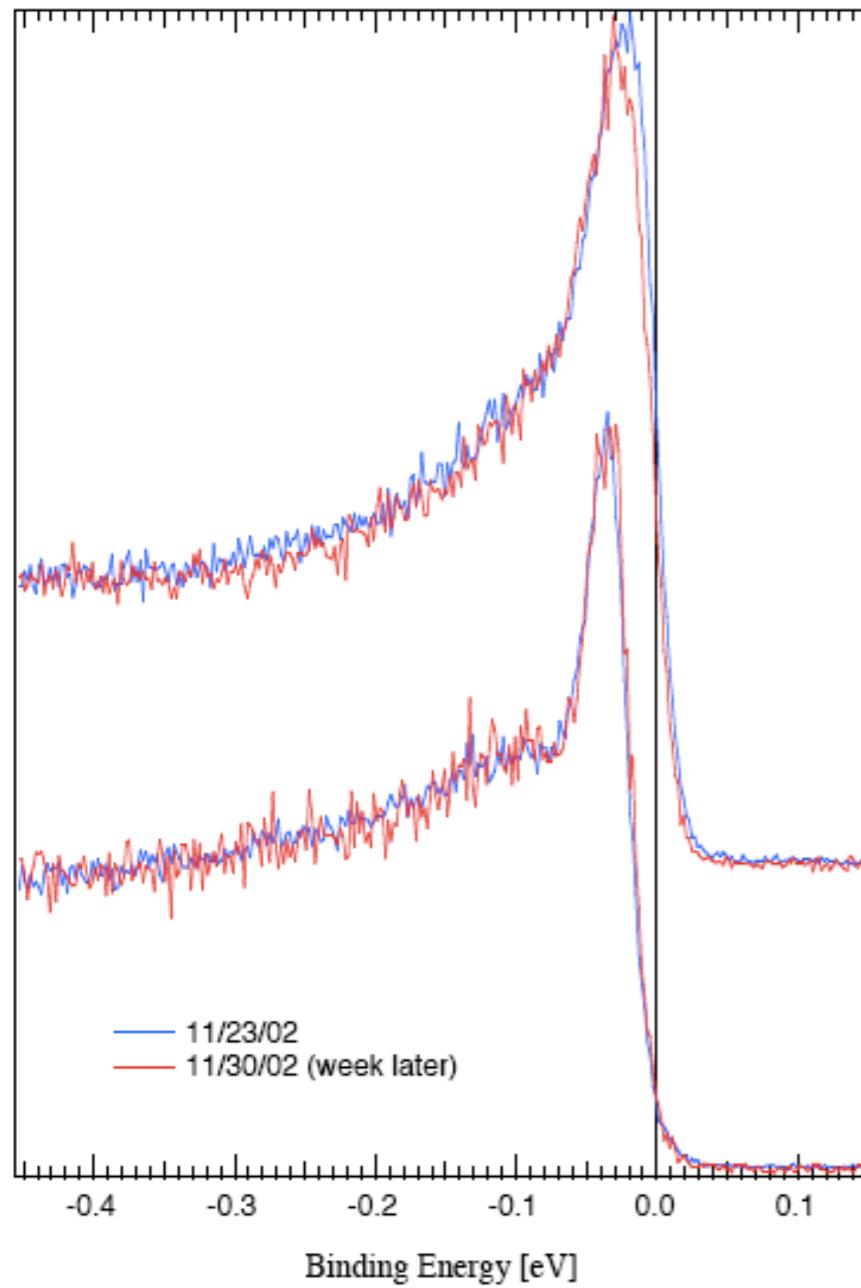


just  
after cleaving      25 hours later

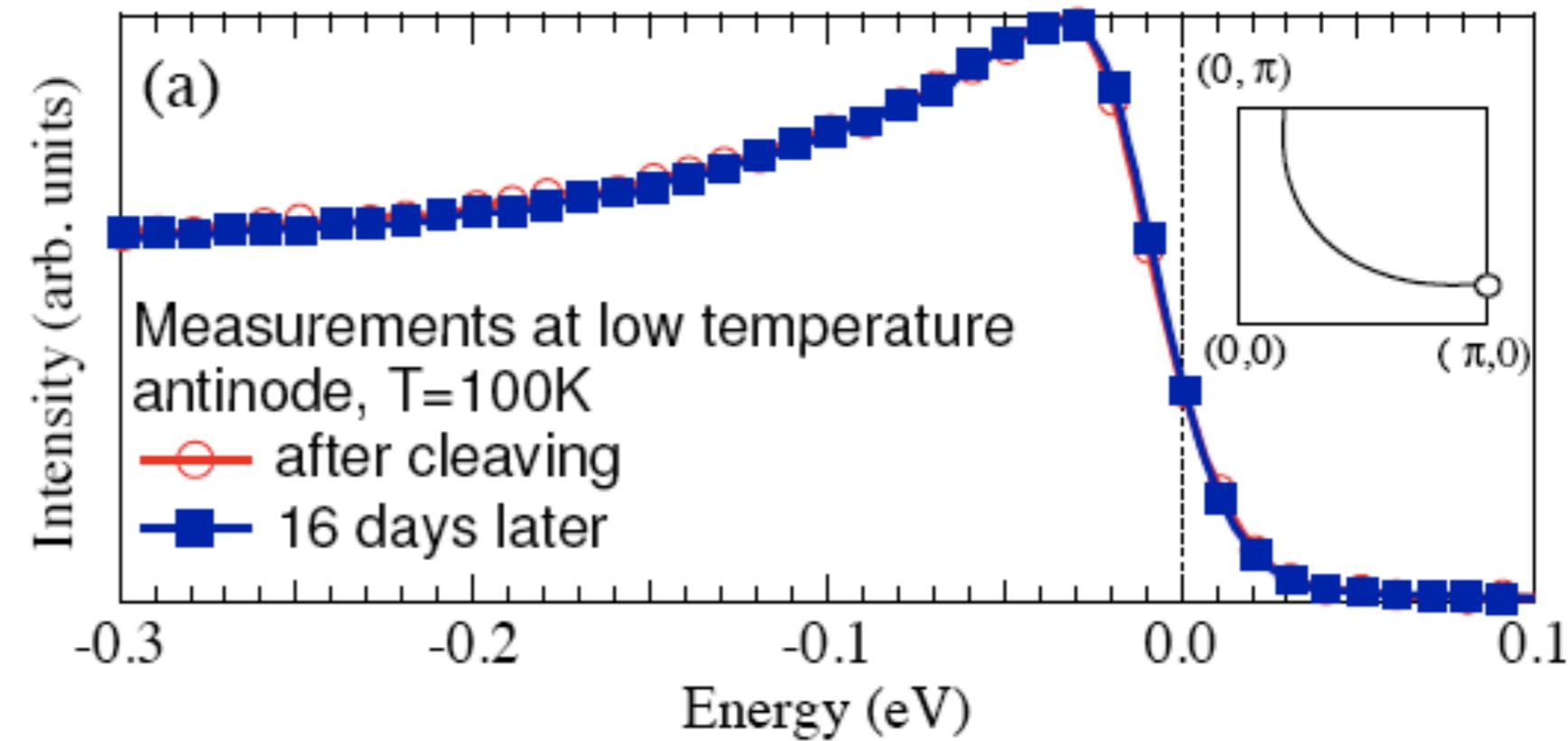


# side note - decent vacuum conditions

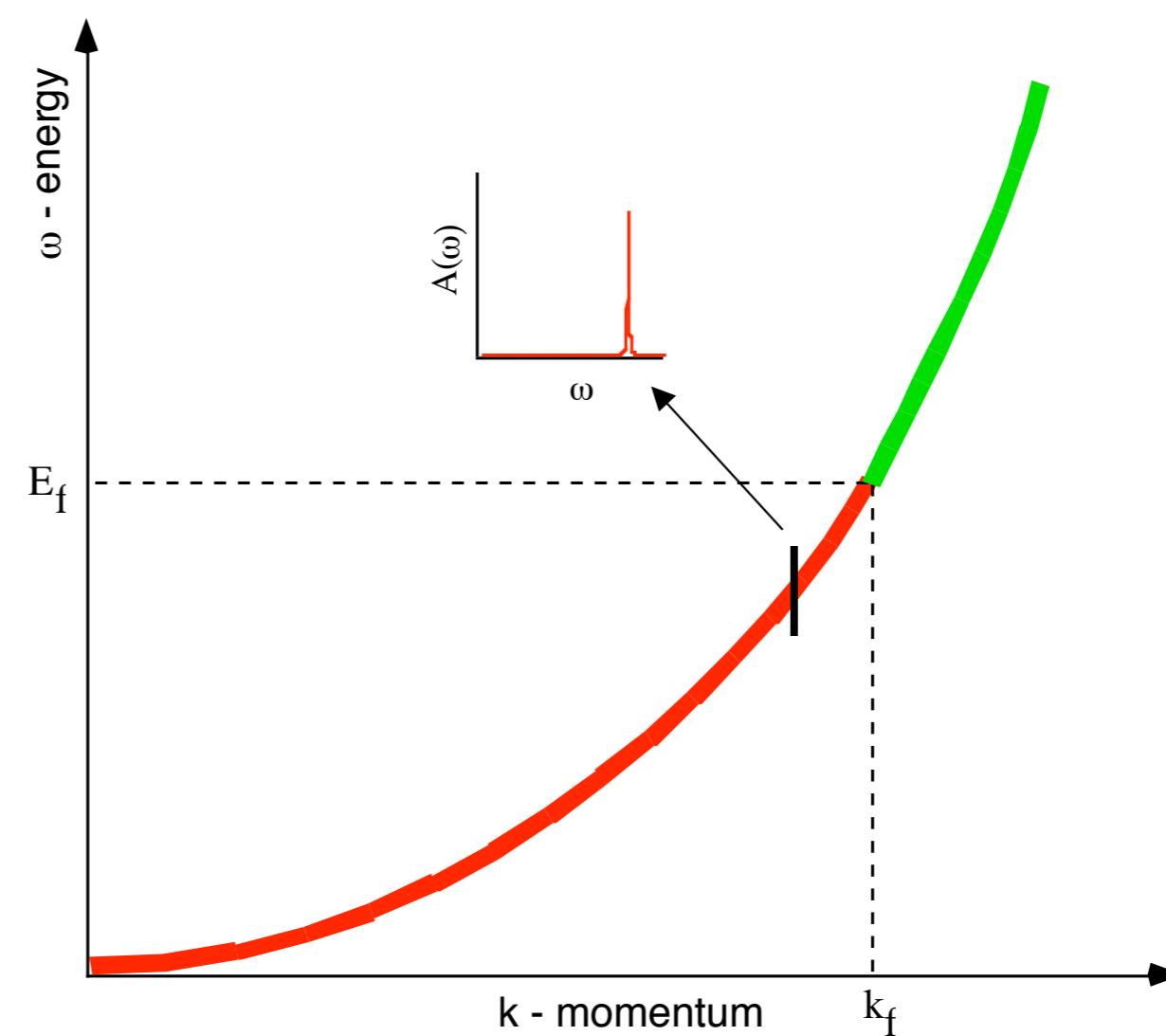
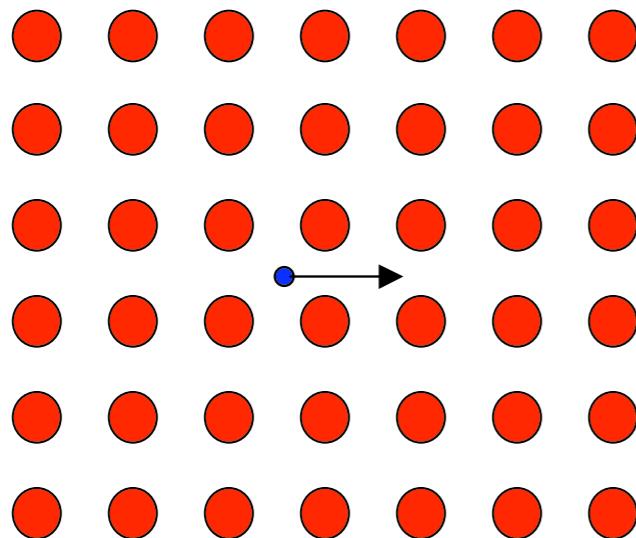
Normalized intensity



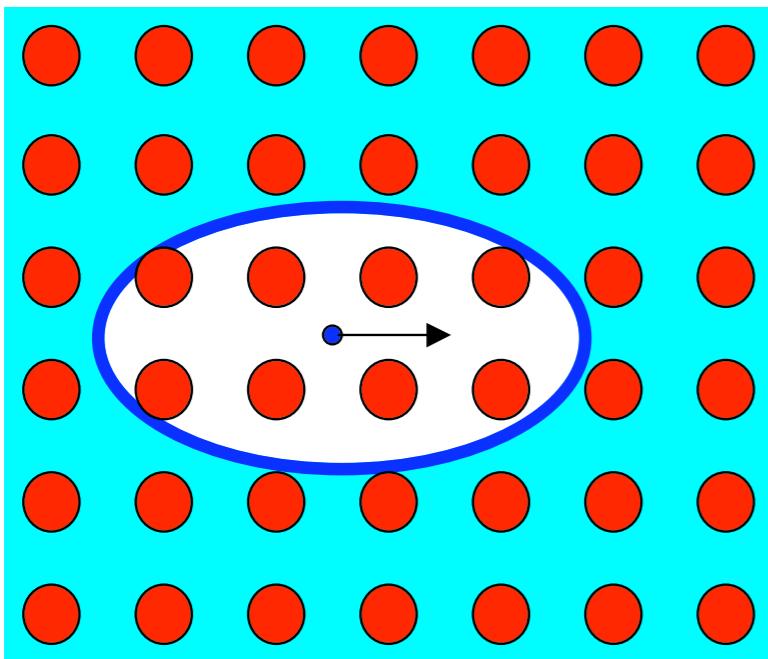
Intensity (arb. units)



## non-interacting electrons - free electron model



## weakly interacting electrons - Fermi liquid model

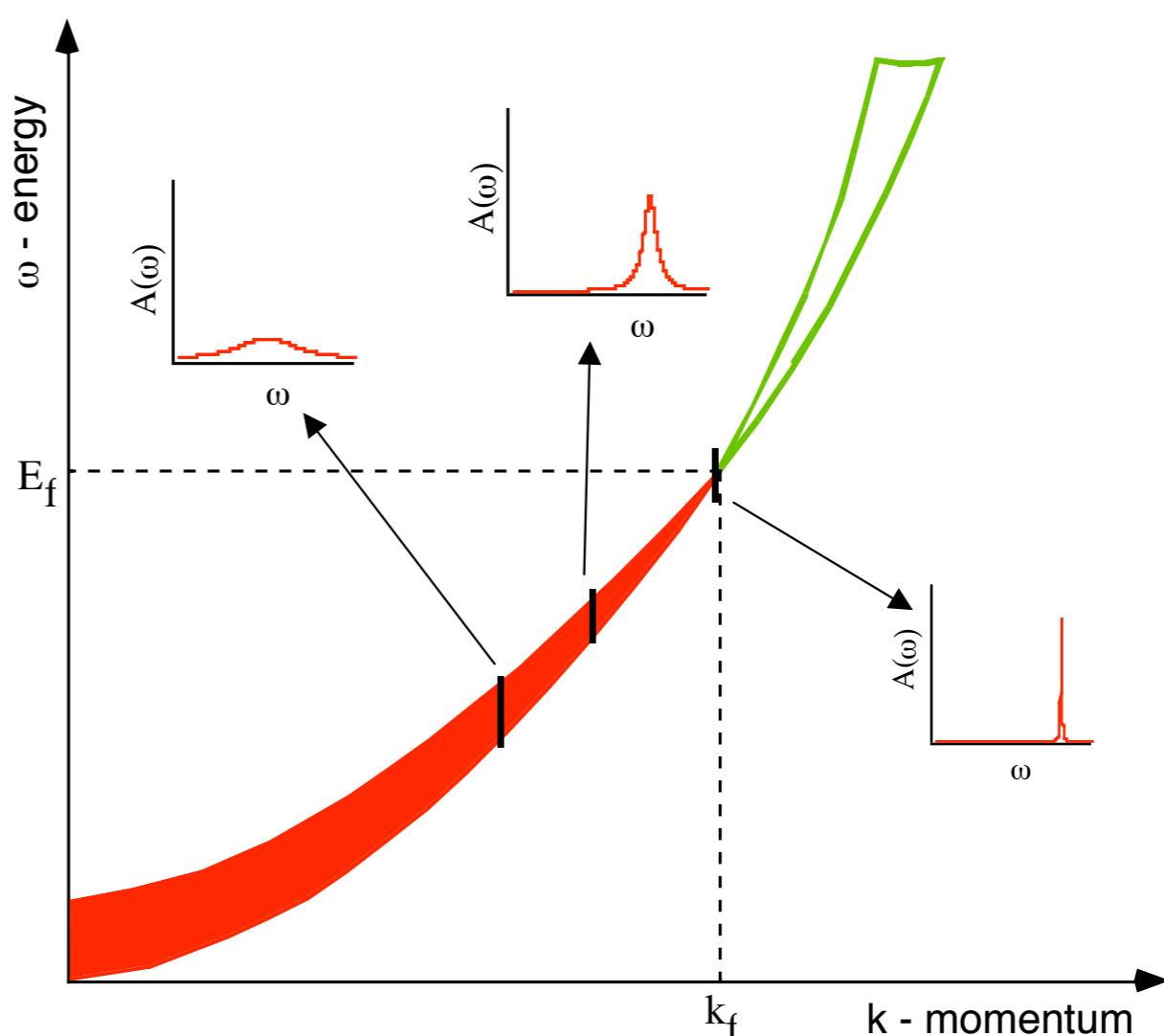


Quasiparticle=“renormalized electron”

$m^*$ ,  $\tau$

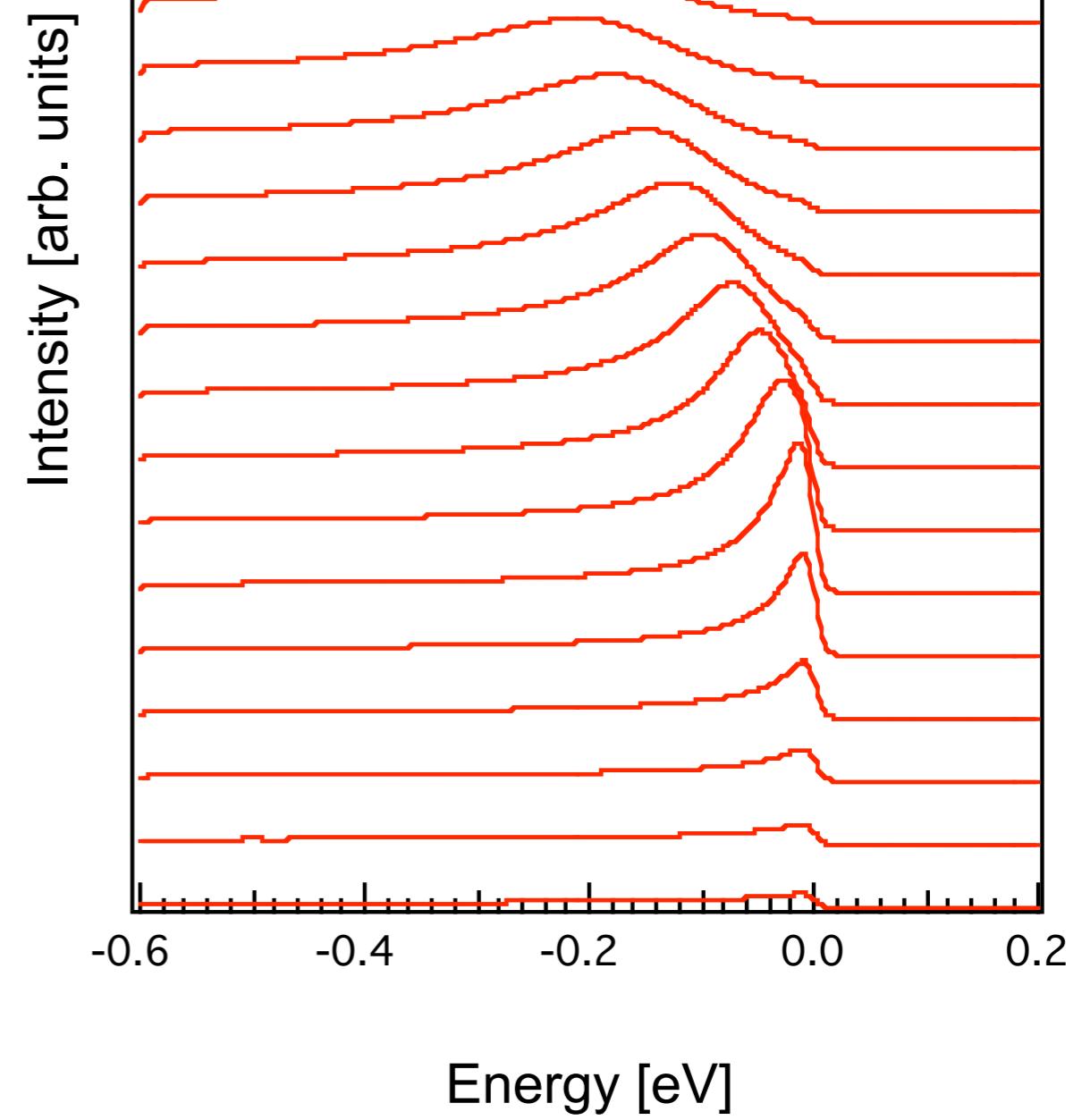
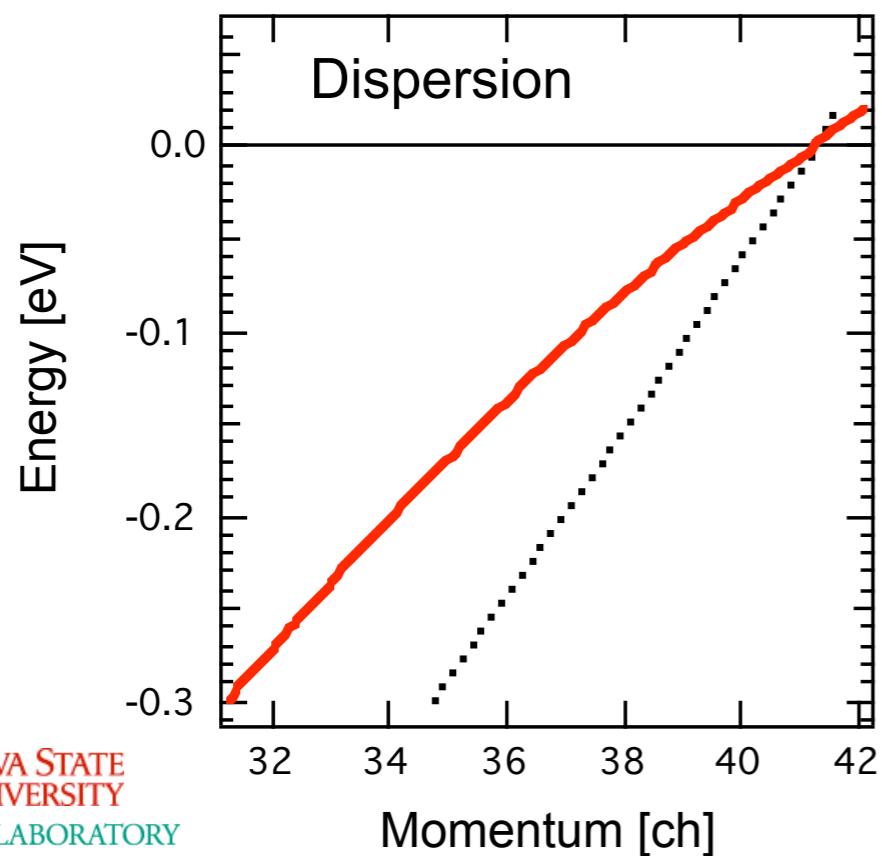
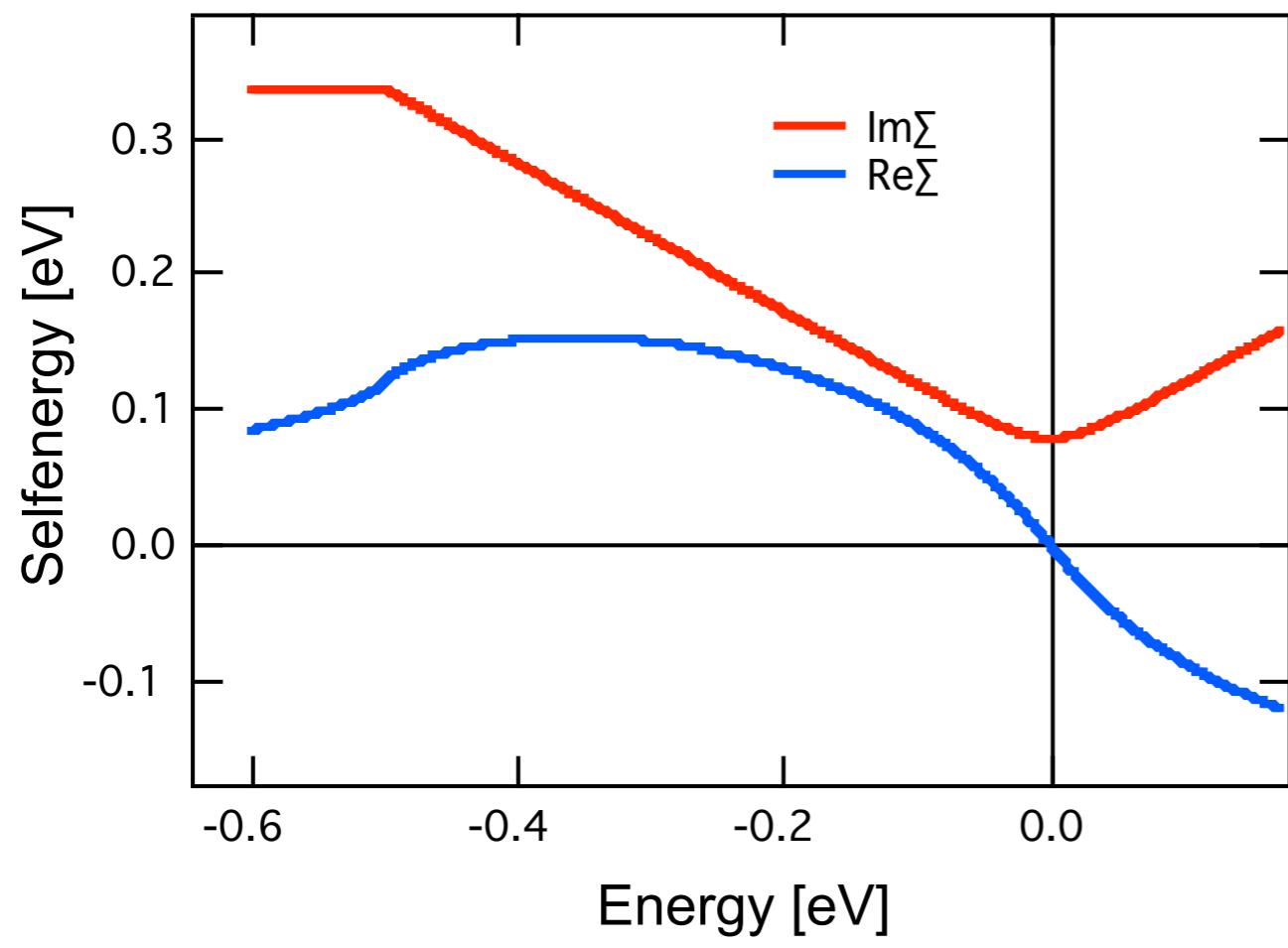
$\Sigma$  – self energy

$$\Sigma(k, \omega) = \alpha\omega + i(\beta\omega^2 + \gamma T^2)$$

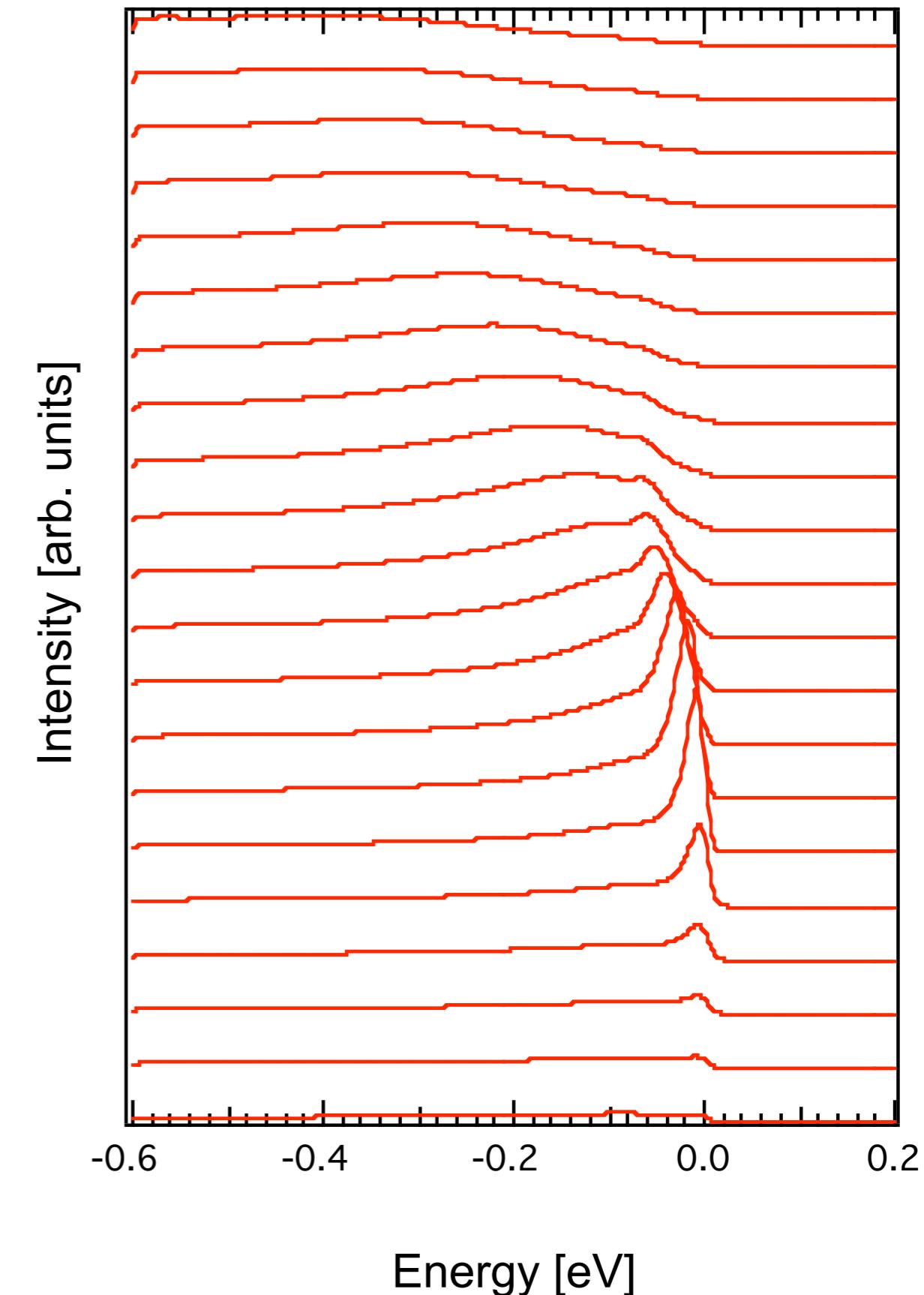
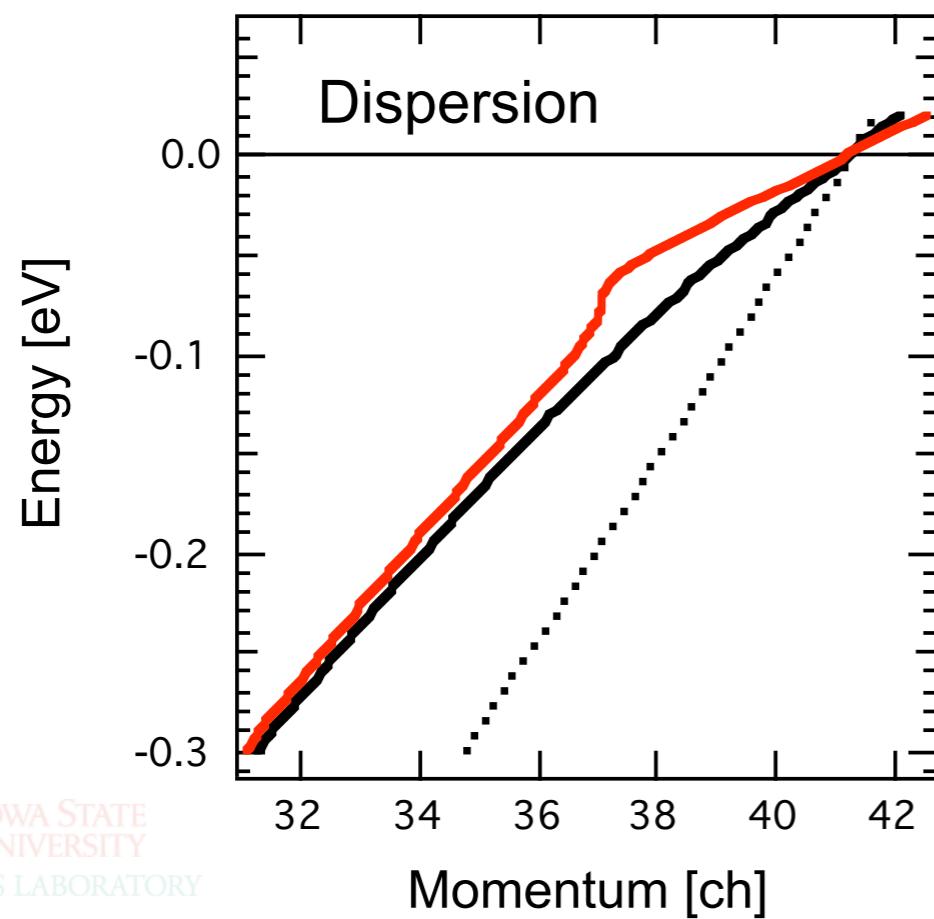
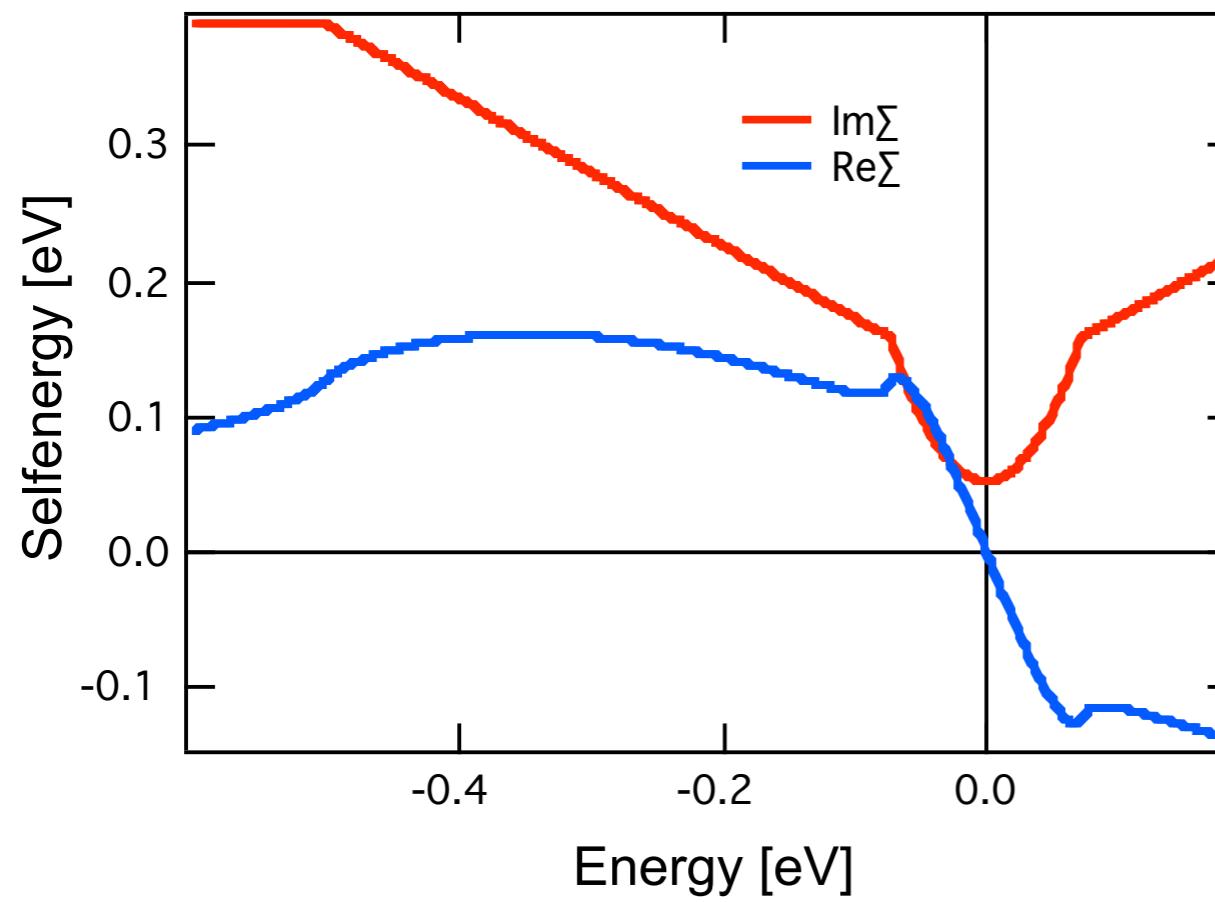


# Scattering rates

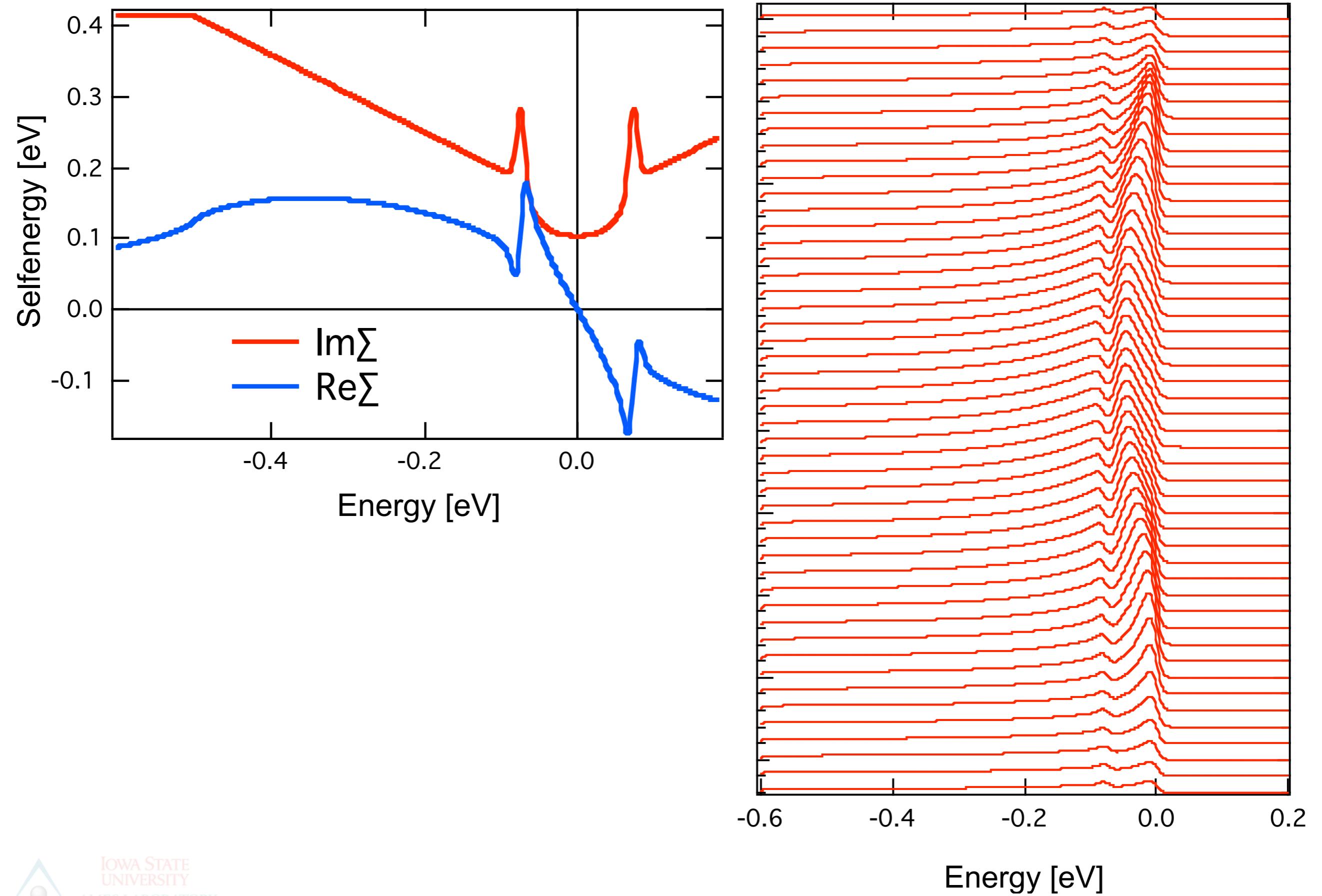
$$A(k, \omega) = \text{Im}(G(k, \omega)) = \frac{\Sigma''(k, \omega)}{(\omega - \epsilon(k) - \Sigma'(k, \omega))^2 - (\Sigma''(k, \omega))^2}$$



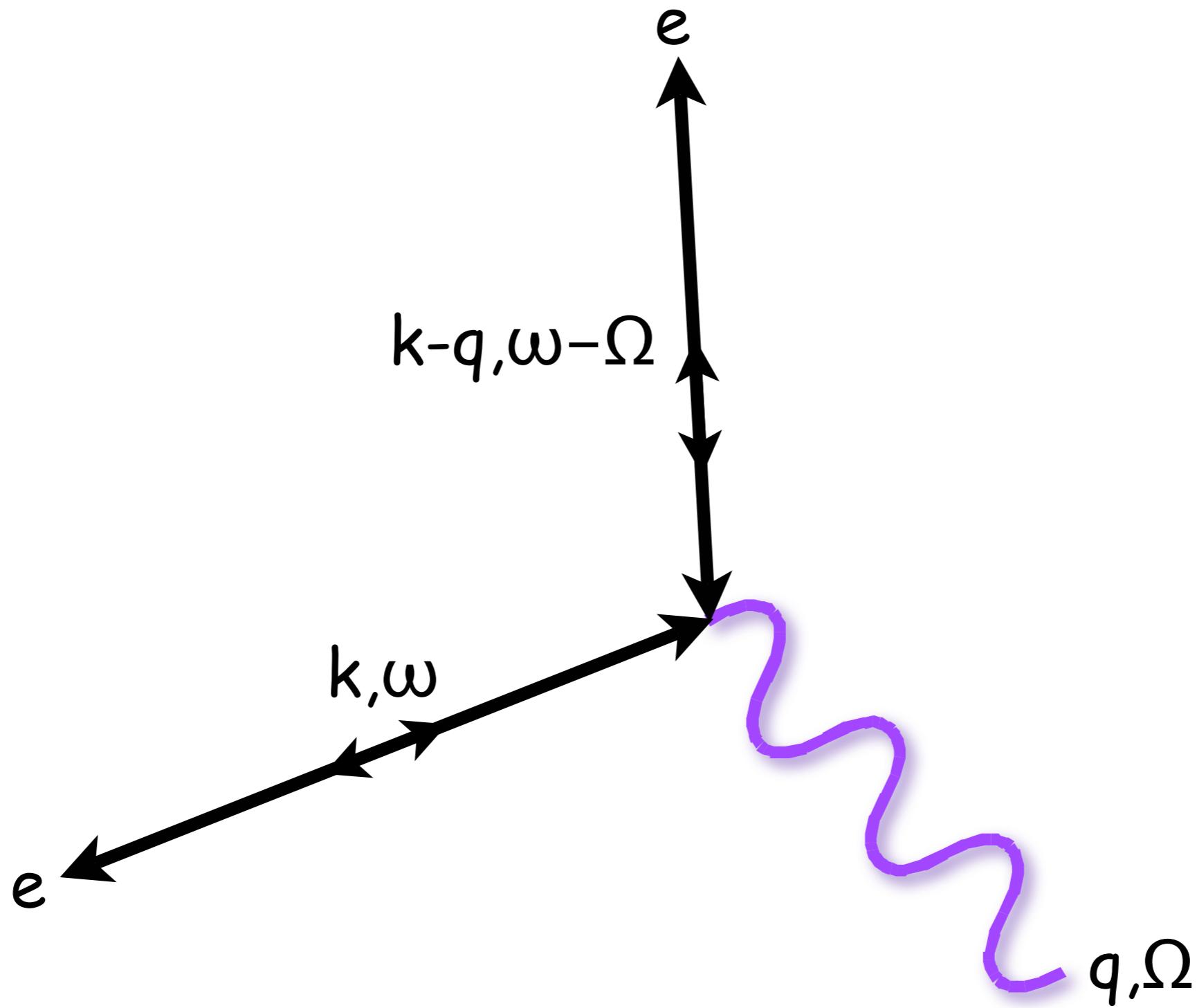
# Simulation - weak interaction with collective mode

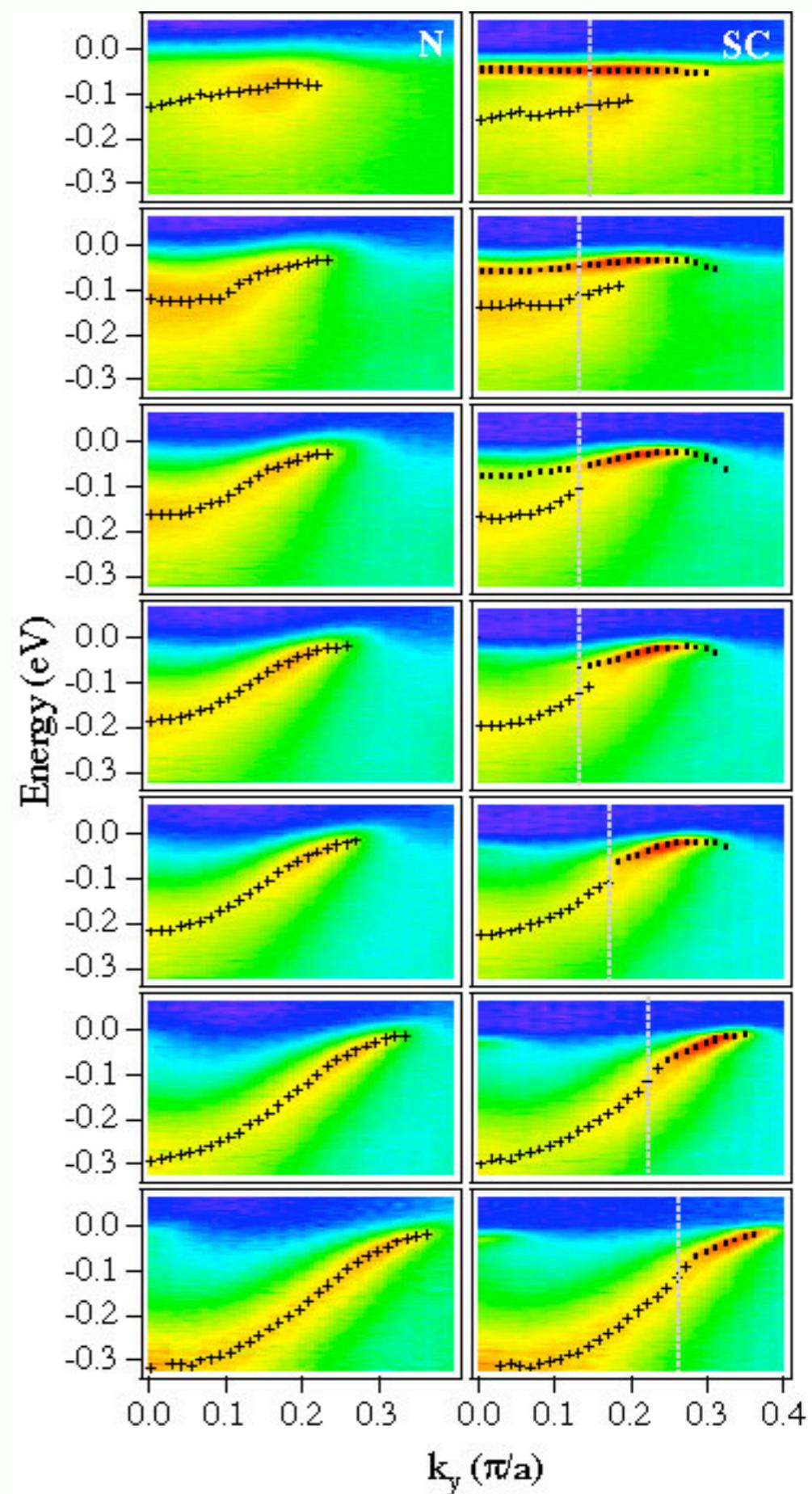
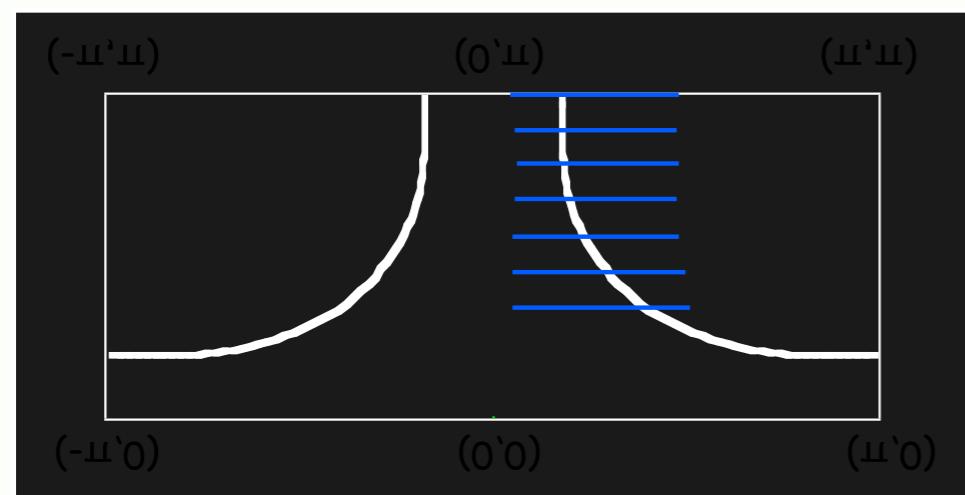


# Simulation - strong interaction with collective mode

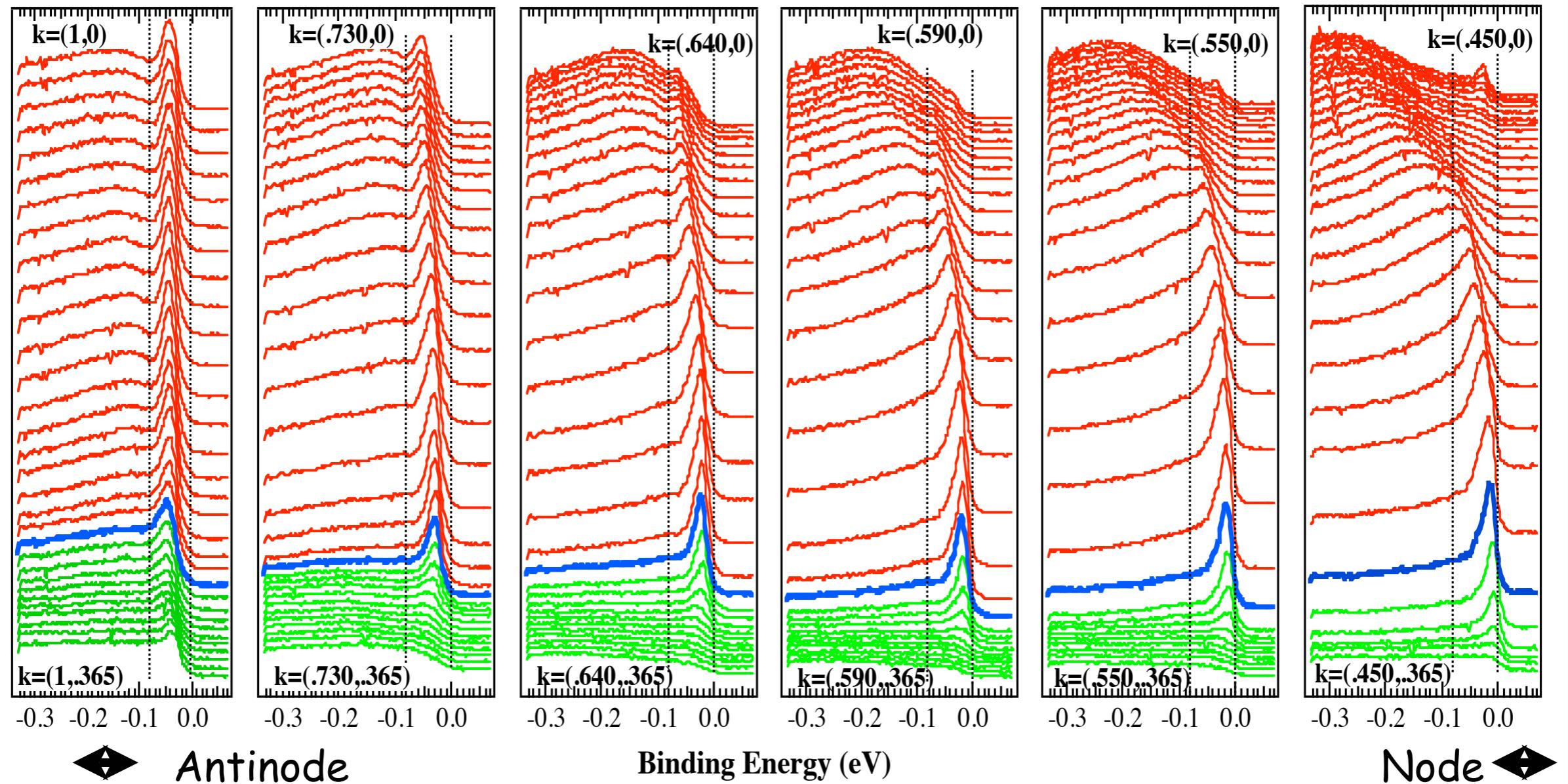


# Collective modes

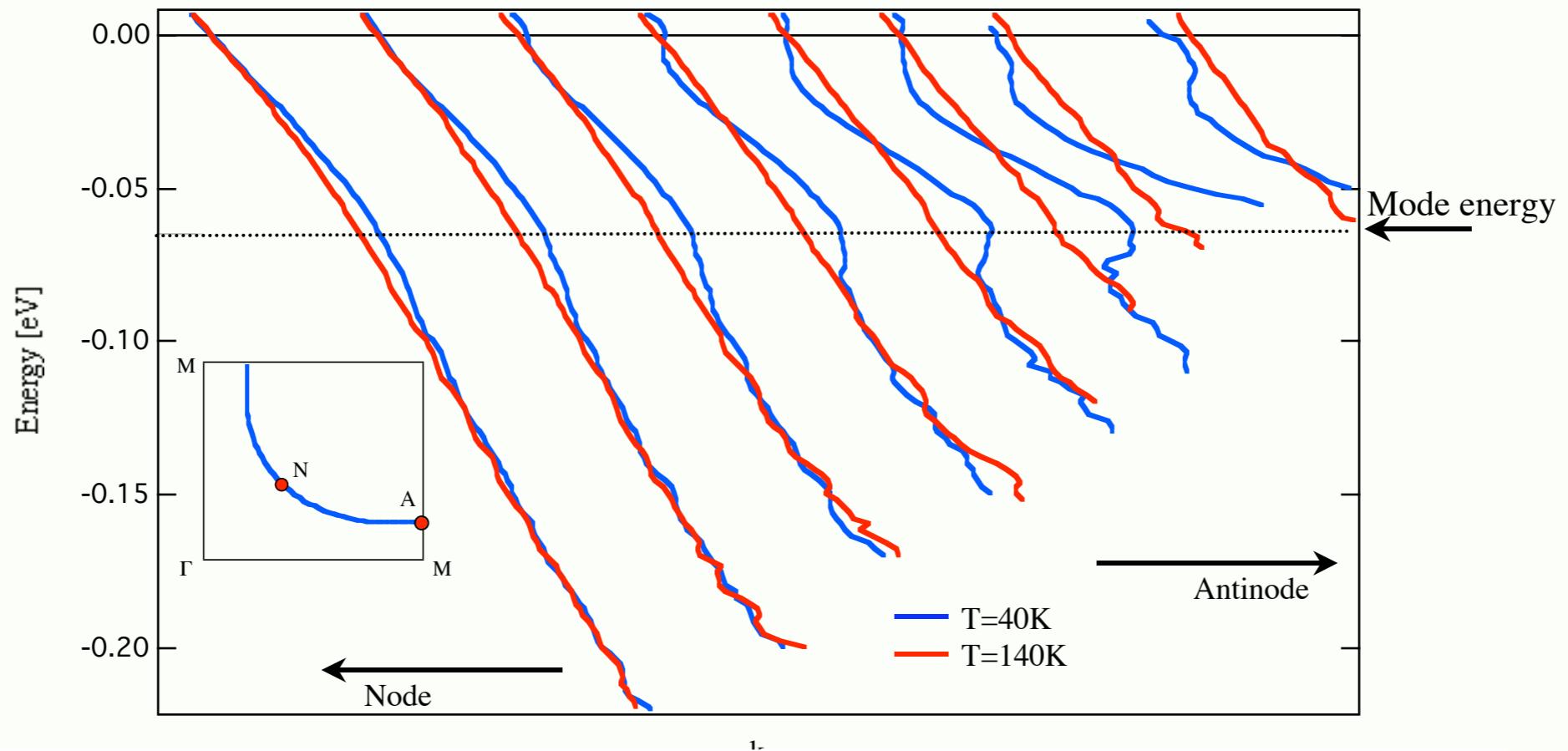




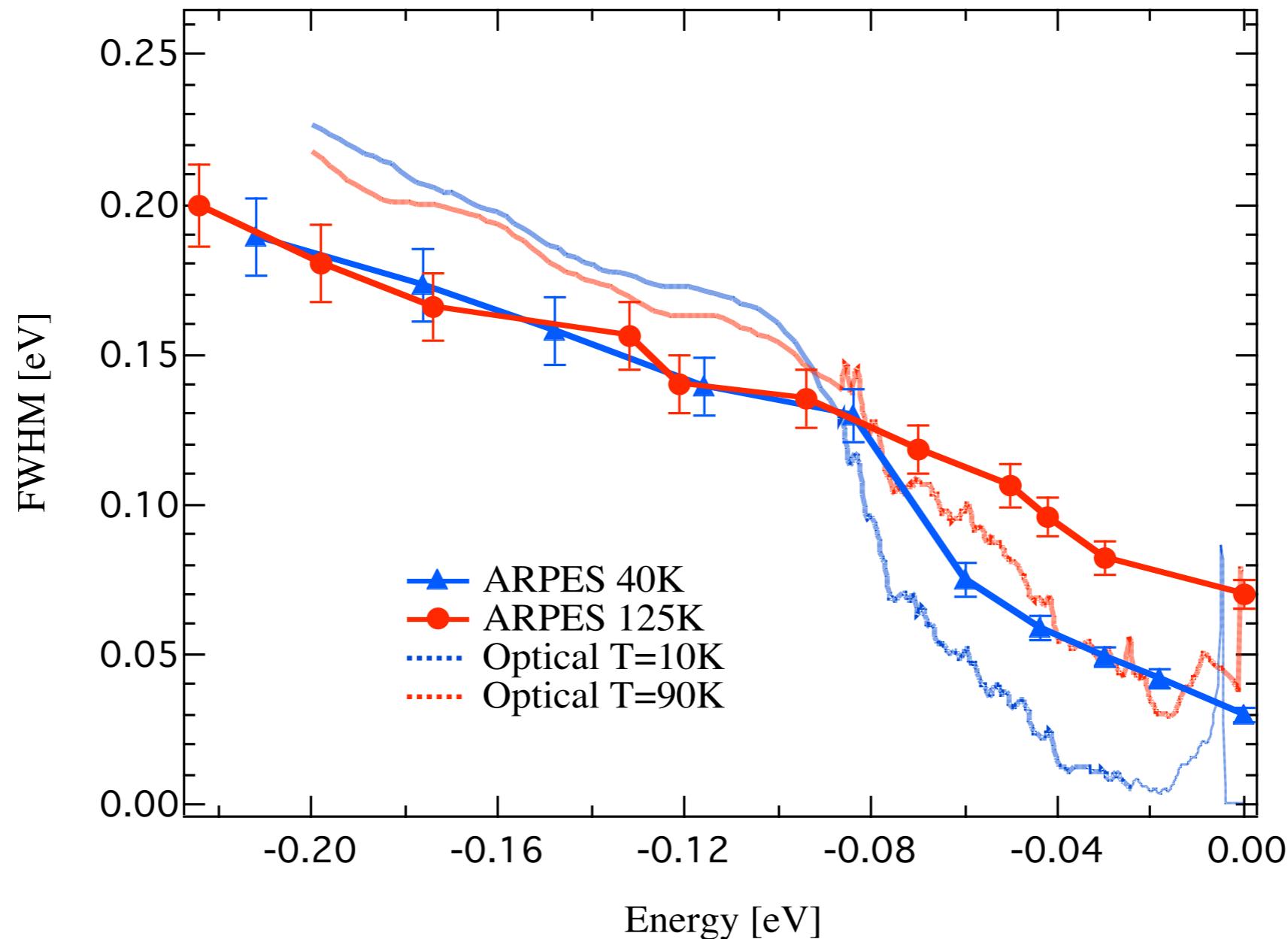
# EDC's in the superconducting state



## Interaction of the electrons with a collective mode



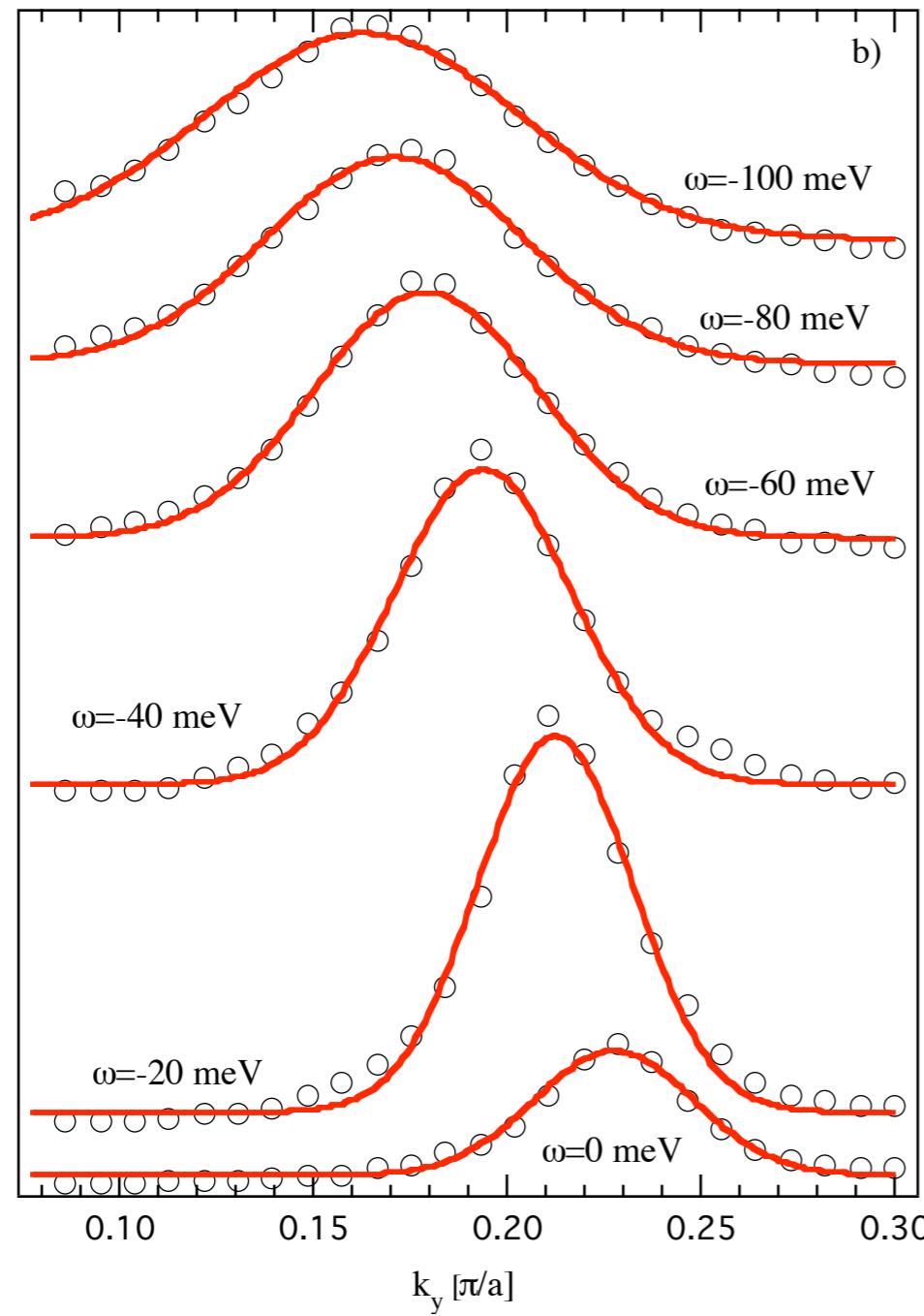
# Self energy ( $\Rightarrow$ scattering rate)



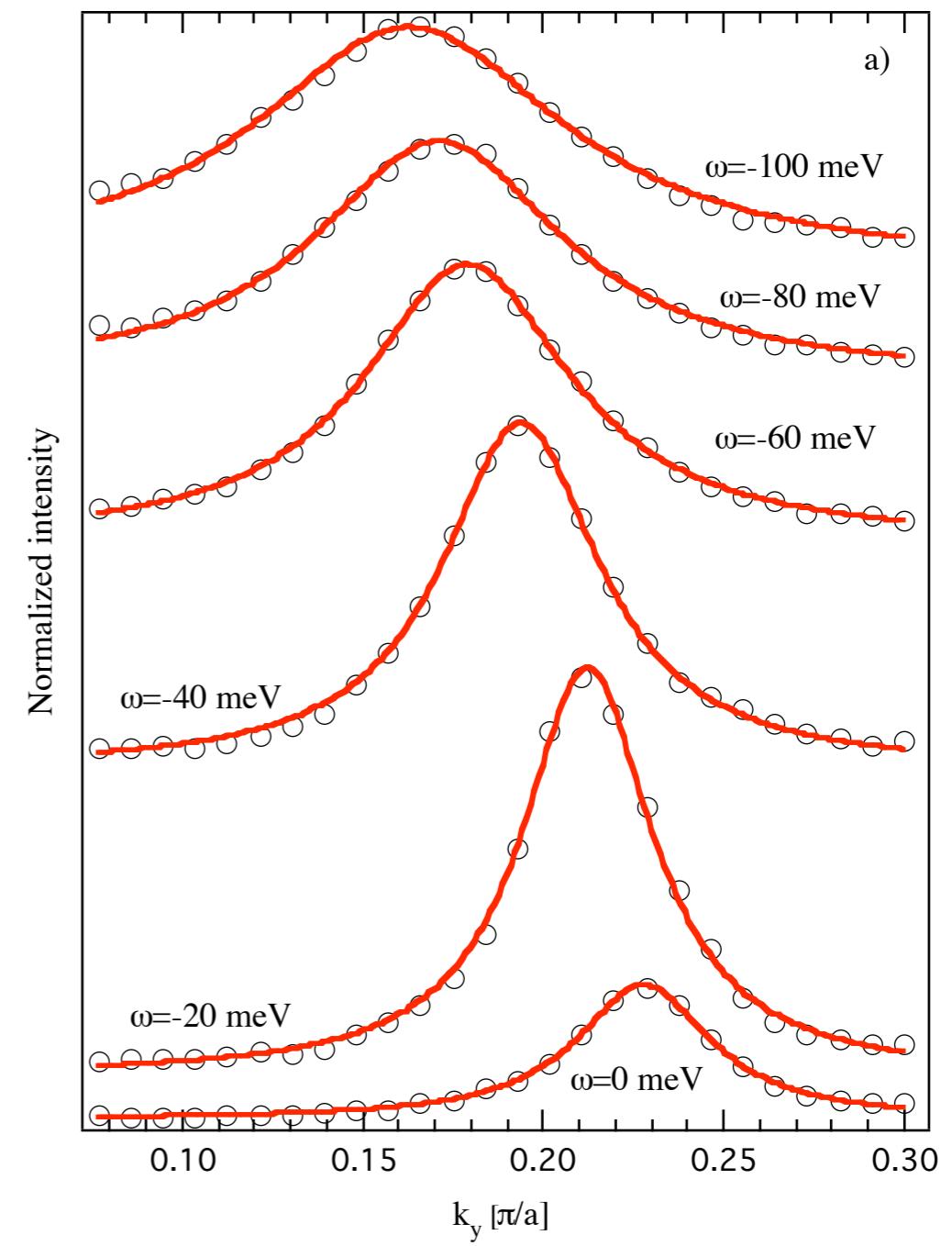
ARPES estimate of of scattering rate compares well to the one obtained from optical reflectivity data  
A.V. Puchkov, D.N. Basov, and T. Timusk, J. Phys. Condens. Matter **8**, 10 049 (1996).

# Fits to the MDCs':

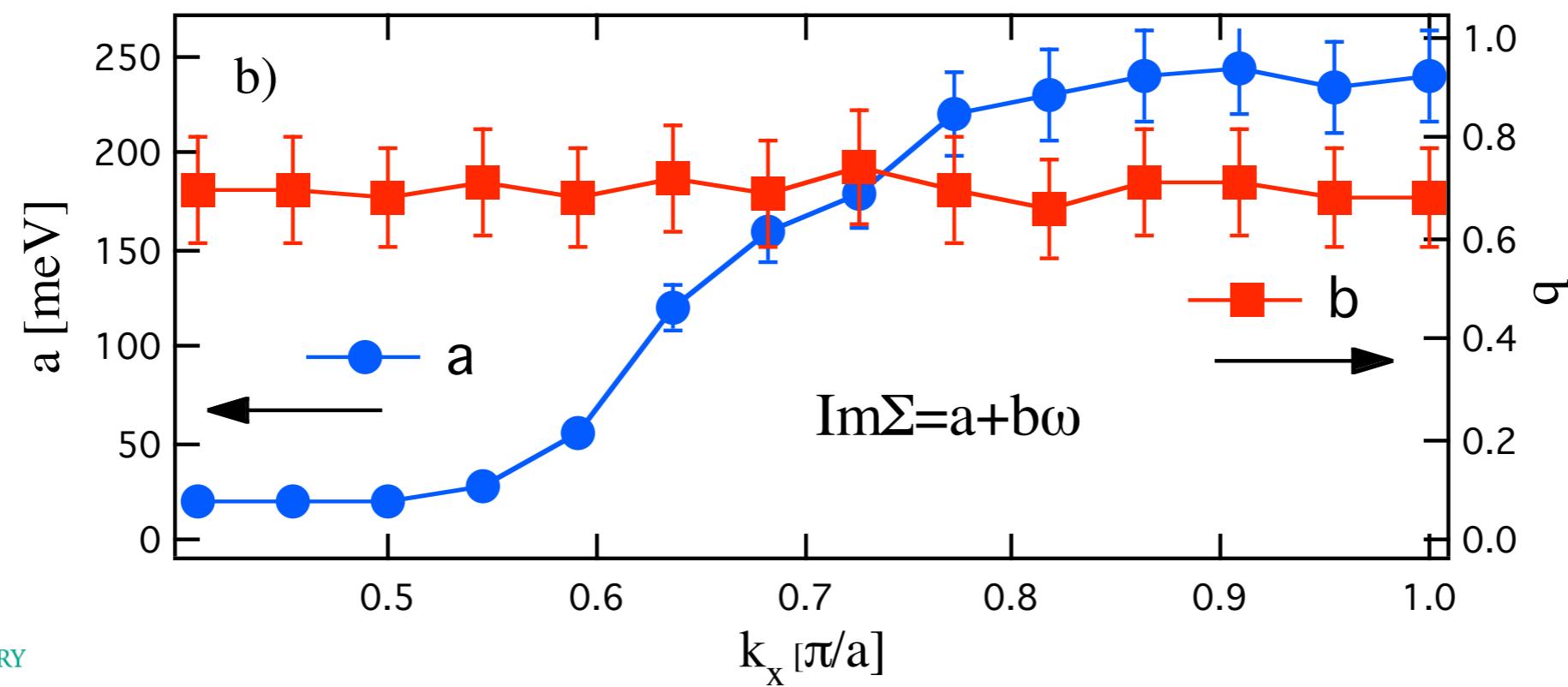
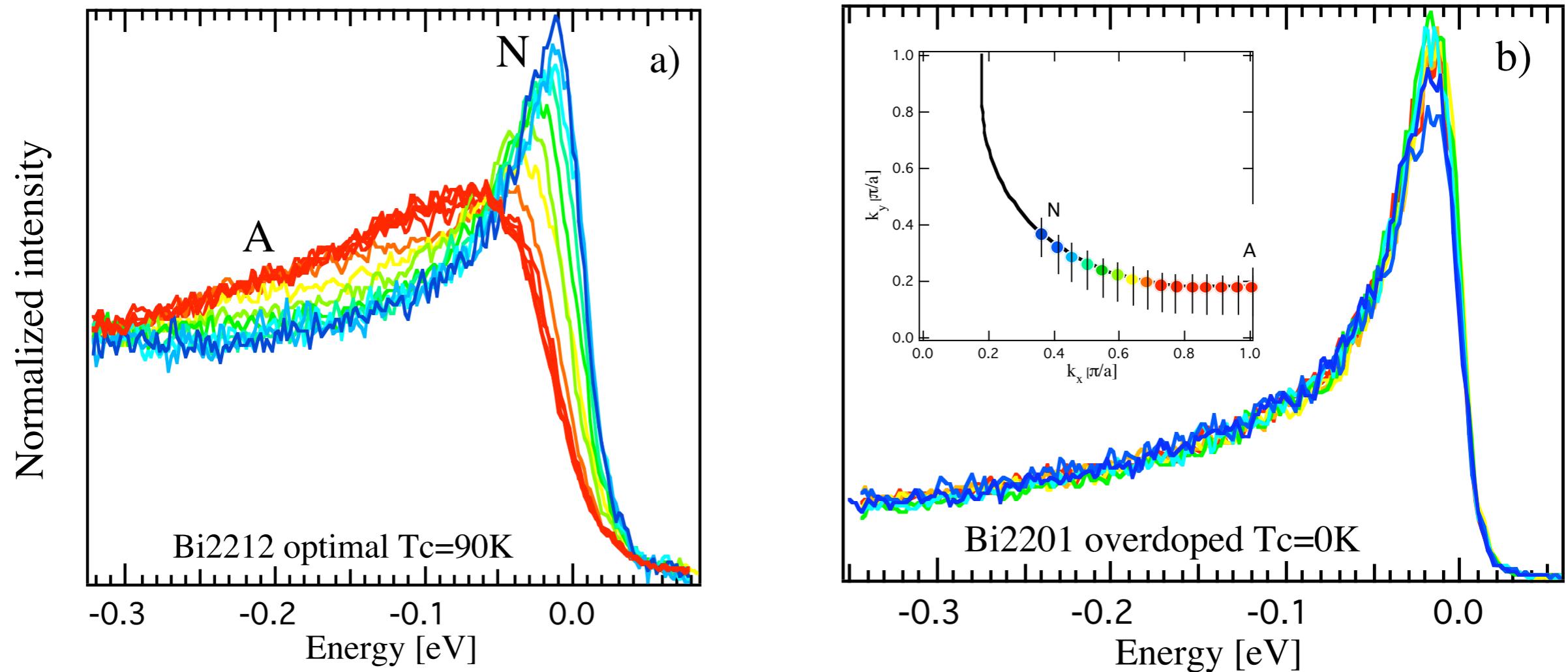
gaussian

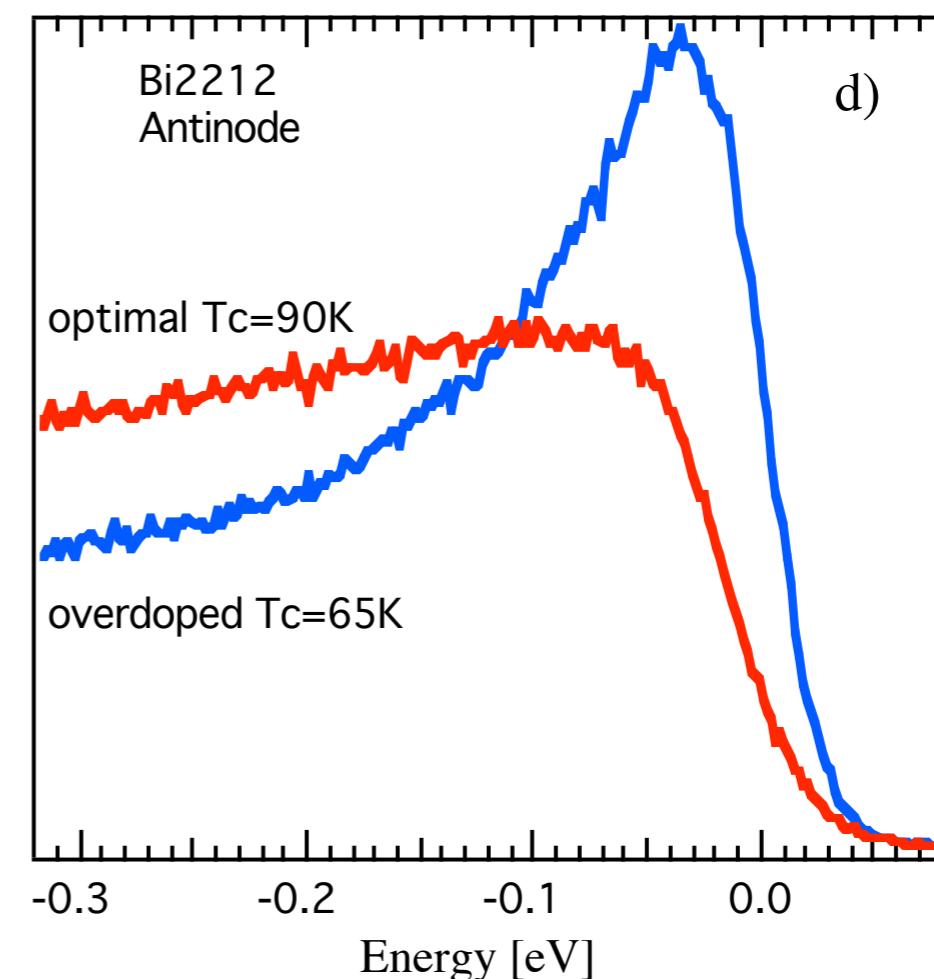
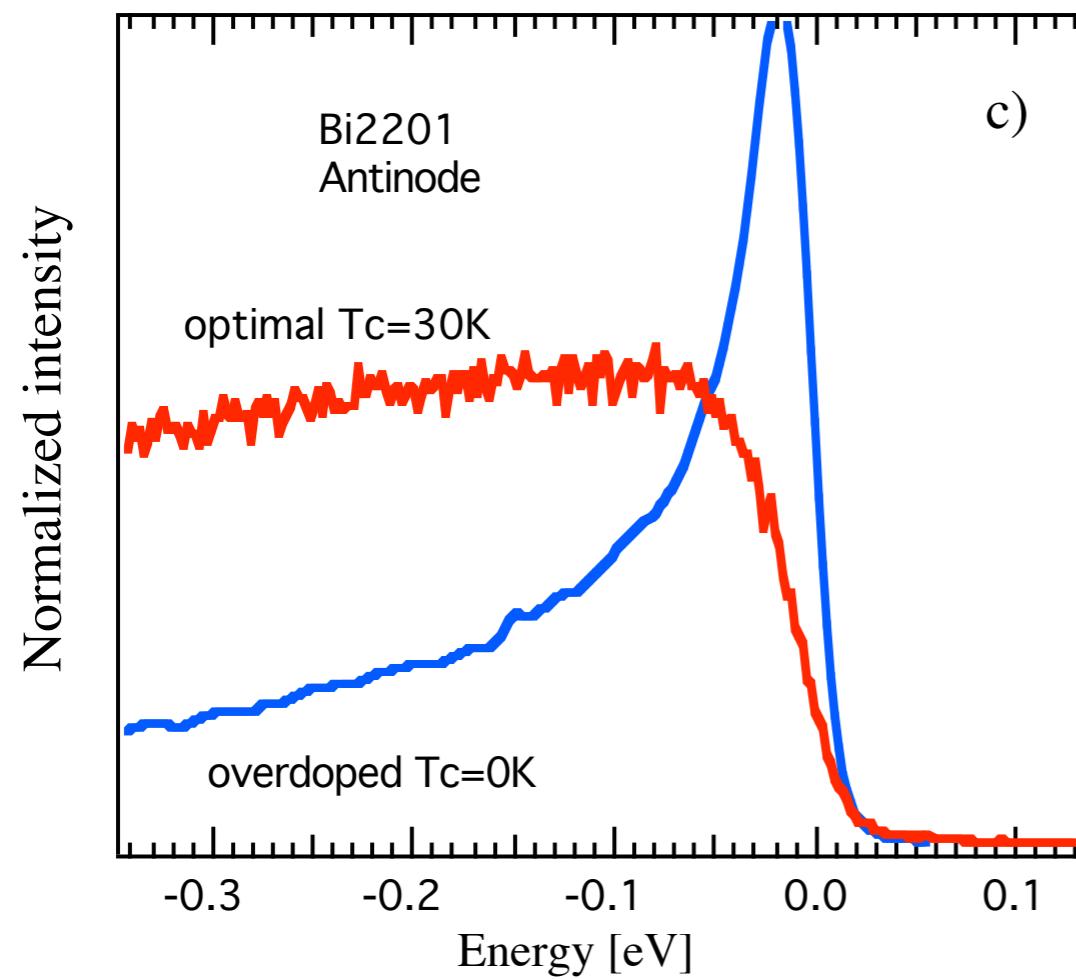


lorentzian

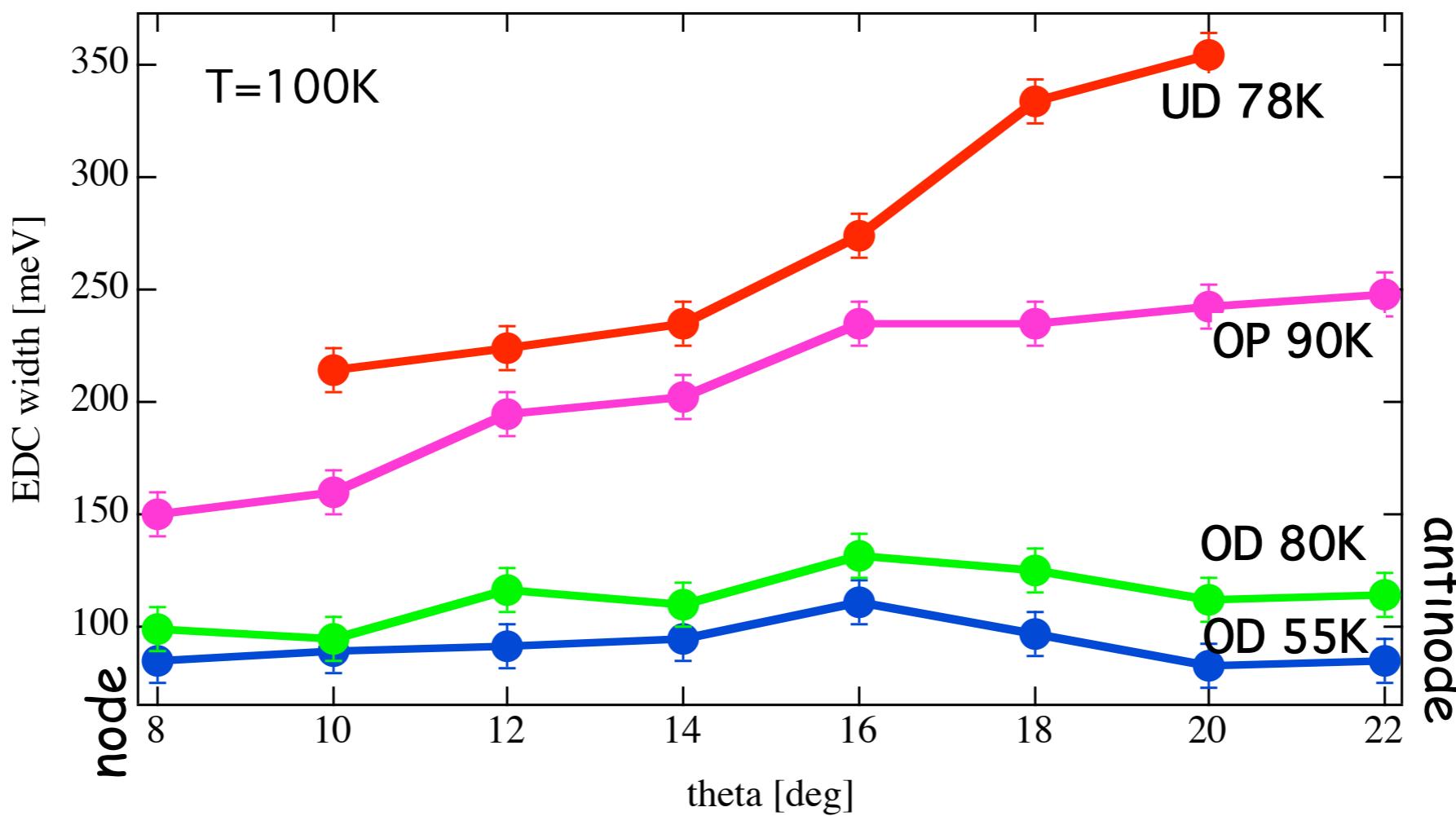


# Momentum anisotropy of the scattering rate

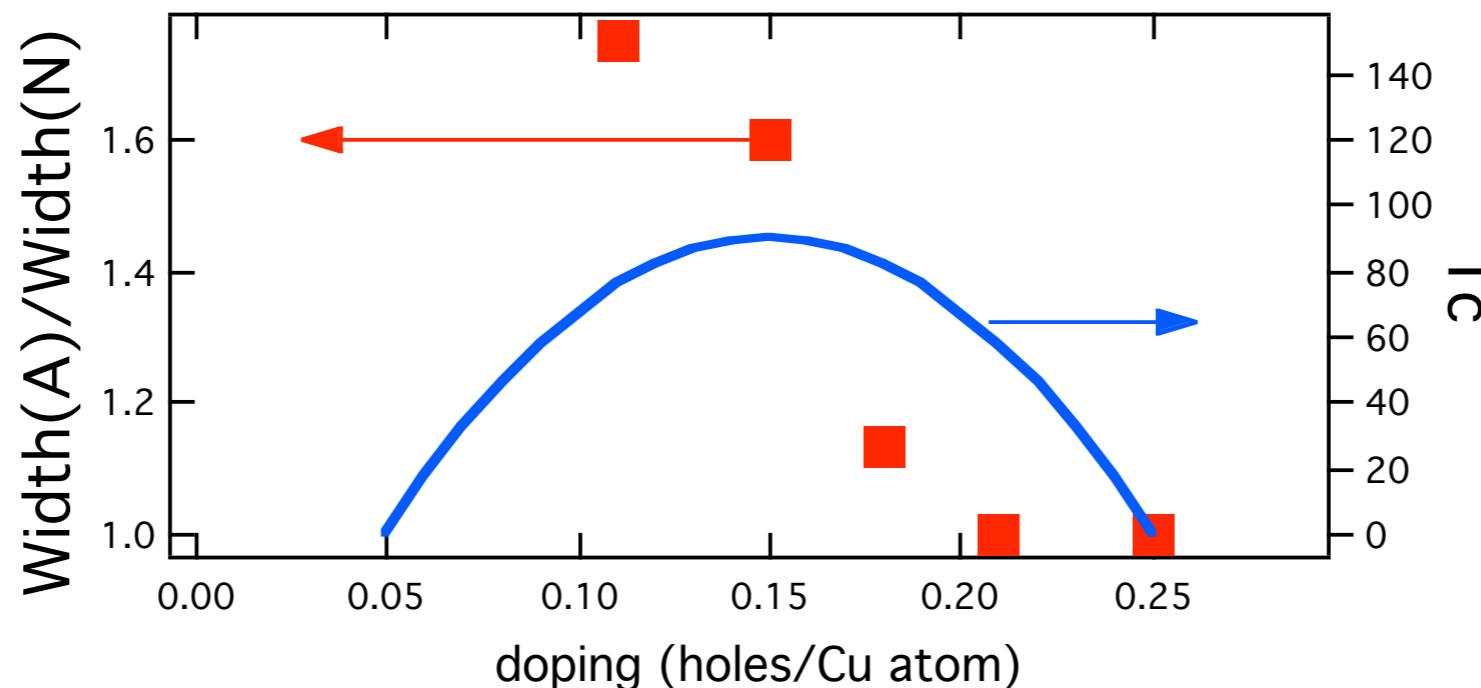




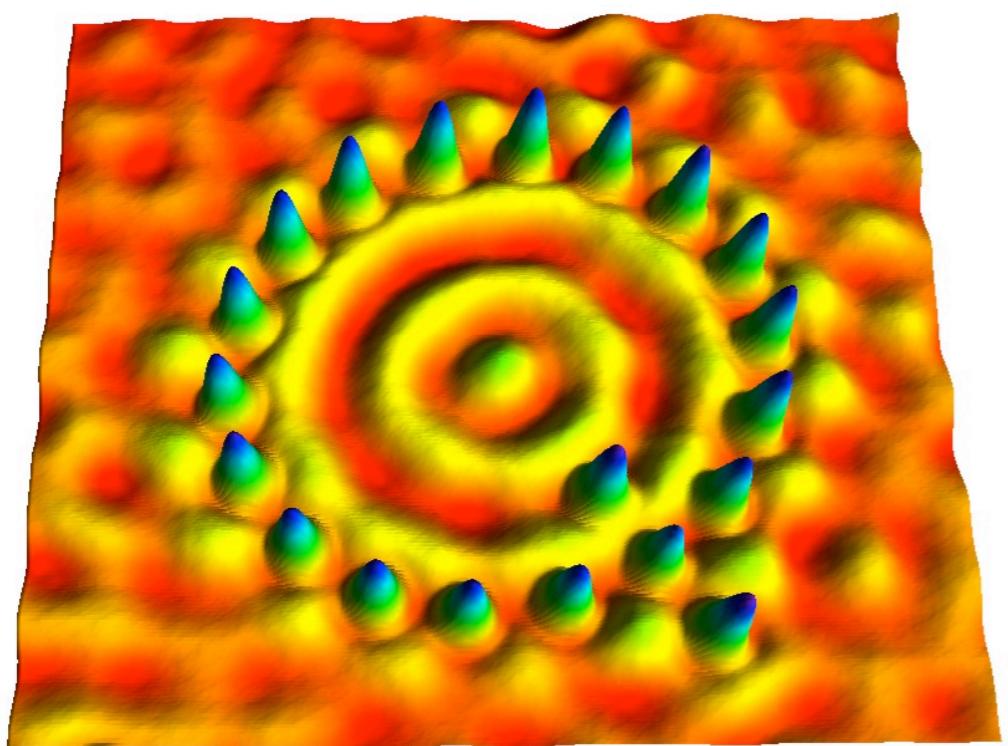
# EDC width around the Fermi surface



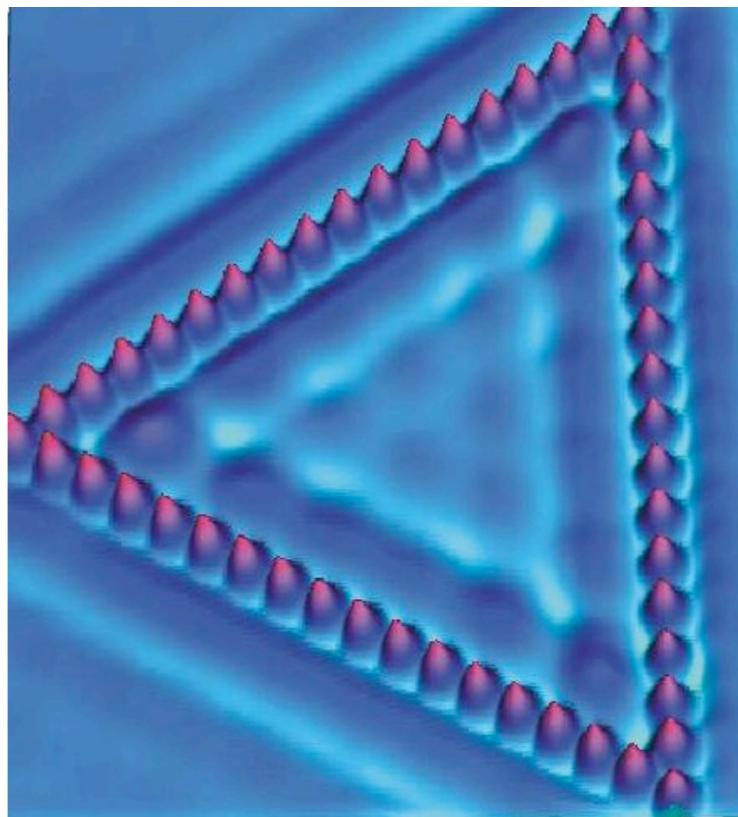
## doping dependence of the anisotropy



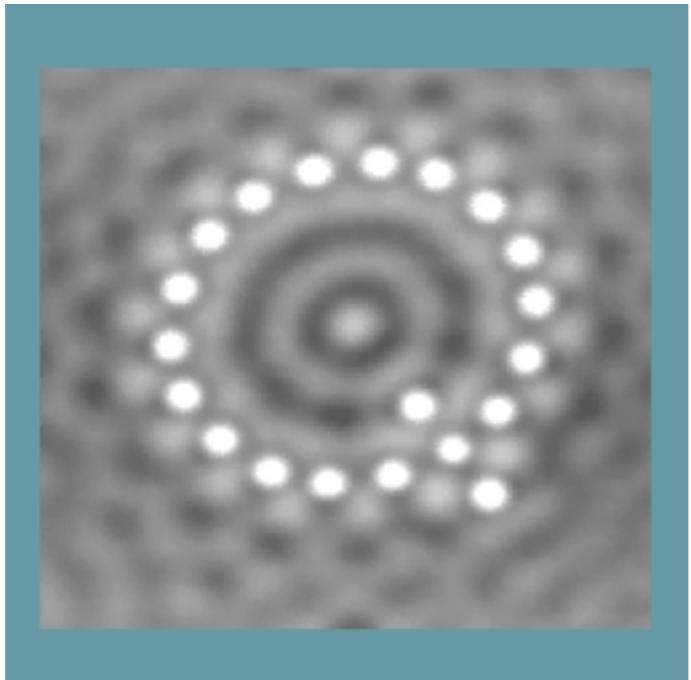
# Scattering in traditional STM



Cu on Cu(111)

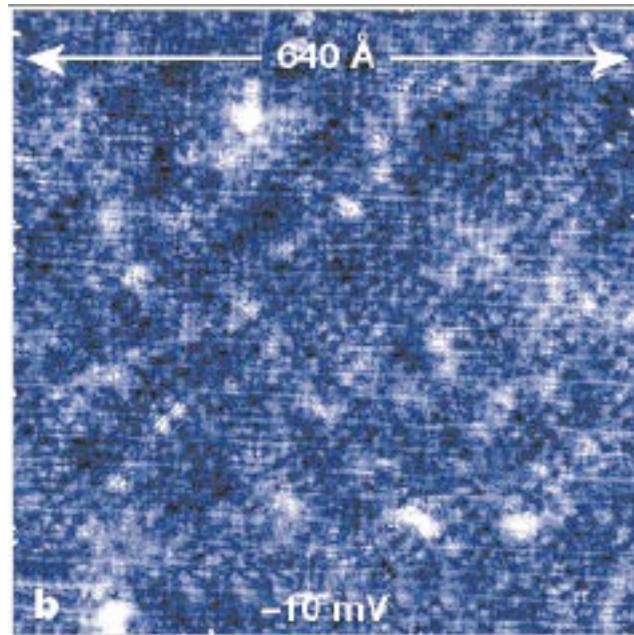


Ag on Ag(111)

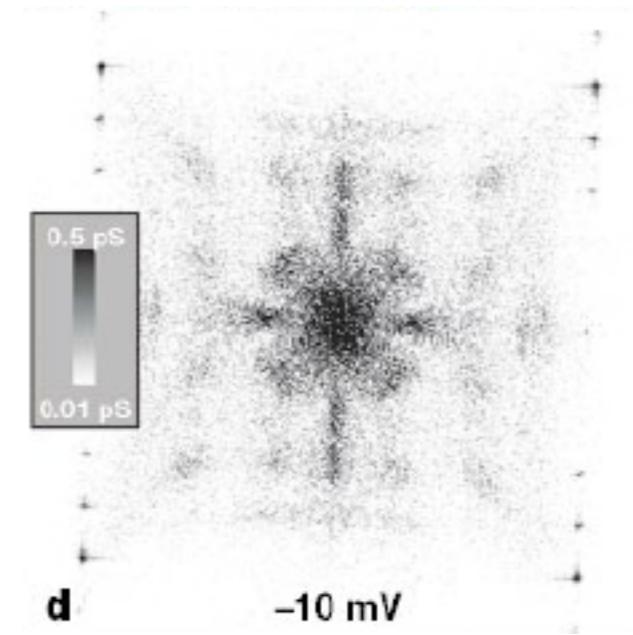


9K => 12K

# Fourier Transform STM (FT STM)



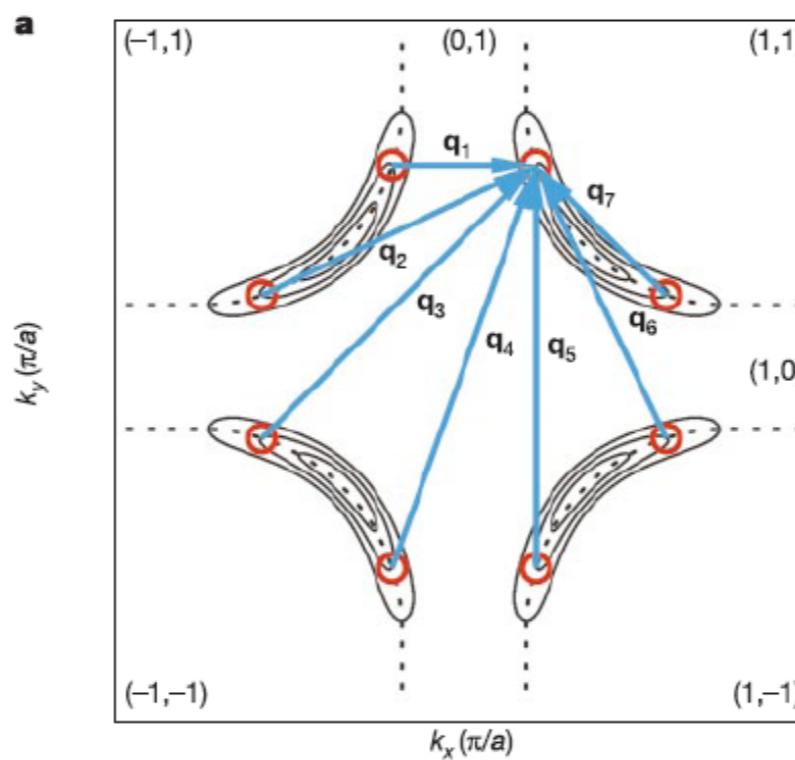
Fourier transform



J. E. Hoffman et al,  
*Science* **295**, 466 (2002)

J. E. Hoffman et al,  
*Science* **297**, 1148 (2002)

K. McElroy et al,  
*Nature* **422**, 592 (2004)

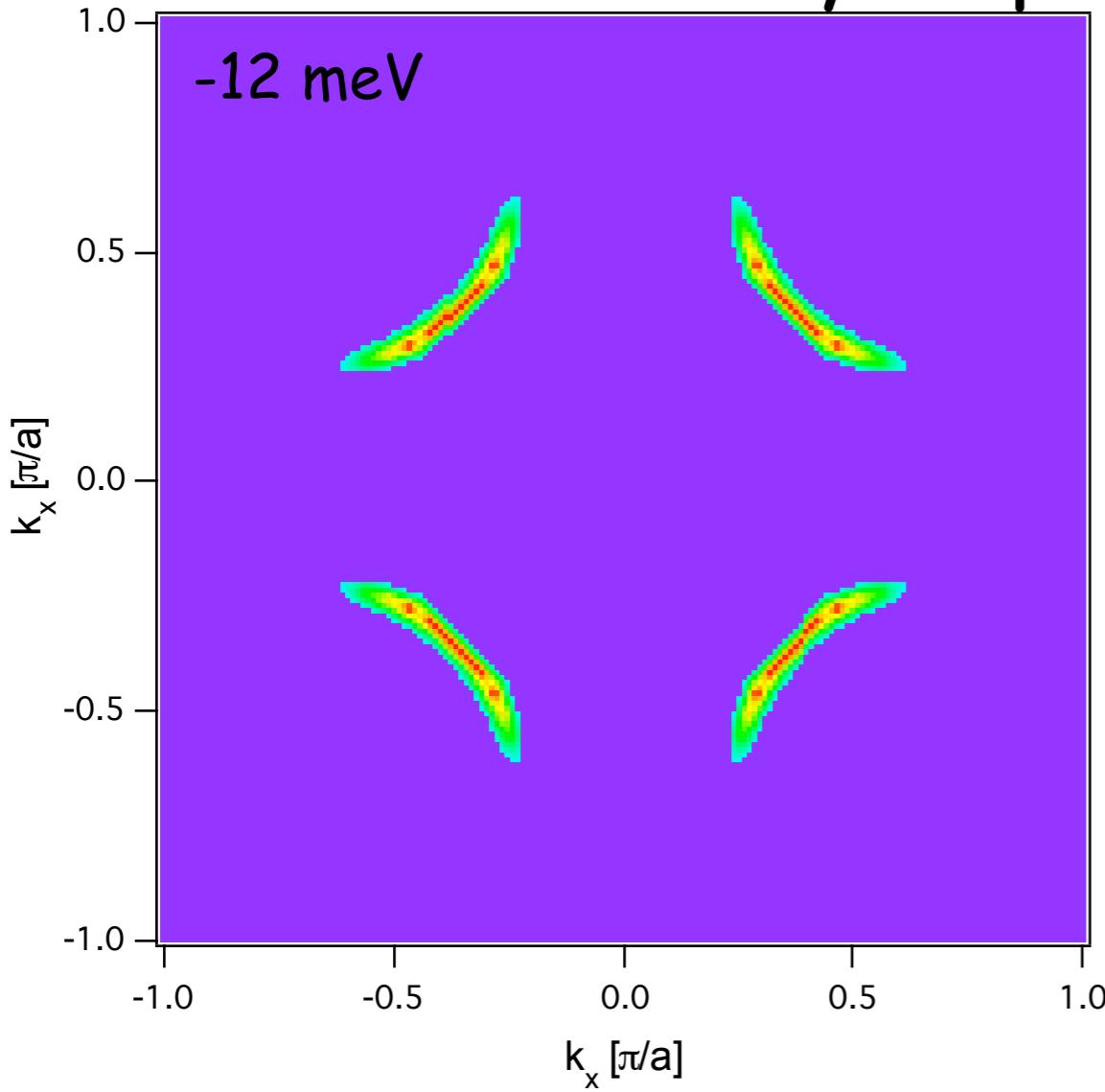


L. Capriotti et al,  
PRB **68**, 014508 (2003)

R. S. Markiewicz et al,  
PRB **69**, 214517 (2004)

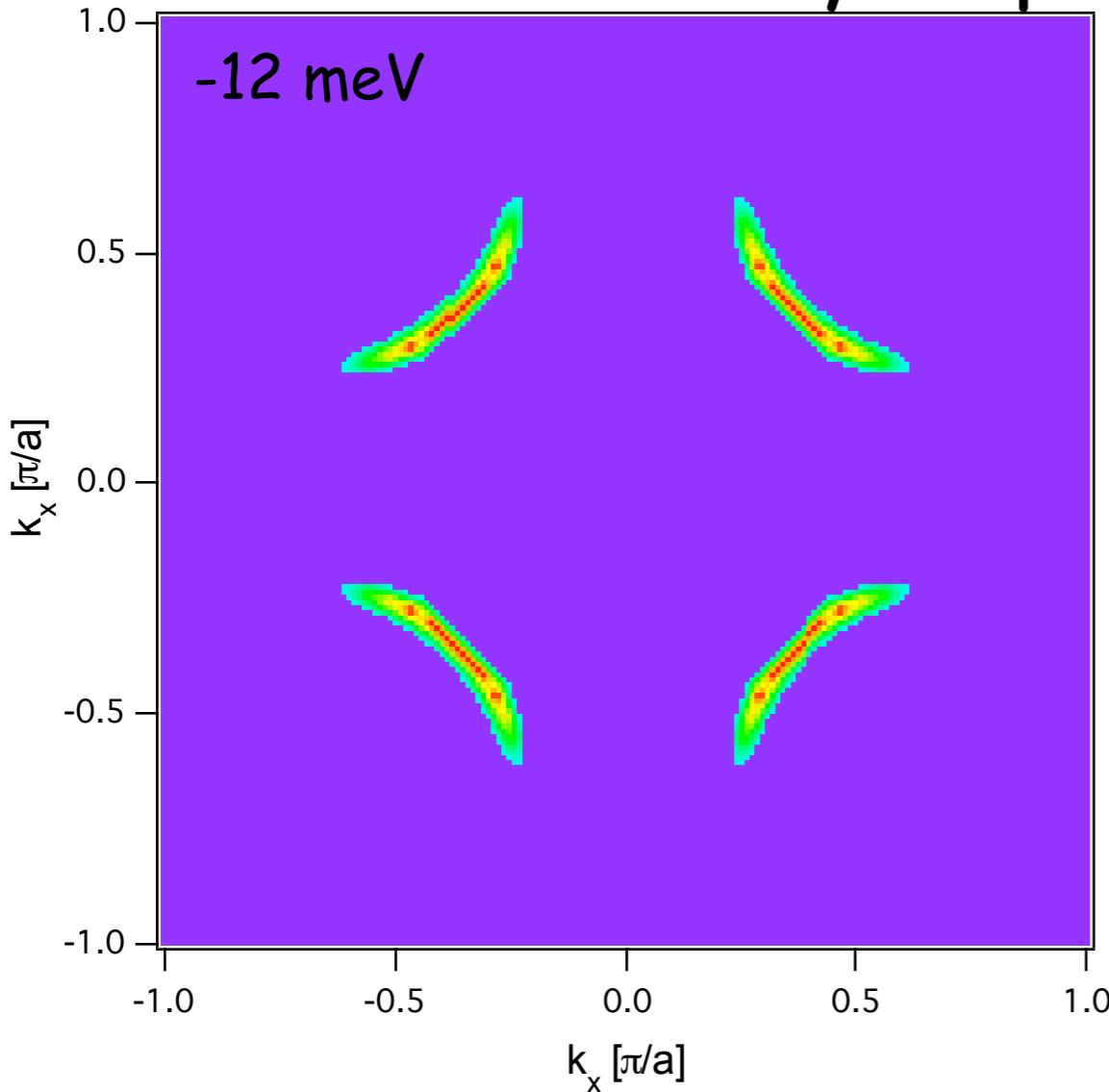
# Probe of scattering processes: AutoCorrelated (AC) ARPES

ARPES intensity map



# Probe of scattering processes: AutoCorrelated (AC) ARPES

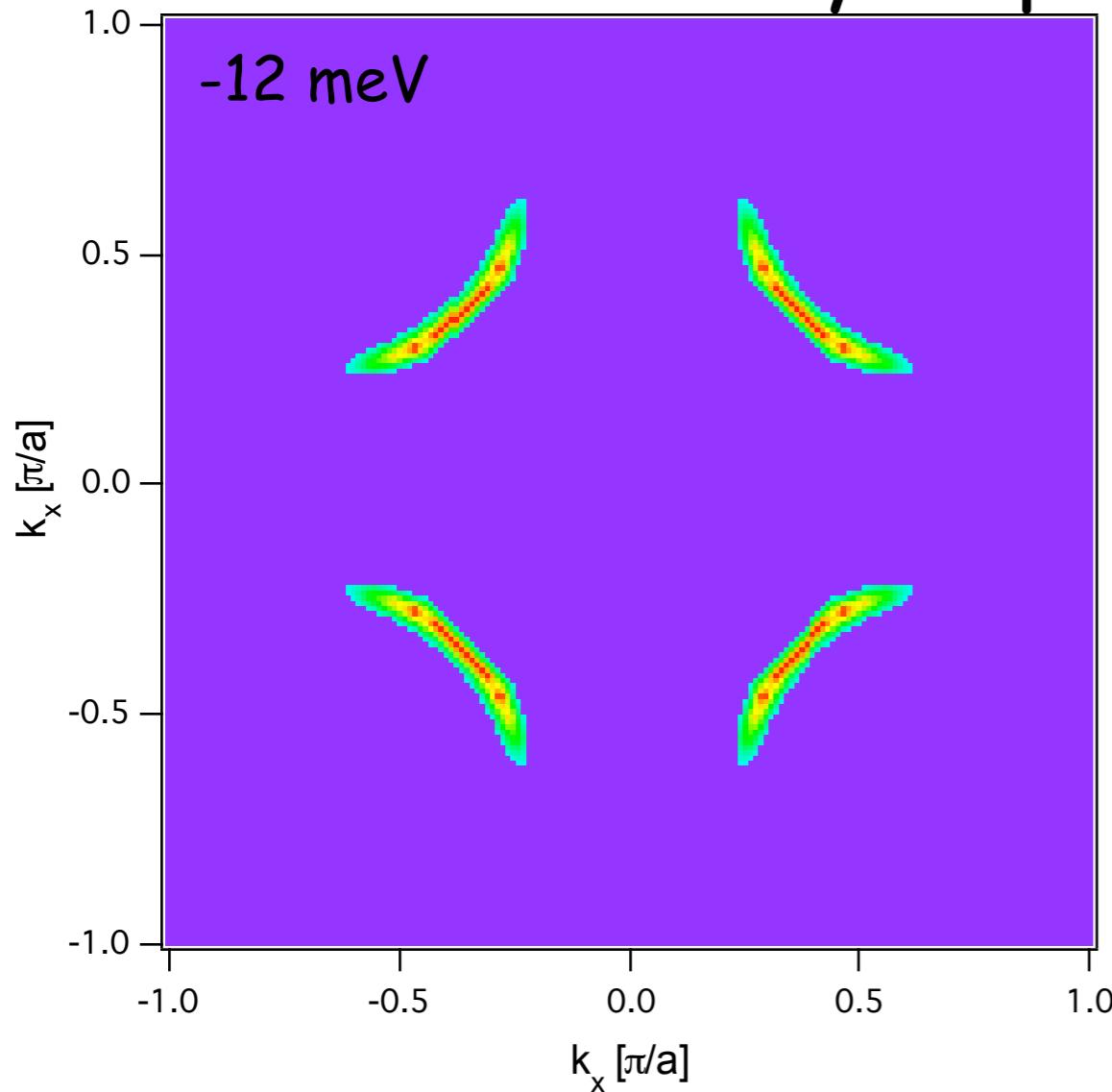
ARPES intensity map



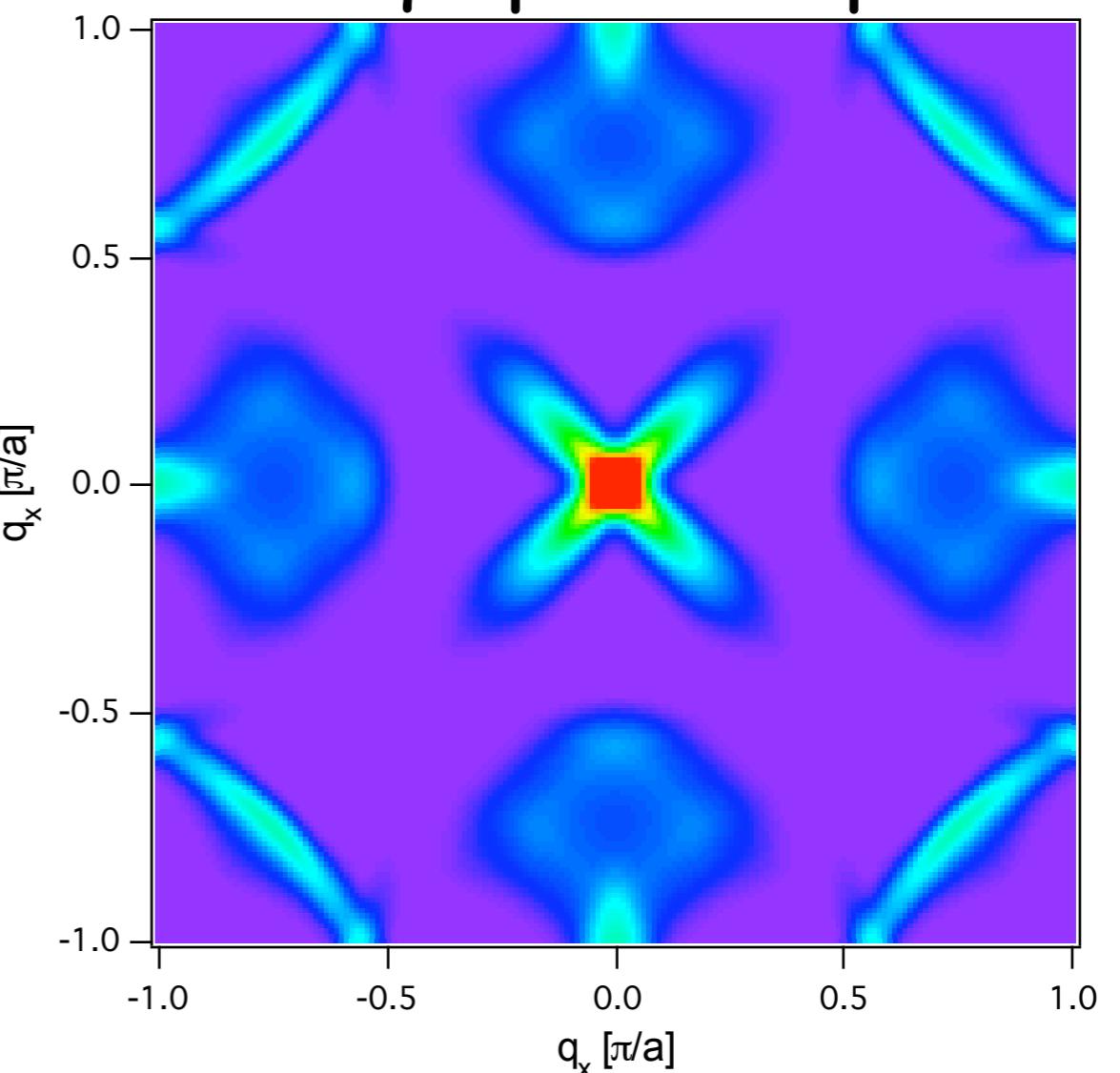
$$S(q, \omega = \omega_0) = \sum_{k_x, k_y} I(k, \omega) I(k + q, \omega)$$

# Probe of scattering processes: AutoCorrelated (AC) ARPES

ARPES intensity map



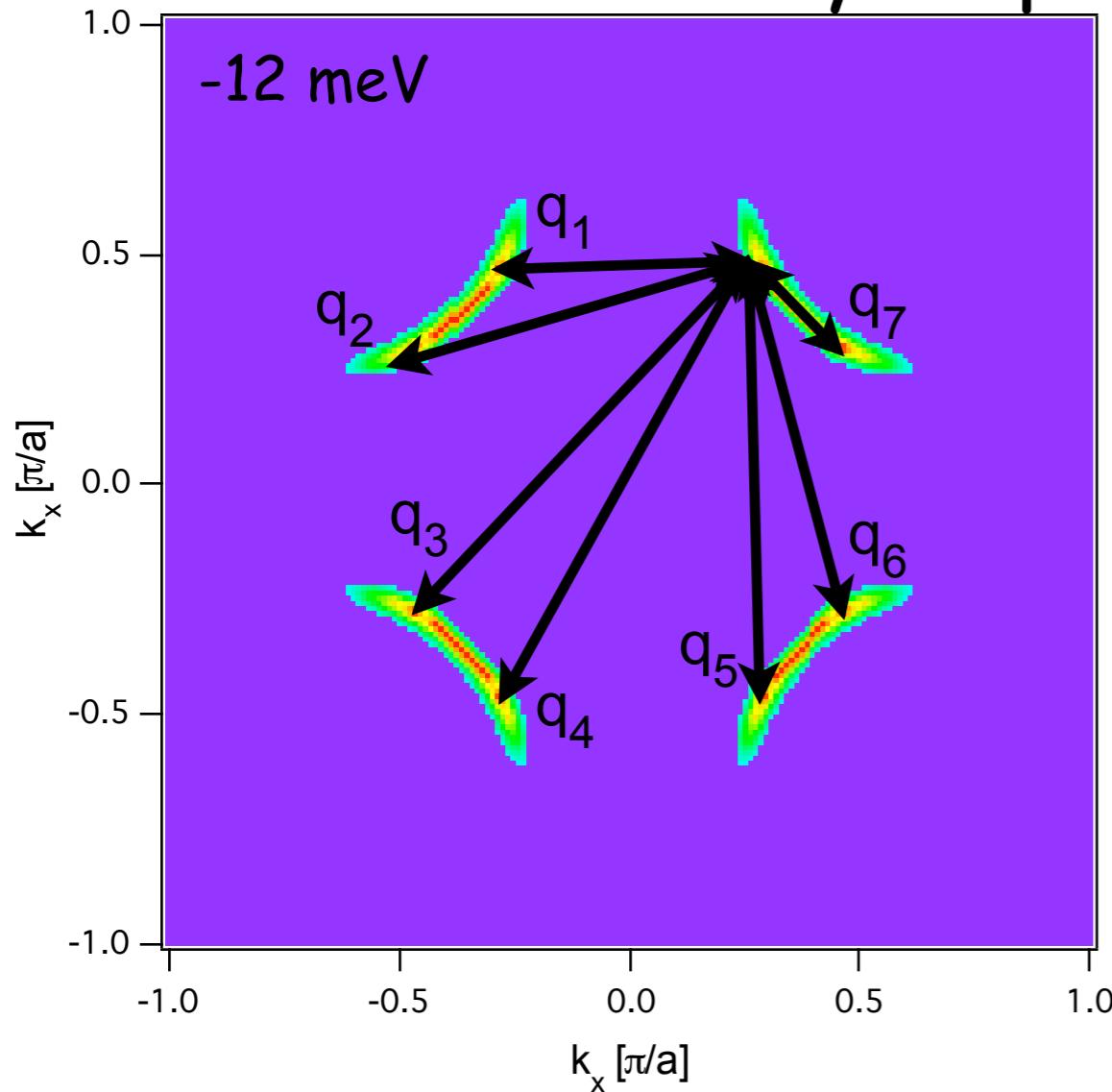
q-space map



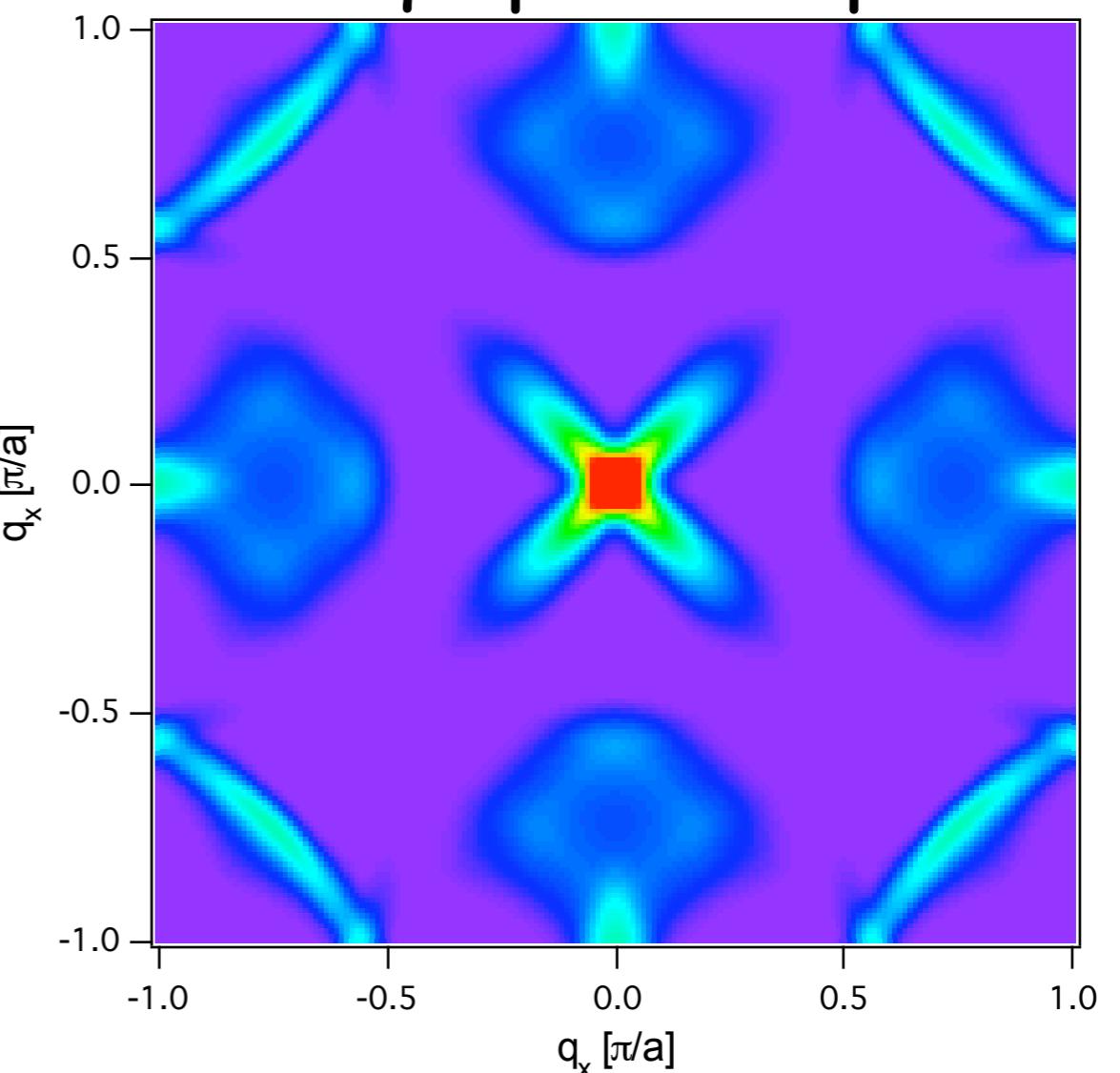
$$S(q, \omega = \omega_0) = \sum_{k_x, k_y} I(k, \omega) I(k + q, \omega)$$

# Probe of scattering processes: AutoCorrelated (AC) ARPES

ARPES intensity map



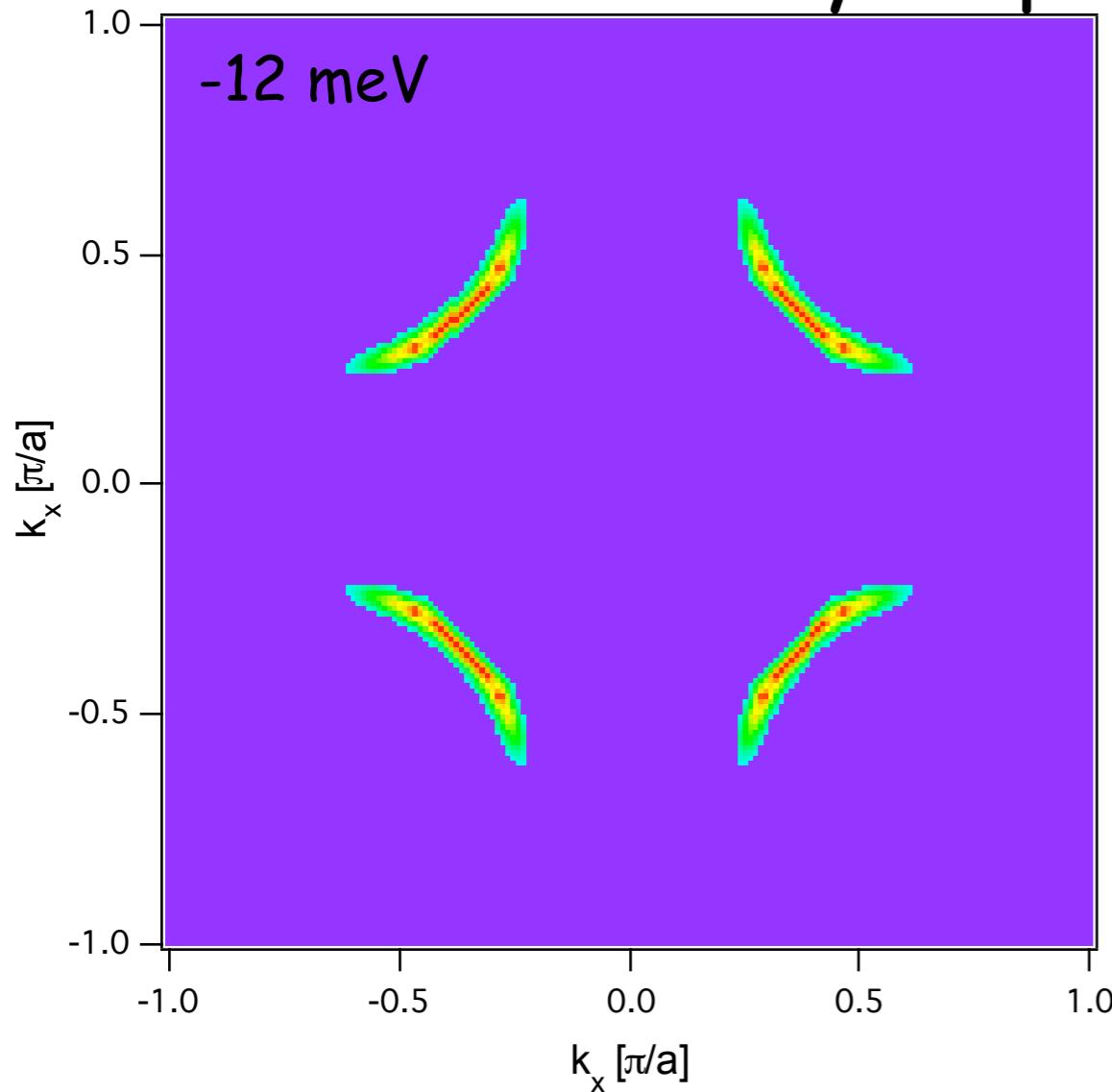
q-space map



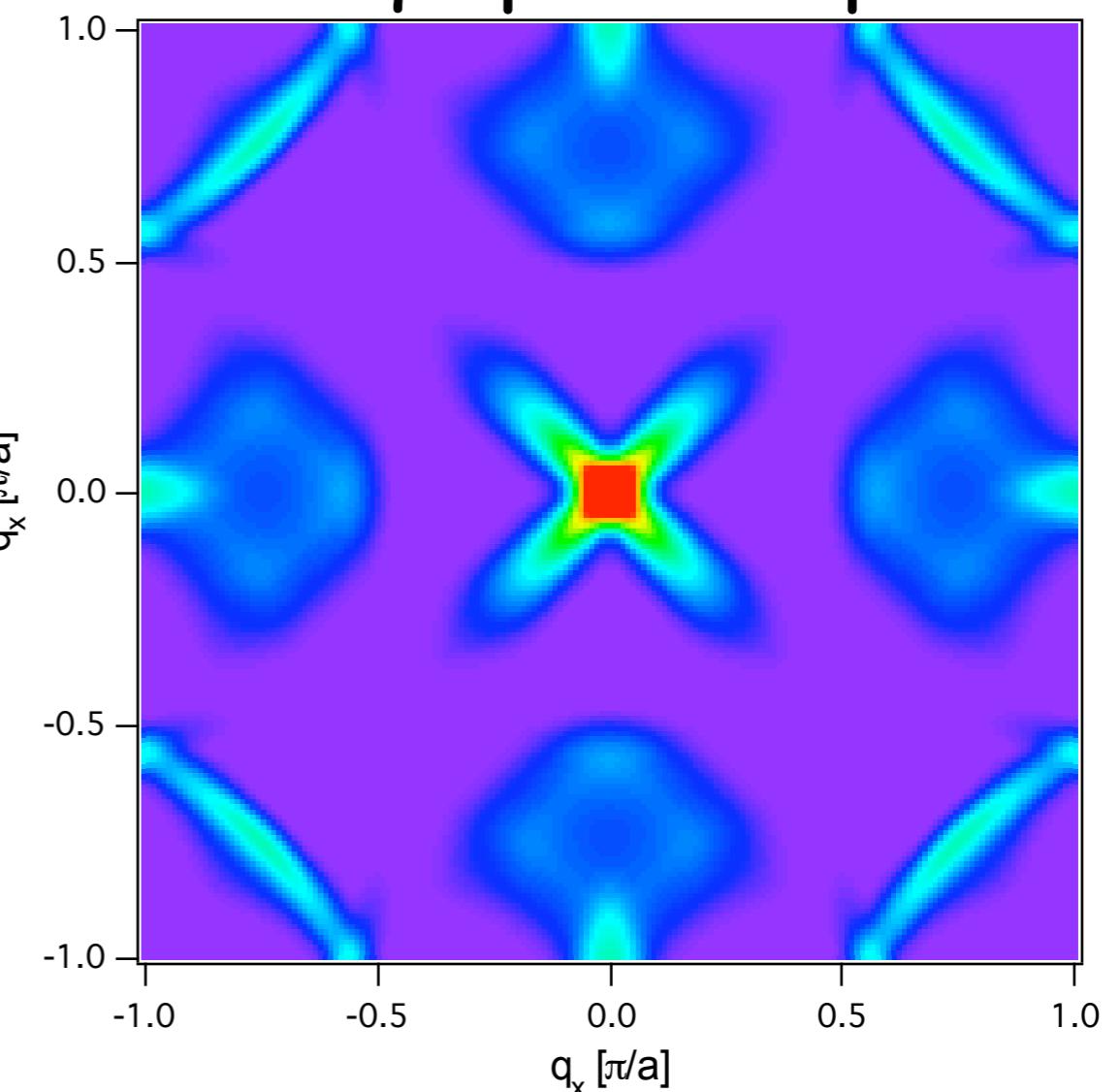
$$S(q, \omega = \omega_0) = \sum_{k_x, k_y} I(k, \omega) I(k + q, \omega)$$

# Probe of scattering processes: AutoCorrelated (AC) ARPES

ARPES intensity map



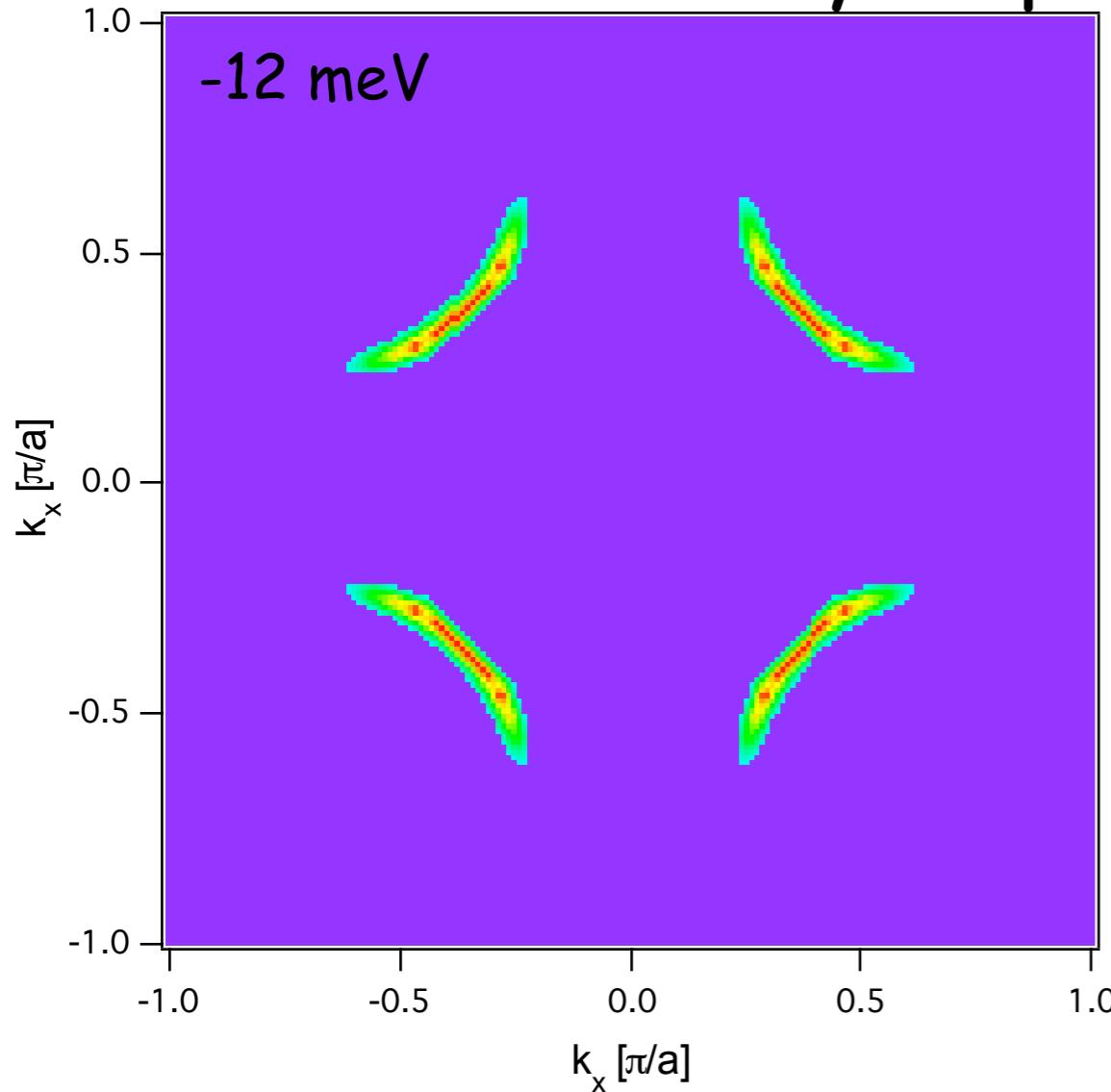
q-space map



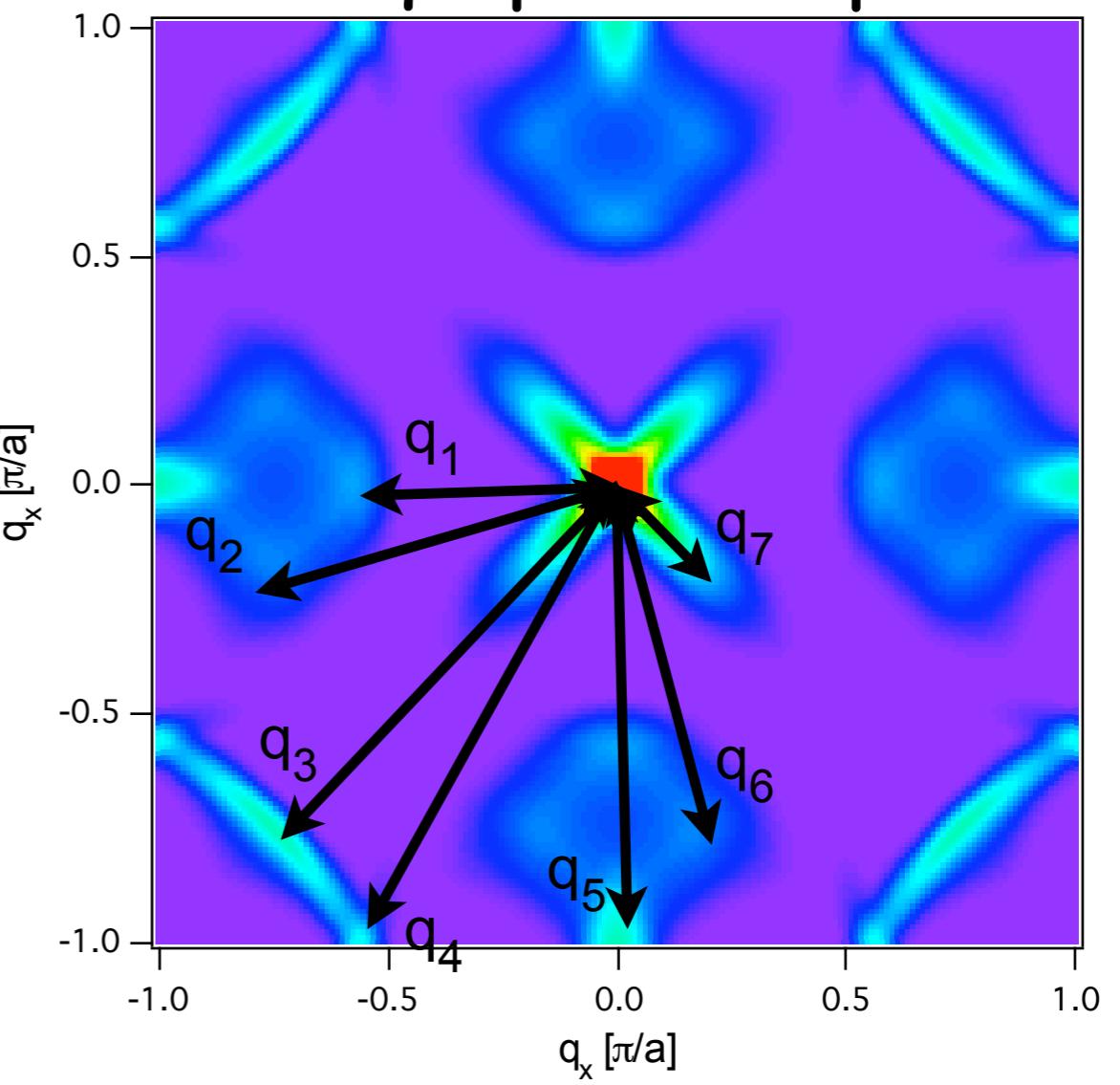
$$S(q, \omega = \omega_0) = \sum_{k_x, k_y} I(k, \omega) I(k + q, \omega)$$

# Probe of scattering processes: AutoCorrelated (AC) ARPES

ARPES intensity map



q-space map

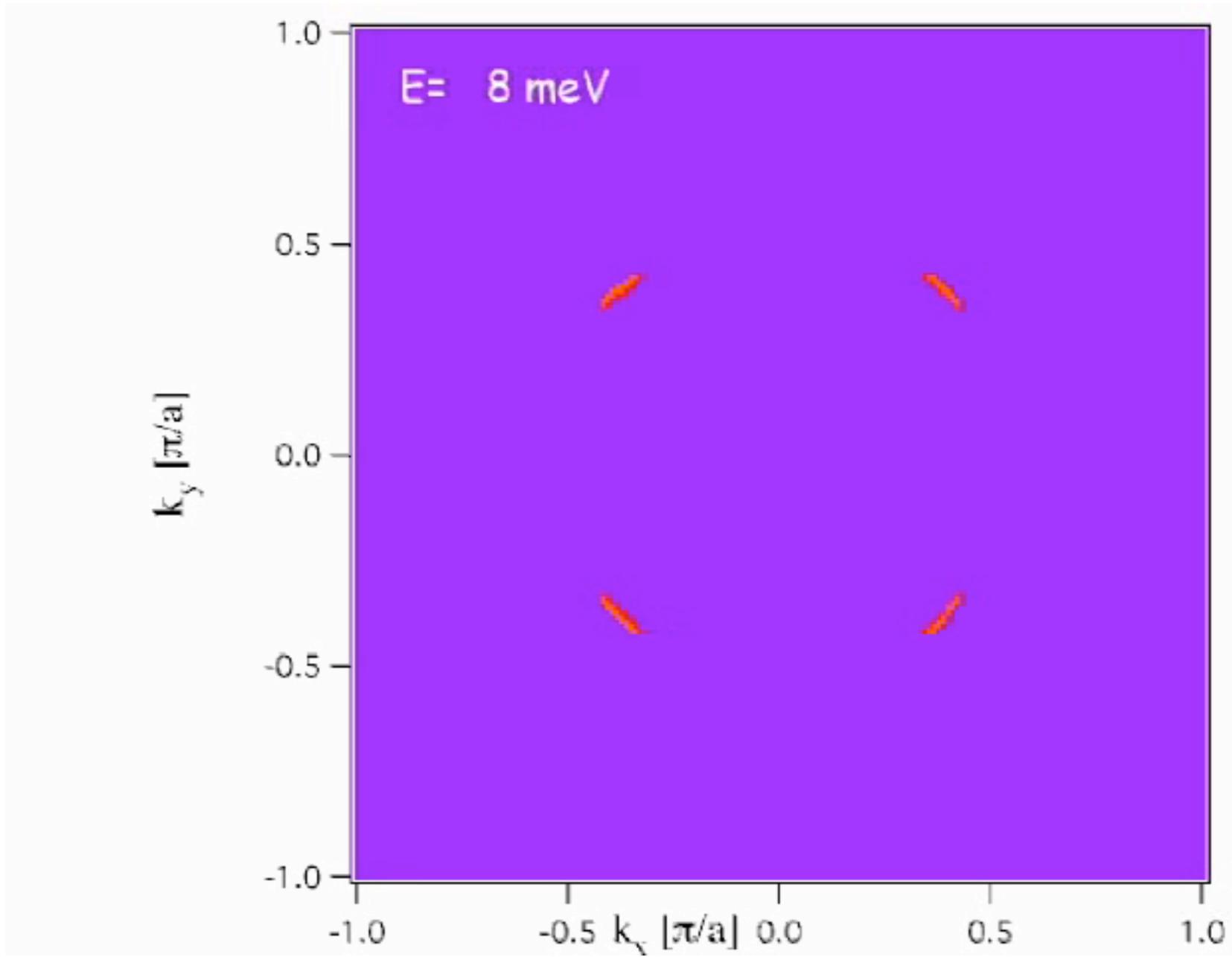


$$S(q, \omega = \omega_0) = \sum_{k_x, k_y} I(k, \omega) I(k + q, \omega)$$

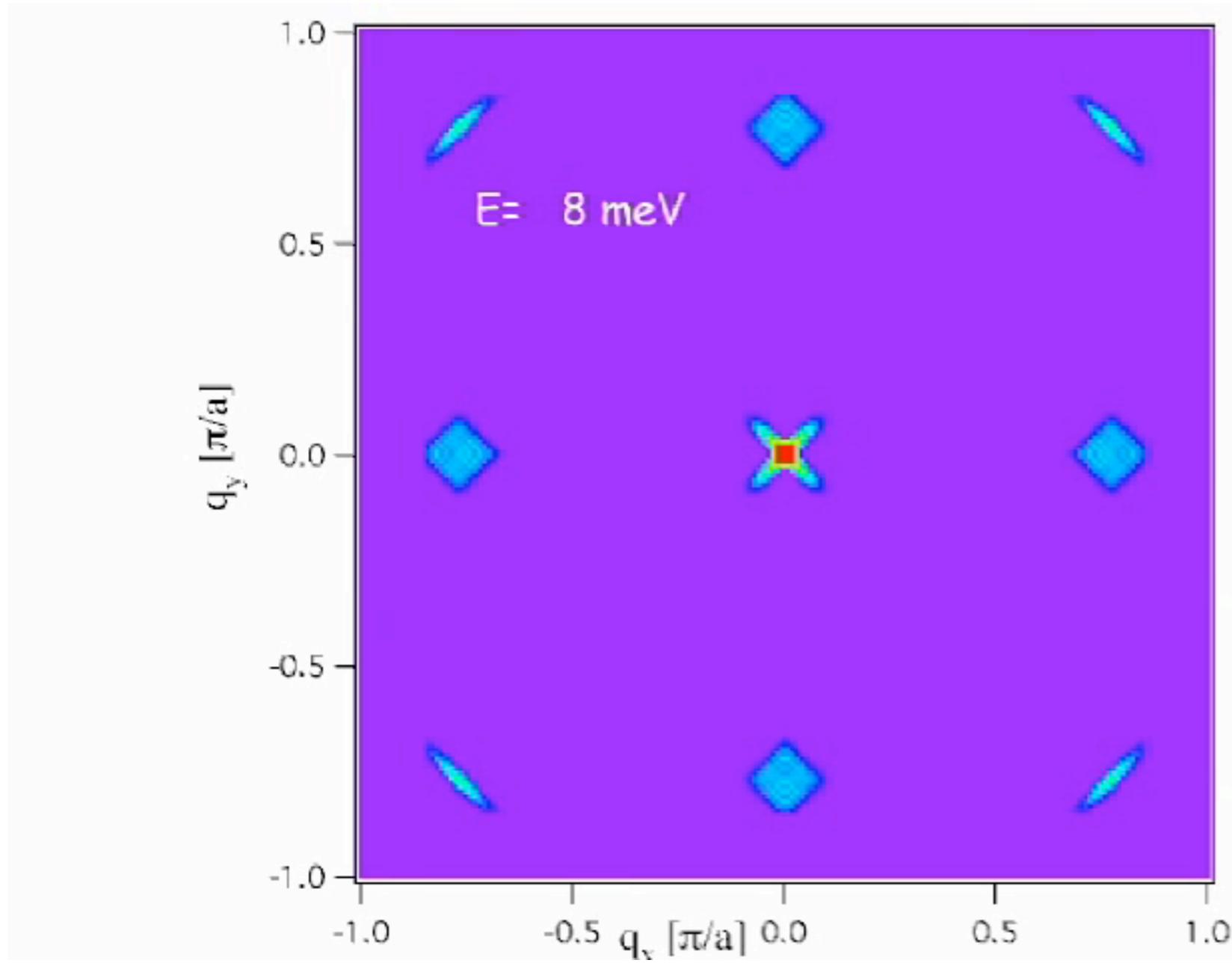
# Scattering maps

- elastic ( $\Omega=0$ ) - analogous to FT STM
- inelastic ( $\Omega \neq 0$ ) - analogous to INS

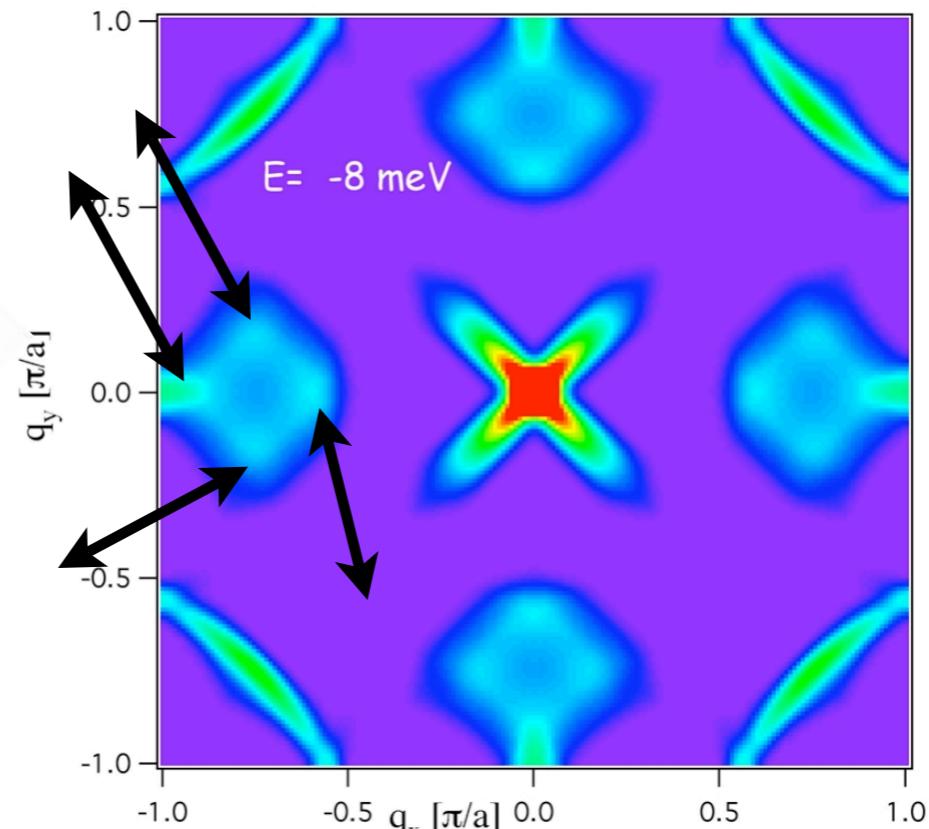
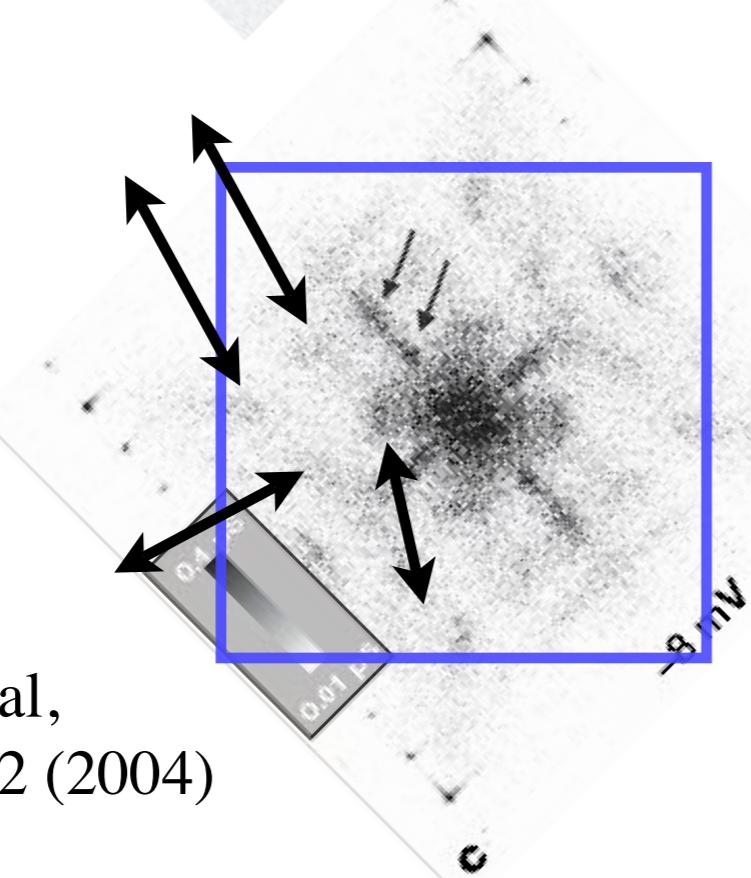
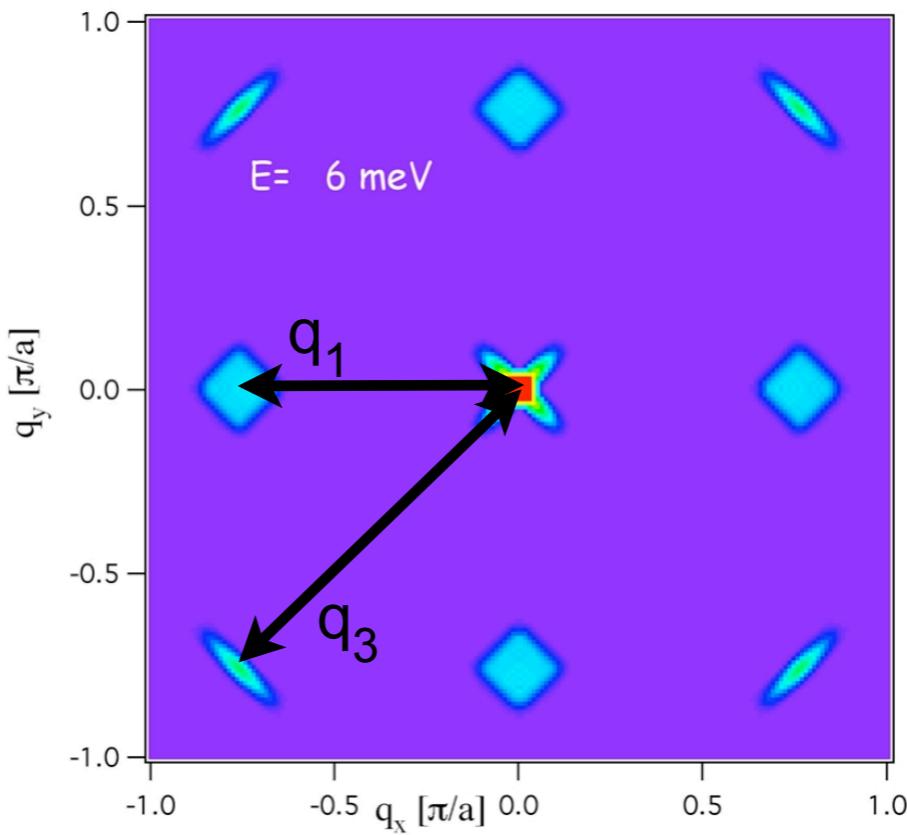
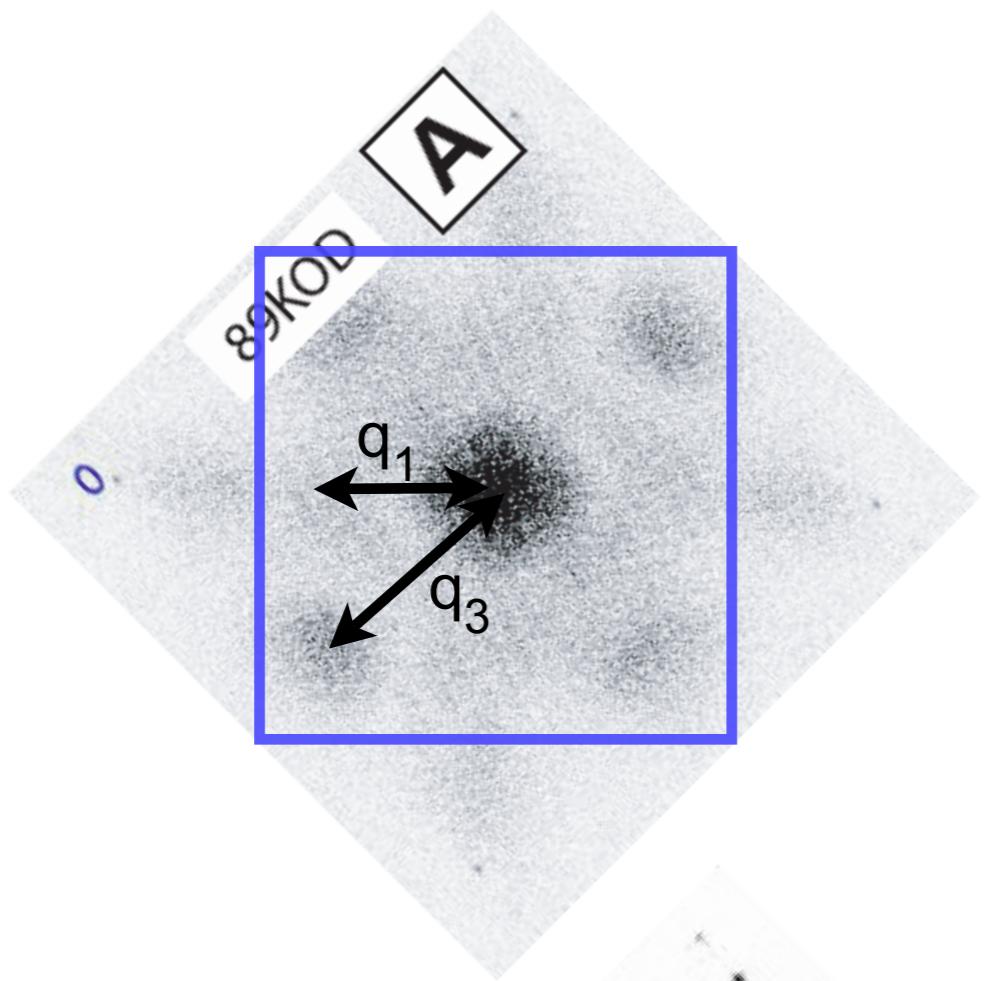
# ARPES intensity maps



# q-space



# Comparison of FT STM and AC ARPES



K. McElroy et al,  
*Nature* **422**, 592 (2004)